## Chapter IV

# Sailcraft Trajectory Options for the Interstellar Probe: Mathematical Theory and Numerical Results 

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## IV. 1 Introduction

Gregory Matloff dealt with the purposes of NASA Interstellar Probe (ISP) in the previous chapters of this report to NASA George C. Marshall Space Flight Center. Les Johnson provided report authors with basic input (Johnson, 2001). Preliminary design of ISP baseline mission and sailcraft systems can be found in (Mewaldt et al., 2000) and (Liewer et al., 2000). This chapter aims at identifying other options for the ISP mission based on solar-sail propulsion. Unavoidably, mission strategies and results are interrelated to the sailcraft technology, in general, and the sail system, in particular. Although literature on solar sailing has been enriching since the Eighties, perhaps the general reader is not full aware of all aspects on advanced space sailing. Thus, we arranged this chapter as follows: §IV. 2 and $\S$ IV. 3 present a background on fast solar sailing and considerations about modeling the translational motion of a sail in space. §IV. 4 focuses on the important topic of optical sail degradation, whereas $\S$ IV. 5 shortly describes the computer code we have employed to get the numerical results presented in §IV. 6 and §IV.7. Considerations on the ISP feasibility and suggestions about some items of next ISP research \& design are given in §IV. 8 and §IV.9.

## IV. 2 Background on Fast 3D Trajectories by Solar Sailing

In this section, we summarize the basics of fast heliocentric sailcraft trajectories by using a formalism developed in the last decade of the $20^{\text {th }}$ century. Details can be found in Vulpetti $(1996,1999 a, 1999 b)$ and the references inside. With regard to nomenclature, symbols will be explained on the way; normally, bold letters refers to as three-dimensional column vectors whereas capital Greek letters denotes matrices, unless otherwise specified. Although the used formalism is coordinate-free, however, we shall use coordinates, implicitly or explicitly, that are defaulted to the Cartesian ones.

### 2.1 Frames of Reference and Units

In the present theory and related numerical code, we use two heliocentric reference frames and one sailcraftcentred frame. The first frame, hereby called the Heliocentric Inertial Frame (HIF), has been built starting from the realization, named the International Celestial Reference Frame (ICRF), of the International Celestial Reference System (ICRS) that is provided by the International Earth Rotation Service (IERS). The strict definition of ICRF and its related documentation can be found at http://www.iers.org. Here, we very briefly report that the origin of the ICRF is the barycenter of the Solar System and its orientation is close to dynamical equinox and mean equator at J2000. HIF has been obtained by rotating the YZ-plane of ICRF counterclockwise about its X-axis by the value of Earth obliquity ( $23^{\circ} 26^{\prime} 21.16^{\prime}{ }^{\prime}$ ) at J2000. HIF is centred on the Sun barycenter and it is oriented close to the dynamical equinox and mean ecliptic at J2000. That is particularly useful when planetary perturbations are included, via standard ephemerides, in the sailcraft motion (as a matter of fact, $a$ priori one does not know whether the sailcraft will be flying-by some planet).
The second frame, hereby named the Extended Heliocentric Orbital Frame (EHOF), is defined as follows:
2D motion in HIF with trajectory curvature supposed not to diverge at any time

1. If motion is direct or counterclockwise (in HIF), then the reference direction \& orientation are those ones of the sailcraft position vector $\mathbf{R}$; the reference plane is given by $(\mathbf{R}, \mathbf{V}), \mathbf{V}$ denoting the sailcraft

[^0]velocity vector, and the Z-axis coincides with the direction \& orientation of the orbital angular momentum per unit mass $\mathbf{H}=\mathbf{R} \times \mathbf{V}$
2. If motion is retrograde or clockwise (in HIF), then the X -axis is the same as in (1), but the Z -axis is oriented opposite to $\mathbf{H}$ and, consequently, the Y -axis is in the semi-plane ( $\mathbf{R},-\mathbf{V}$ ).
3. At some time, say, t* where $\mathbf{H}=\mathbf{0}$ (if any), the Z -axis is the limit of the Z-direction of either (1) or (2) when $t$ approaches $t^{*}$. It is easy to show by considerations of geometry and vector analysis that such a direction, here denoted by $\mathbf{h}^{*}$, exists and is unique.
3D motion in HIF with trajectory torsion assumed to be limited at any time
a. If flight begins with a direct motion (in HIF), then EHOF axes are defined the same way in 2D-1
b. If flight begins with a retrograde motion (in HIF), then EHOF axes are defined the same way in 2D-2.

The direction of the Z-axis is denoted by $\mathbf{h}$, whereas $\mathbf{r}$ is the direction of $\mathbf{R}$. At any time $t$, there is a well-posed triad ( $\mathbf{r}, \mathbf{h} \times \mathbf{r}, \mathbf{h}$ ), which defines the extended orbital heliocentric frame. The attribute extended refers to the fact that a general sailcraft trajectory may be composed of pieces separated by at least one point where the orbital angular momentum vanishes. General discussion on the EHOF can be found in (Vulpetti, 1999a). The case characterized by $\mathbf{H}=\mathbf{0}$ for a finite interval of time can be also dealt with appropriately, but is beyond the scope of this report and the realistic options related to the Interstellar Probe.
The third frame, named the Sailcraft Orbital Frame (SOF), has its origin on the vehicle's barycenter and it is instantaneously at rest, according to Special Relativity (SR). In general, its orientation differs from that of EHOF by an amount due to the aberration of light, which is a first-order effect in speed. For ISP, the orientations of EHOF and SOF are very close to one another.
The computer code described in $\S I V .5$ is fully based on SR. However, we shall use the classical approximation for ISP, here, to simplify presentation of solar sailing theory and discussion/comparison of the results. Evenly, HIF/EHOF-related time and SOF proper time scales can be considered equal to each other. Julian Date (JD) has been used for astronomical events and coordinates such as position and velocity of planets in HIF at different times, whereas sailcraft thrusting and/or coasting time intervals could be specified in either SI seconds or days (1 day $=86400$ SI seconds) or standard years ( 1 standard year $=365.25$ days).

### 2.2 The Lightness Vector Formalism

Let us consider the vector solar-pressure acceleration that acts on the sailcraft center of mass. Think about this vector (1) resolved in EHOF, (2) normalized to the local solar gravitational acceleration. Let us denote it by $\mathbf{L}$ and name it the lightness vector. We call its components the radial, transversal and normal numbers as follows:

$$
\mathbf{L}=\left[\begin{array}{lll}
\lambda_{r} & \lambda_{t} & \lambda_{n} \tag{IV-1}
\end{array}\right]^{\mathrm{T}} \quad \lambda \equiv|\mathbf{L}|
$$

$\mathbf{L}$ is a function of time. Its magnitude is called the lightness number here; it should not be confused with the same-name parameter defined in (Wright, 1993); that one is a particular case of the current $\lambda(\mathrm{t})$ function. The motion of the sailcraft barycenter in HIF can be described by the following system of ordinary differential equations (ODE)

$$
\begin{align*}
\frac{d}{d t} \mathbf{R}= & \mathbf{V} \\
\frac{d}{d t} \mathbf{V}= & -\frac{\mu}{R^{2}} \mathbf{r}+\frac{\mu}{R^{2}} \Phi \mathbf{L}+\left(\sum_{j=1}^{N_{p}} \mathbf{P}_{j}\right) p=  \tag{IV-2}\\
& \frac{\mu}{R^{2}}\left[-\left(1-\lambda_{r}\right) \mathbf{r}+\lambda_{t} \mathbf{h} \times \mathbf{r}+\lambda_{n} \mathbf{h}\right]+\left(\sum_{j=1}^{N_{p}} \mathbf{P}_{j}\right) p \\
\frac{d}{d t} m=- & \dot{m}_{\text {sail ACS }}
\end{align*}
$$

where $m$ is the sailcraft mass, $\mathbf{V}$ its velocity, $R=|\mathbf{R}|$ is the Sun-sailcraft distance; $\mu$ denotes the solar gravitational constant, whereas $\mathbf{P}_{j}$ represents the gravitational perturbation of the j -th of $\mathrm{N}_{P}$ planets on the spacecraft,
according to Celestial Mechanics. The symbol $p$ denotes a switch, either 1 or 0 , for including planetary perturbation(s) or not, respectively. $\Phi$ denotes the matrix of rotation from EHOF to HIF; it is equal to $\left(\begin{array}{ll}\mathbf{r} \mathbf{h} \times \mathbf{r} & \mathbf{h}\end{array}\right)_{\text {HIF }}$, according to what defined in sect. IV-2.1. The scalar differential equation in IV-2 accounts for any mass consumption, for instance due to some small-rocket control of the sail orientation; one supposes that mass is exhausted at zero total momentum in SOF, namely, no residual force acts on the vehicle barycenter.
Some remarks are in order: first, although in principle equation IV-2b may be valid also for an (ideally) rocketcontrolled spacecraft, in practice, however, only a sailcraft is characterized by the fields appearing in the acceleration equation, namely, two conservative fields and one non-conservative (aside from planetary perturbations). Second, if $\lambda$ is sufficiently high, the features of the heliocentric spacecraft trajectory are determined mainly by solar gravity and solar pressure (even though some close planetary fly-by may affect lowspeed trajectory arcs). Third, as such, equations IV-2 do not contain any reference to sailcraft technology; in other words, all sailcraft trajectory classes can be studied by reasoning only in terms of L's magnitude and components. Subsequently, a real mission shall be analyzed by connecting dynamics and vehicle technology (§IV.3). Such observation is particularly important since it allows the analyst to be aware of strong non-linear behaviors that a conventional spacecraft does not have.
From the above observations, it is convenient to focus our attention on the solar fields here for illustrating and discussing solar sailing behaviors. Thus, unless otherwise specified, we refer to the following simplified equations

$$
\begin{align*}
\frac{d}{d t} \mathbf{R} & =\mathbf{V} \\
\frac{d}{d t} \mathbf{V} & =\frac{\mu}{R^{2}}\left[-\left(1-\lambda_{r}\right) \mathbf{r}+\lambda_{t} \mathbf{h} \times \mathbf{r}+\lambda_{n} \mathbf{h}\right] \tag{IV-2A}
\end{align*}
$$

It is a simple matter to show how sailcraft energy and (orbital) angular momentum evolve under equations IV2 A . By introducing the quantity

$$
\begin{equation*}
H=\mathbf{H} \cdot \mathbf{h} \quad \Leftrightarrow \quad \mathbf{H}=H \mathbf{h} \quad H= \pm\|\mathbf{H}\| \tag{IV-3}
\end{equation*}
$$

which is an invariant, named the $H$-function, one gets the following equations for energy

$$
\begin{align*}
& E=\frac{1}{2} V^{2}-\left(1-\lambda_{r}\right) \frac{\mu}{R}  \tag{IV-4}\\
& \frac{d}{d t} E=\frac{H}{R^{2}} \frac{d}{d t} H
\end{align*}
$$

and the following equations for angular momentum and invariant:

$$
\begin{align*}
& \mathbf{H} \times \frac{d}{d t} \mathbf{H}=H \lambda_{n} \frac{\mu}{R} \mathbf{r} \\
& \frac{d}{d t} \mathbf{H}=\frac{\mu}{R}\left(\lambda_{t} \mathbf{h}-\lambda_{n} \mathbf{h} \times \mathbf{r}\right)  \tag{IV-5}\\
& \frac{d}{d t} H=\lambda_{t} \frac{\mu}{R} \quad \Rightarrow \quad \frac{d}{d t} E=\lambda_{t} \frac{H \mu}{R^{3}}
\end{align*}
$$

In words, sailcraft energy depends of the radial number; energy rate does on the transversal number (through equation IV-5c), whereas the normal number drives the angular momentum bending. The evolution of $\mathbf{H}$ does not depend explicitly on the radial number. Equation IV-5c is a basic equation for controlling sailcraft trajectory; trajectory classes depend on the initial invariant value and how it evolves (Vulpetti, 1996, 1997, 1999a). One should note that, unless the analyst knows the vector functions $\mathbf{L}(\mathrm{t})$ and $\mathbf{h}(\mathrm{t})$ in advance, equations IV-2 and IV5 c have to be integrated simultaneously to propagate a sailcraft trajectory. As a point of fact, in general, one does not know whether/when sailcraft may reverse its motion or not.

If vector $\mathbf{L}$ were aligned with the radial direction $\mathbf{r}$, for instance after the sail deployment at some suitable perihelion $R_{P}$ from the Sun, the sailcraft energy change would amount to $\lambda_{r} \mu / R_{P}$; as a result, the hyperbolic excess would be $V_{\infty}=\sqrt{V_{P}^{2}-2\left(1-\lambda_{r}\right) \mu / R_{P}}$. A very good way to get a high cruise speed would be to make a sailcraft with high lightness number and launch it on either parabolic or quasi-parabolic orbit down to $R_{P}$. This results in the following speed

$$
\begin{equation*}
V_{\infty}=\sqrt{[(1+e) \mu / \ell]^{2}-2\left(1-\lambda_{r}\right) \mu / R_{P}} \tag{IV-6}
\end{equation*}
$$

In equation IV-6, $(e, \ell)$ denote the eccentricity and the magnitude of angular momentum, respectively, of the preperihelion orbit. Options for pre-perihelion acceleration have been investigated extensively (Matloff and Mallove, 1983) and summarized critically (Matloff, 2000). One should realize that the value, say, $V_{\infty}^{p}$ obtained from equation IV-6 (or an equivalent one) by parabolic pre-perihelion mode could be taken as a useful reference with which actual fast trajectories may be compared. As a point of fact, one knows that a mission obeying equation IV-6 is somewhat hard to implement, in practice. In addition, one should note that $V_{\infty}^{p}$ represents an upper limit only for supercritical sailcraft (§IV.6).
When perturbations are added to the sailcraft motion, equations IV-4 and IV-5 are to be modified. For instance, the invariant's evolution equation changes to:

$$
\begin{equation*}
\frac{d}{d t} H=\lambda_{t} \frac{\mu}{R}+R \mathbf{h} \times \mathbf{r} \cdot \mathbf{P} \tag{IV-7}
\end{equation*}
$$

In equation IV-7, $\mathbf{P}$ denotes the sum of sailcraft accelerations other than solar gravity and photon-sail interaction. However, a good quasi-optimal profile of a 3D trajectory could be carried out by using the simpler form again, especially around the perihelion.

### 2.3 The Motion Reversal Mode

A sailcraft with $\lambda=\lambda_{r}$ moves on a "generalized" keplerian orbit inasmuch as it senses the Sun with an effective mass equal to $\left(1-\lambda_{r}\right) \mu$. However, there is no way to change energy, according to the last equation in IV-5, since any transversal components of the lightness vector vanishes. Thus, if one wants to increase sailcraft speed, some non-radial control has to be applied. The problem is not simple even because, if any non-radial component of the lightness vector is different from zero, the sailcraft equations of motion admit no Lagrangian. It is possible to show strictly by the theory of Lie Groups that no analytical solution to IV-2A exists (Vulpetti, 2001). However, many important properties and features of solar sailing trajectories can be drawn by analyzing equations IV-2A through IV-5 appropriately.
Let us consider the evolution equation of the invariant. It is easy to recognize that, if the transversal number is negative (and not too low) and the trajectory arc time is sufficiently long, some point can be reached where either $H$ vanishes or achieves a local low minimum (or a local high maximum, if the initial motion is retrograde). It can be proved that the first possibility can arise in 2D motion (Vulpetti, 1997), whereas the second one pertains to either mixed 2D/3D-trajectory arcs or full 3D-trajectory arcs (Vulpetti, 1996, 1999a). Only for special cases, conditions can cast them in simple form such as

$$
\left\{\begin{array}{l}
\frac{1}{2} \leq \lambda_{r}<1  \tag{IV-8}\\
-1<\lambda_{t} \frac{\left(t_{p}-t^{*}\right) \mu}{R_{p} V_{p} R^{*}}<-\frac{R_{p}}{R^{*}}
\end{array}\right.
$$

Here, the lightness vector is assumed constant throughout the flight. The subscript p denotes quantities evaluated at the perihelion, whereas starred quantities refer to the $H=0$ event. Another special case is the mixed 2D/3D trajectory in which one has a piecewise-constant lightness vector. In this case, one gets

$$
\begin{array}{ll}
t \in\left[t_{0}, t_{A}\right] & t_{A}>t^{*}
\end{array}\left[\begin{array}{c}
\lambda_{r} \\
\lambda_{t}  \tag{IV-9}\\
0
\end{array}\right]=\mathbf{L}_{A} \quad \text { (with constraints IV-8) }
$$

A realistic 3D trajectory class shall be dealt with extensively in §IV.3.
Why an analysis on sailcraft mission should consider the option in which the orbital angular momentum of the vehicle may reverse somewhere?
The strict mathematical treatment of the motion-reversal sailing mode is beyond the scopes of this report. Here, we limit ourselves to show what happens semi-quantitatively. Let us begin by calculating the along-track component of the total acceleration, namely, the time derivative of the sailcraft speed

$$
\begin{equation*}
\frac{d}{d t} V=\mathbf{V} \cdot \dot{\mathbf{V}} / V=\left[-\left(1-\lambda_{r}\right) \cos \varphi+\lambda_{t} \sin \varphi\right] \mu / R^{2}+\mathbf{v} \cdot \mathbf{P} \tag{IV-10}
\end{equation*}
$$

In IV-10, the quantity $\varphi: \varphi \in[0,2 \pi), R V \sin \varphi=H$ denotes the generalized angle between sailcraft's position and velocity vectors. $\mathbf{v}$ stands for the direction of $\mathbf{V}$. Note that the normal number does not appear in equation IV-10. If one ignores small perturbations, this along-track quantity vanishes when

$$
\begin{equation*}
\cot \varphi=\lambda_{t} /\left(1-\lambda_{r}\right) \tag{IV-11}
\end{equation*}
$$

For simplifying discussion, let us assume both radial and transversal numbers constant throughout the flight; this means that there are two values of the $j$ angle satisfying equation IV-11 as follows

$$
\begin{align*}
& \left\{\begin{array}{lll}
0<\varphi_{s}<\pi / 2 \\
\pi / 2<\varphi_{s}<\pi
\end{array}\right. \\
& \varphi_{e}=\varphi_{s}+\pi  \tag{IV-12}\\
& \begin{cases}\pi<\varphi_{e}<\frac{3}{2} \pi & \lambda_{t}<0\end{cases} \\
& \begin{cases}\prime 3 \\
\frac{3}{2} \pi<\varphi_{e}<2 \pi\end{cases} \\
& \lambda_{t}>0
\end{align*}
$$

It is possible to show that the angle labeled by $S$ refers to local maximum or minimum of sailcraft speed, occurring at time $t_{S}$, if $I_{t}$ is positive or negative, respectively. Typically, if sailcraft starts from a near circular orbit such as the Earth-Moon barycenter orbit (plus an hyperbolic excess) with a sufficiently positive transversal number, say, $\lambda_{t} \approx \lambda / 3$, it accelerates while increasing its distance from the Sun. Rapidly, it achieves the maximum of speed, then decelerates though it can escape the solar system radially (if the lightness number is high enough). There is no local minimum of speed, since $d V / d t$ is always negative past the maximum. As a point of fact, the invariant $H$ is positive and increases monotonically; consequently, the angle between position and velocity can pass through neither zero nor 180 degrees. In such a trajectory class, $\mathrm{j}_{e}$ does not represent a physical solution. Even more, this happens for slow spiraling-out trajectories (for which $I$ is low), whereupon sailcraft speed changes through local maxima and minima characterized by $\mathrm{j}=\mathrm{j}_{s}$.
A quite asymmetrical situation arises from a sufficiently negative transversal number. Since $H$ may vanish, the $\mathrm{j}=\mathrm{j} e_{e}$ solution can physically exist at some time $t_{e}$. Consequently, one may integrate (the main terms of) equation IV-10 from time $t_{s}$ to time $t_{e}$

$$
\begin{equation*}
\left(V_{\max }-V_{\min }\right) / \mu=-\left(1-\lambda_{r}\right) \int_{t_{s}}^{t_{e}} \frac{\cos \varphi}{R^{2}} d t+\lambda_{t} \int_{t_{s}}^{t_{e}} \frac{\sin \varphi}{R^{2}} d t \tag{IV-13}
\end{equation*}
$$

(The fact we are dealing with the simplified problem of $\mathbf{L}=$ constant (throughout the flight of interest) has been highlighted). If $\lambda_{r}<1$, the first term gives its highest positive contribution when $\varphi \cong \pi$, namely, around a point where the angular momentum is zero or close to zero, whereas the second term is strongly positive when $\varphi \cong 3 \pi / 2$, that is around the perihelion of the reverse motion arc. Around the perihelion, the first integral gives a total vanishing contribution, while the far dominant term is that one related to the transversal number. In addition, perihelion is not the point of maximum speed; in fact, maximum speed is achieved past the perihelion because of $\varphi_{e}>3 \pi / 2$. Thus, sailcraft goes on accelerating for a long (asymmetric) arc of solar fly-by performed by reversing its initial motion. The sailcraft speed amplification may be high indeed, depending on the perihelion and lightness vector. It is an easy matter to show that the escape point $(E=0)$ is achieved before the perihelion. Many other properties of sailcraft trajectories can be inferred by studying trajectory curvature and torsion (Vulpetti, 1996, 1997). Among them, the pseudo-cruise branch is of concern here. It has the following properties: (a) it begins at few AU from the Sun, (b) it passes through the solar system with a small speed decrease, (c) although it is generally lower than $\mathrm{V}_{\text {max }}$, however $\mathrm{V}_{\text {cruise }}$ can be significantly higher that $\mathrm{V}_{0}$, the sailcraft injection speed (close to the mean Earth Orbital Speed, or EOS, that equals 2 p AU/yr). These considerations apply to 2D trajectories for which the normal lightness number is zero. This is an ideal case useful for reference mission: $\varphi_{e}-\varphi_{s}=\pi$. It is possible to prove (Vulpetti, 1999a) that a real 3D reversal trajectory must have both non-radial numbers variable at least in a time interval around the reversal time. Such variability is essential to guarantee the orbital frame to be smooth and to cause motion reversal. Here, $\mathbf{H}$ does vanish, but its magnitude exhibits a local minimum. In such trajectory class, $\varphi(t)$ approaches P closely, then it reverses back to values less than $\mathrm{p} / 2$. One gets $\varphi_{e}+\varphi_{s}=\pi$; when perturbations are active, such relationship is well approximated.
Equation IV-13 admits non-reverse motion solutions, plainly. As a simple good example, one could think of performing an attitude maneuver at some time (to be determined) in the $\left[t_{s}, t^{*}\right.$ ) interval such that $\lambda_{t} \rightarrow-\lambda_{t}$, (the transversal number being high enough as above). Since $H$ remains positive this case, the angle between position and velocity never achieves 180 degrees; thus, the second term in equation IV-13 is dominant and positive again for a long trajectory arc about the Sun. At, say, 1-2 AU another attitude maneuver adjusts the sail orientation in either the inertial or the orbital frame. The cruise speed for this class of direct motion and that related to the motion reversal may be quite comparable in realistic cases; they also depend on the departure planet position and velocity at the sailcraft injection time or epoch.
Both the direct and the reverse motion strategies share a basic rule: if a sufficiently light sailcraft is planned to exit from the solar system with high speed, it has to lose most of its initial heliocentric energy (passing through a minimum) before accelerating fully.
It is not difficult to show that the $H$-reversal class for sailcraft trajectories exhibits large launch windows, from several days to a few weeks, depending on the distant target coordinates. For targets well beyond Pluto, e.g. the heliopause or the solar gravitational lens, wide favorable injection into the solar field repeats on annual basis.
Thus, the motion reversal represents a full mission opportunity, which has the following additional features: confirming/extending the feasibility of a mission from a dynamical viewpoint, examining the critical role of the (external) optical degradation on unconventional sailcraft trajectories. Both points are among the main aims of this report.

## IV. 3 Specifying Sailcraft Barycenter Motion: the Connection Equations

As emphasized above, each component of the lightness vector may act as a dynamical control variable. However, any real $\mathbf{L}$ stems from the actual physical interaction between the solar photons and the sail material and configuration. Such interaction generates a thrust in the sailcraft frame of reference. Thus, there is a link between the direct control variables/parameters of the sailcraft and L's components. We call them the connection equations. Moreover, such equations contain geometrical/physical features of the source(s) of light
and environment-related effects. Here, we shall, very briefly, report sailcraft-related phenomena and sourcerelated perturbations. Very extensive explanations of photon-metal interactions, both from physical and mathematical viewpoints, can be found in many excellent classical textbooks on optics. A sailing-oriented description of the solar radiation pressure can be read in (McInnes, 1999, chapter 2). Intrinsic and environmentinduced changes of the ideal sail behavior will be mentioned in §IV.4.
In terms of radiant flux, 99 percent of the solar spectrum ranges from $1000 \AA$ to $40,000 \AA$ in wavelength that can affect space sailing. The light a sail receives can be specularly reflected, diffusely reflected, absorbed, transmitted. A good solar sail should exhibit vanishing transmittance ${ }^{2}$, low absorptance (a), low diffuse reflectance $(d)$ and high specular reflectance $(r)$. Therefore, $r+d+a=1$, a condition well achieved even by very thin Aluminium-Chromium films. For the moment, we only mention that such optical quantities are someway averaged over the essential solar spectrum. We shall return on that below. In general, the local solar radiant flux impinges onto the sail surface at an angle $\mathbf{q}$ of incidence, as seen from the sailcraft. (If $\alpha_{n}$ and $\delta_{n}$ denote the azimuth and elevation in EHOF, respectively, of the sail axis $\mathbf{n}$, oriented backward with respect to the reflective sail side, then one has $\cos \theta=\cos \alpha_{n} \cos \delta_{n}$ strictly only if the vehicle speed is zero). Specularly reflected light generates (main) momentum along $\mathbf{n}$, while absorption causes a momentum along the incident radiation direction. The process of light diffusion by the sail's front side induces two additional momenta on the sail: the first one acts along the incident direction, the second one is along $\mathbf{n}$ and is proportional to the surface coefficient, say, $\chi_{f}$ (for an ideal Lambertian surface $\chi=2 / 3$ ) and the $d$-value (which, in turn, depends on the sail roughness). The energy absorbed by the sail materials is re-emitted from front-side and backside according to their respective emissivities, $\varepsilon_{f}$ and $\varepsilon_{b}$. We suppose that each sail side behaves as a uniformly diffuse gray surface. Emissivity is only function of the sail temperature: the sail thickness is so small that one can use the same temperature $T_{S}$ across the sail film. This value follows from the equality between absorbed power and emitted power in vacuum at any distance $R$ from the Sun. By neglecting the cosmic background radiation temperature, the absorption-induced thermal effect consists of a net momentum along the normal-to-sail direction proportional to the following factor

$$
\begin{equation*}
\kappa=\frac{\chi_{f} \varepsilon_{f}\left(T_{s}\right)-\chi_{b} \varepsilon_{b}\left(T_{s}\right)}{\varepsilon_{f}\left(T_{s}\right)+\varepsilon_{b}\left(T_{s}\right)} \tag{IV-14}
\end{equation*}
$$

(In equation IV-14, we have highlighted the dependence on sail temperature). The sail of a fast sailcraft should be composed of a high-reflective layer and a high-emissivity coating. As a result, the function k is negative for Aluminum-Chromium sails; in other words, there is a thrust acceleration, along -n, stronger as absorptance and temperature increase. Even this component of the total thrust is not negligible, especially around the perihelion and for a degraded sail.
The above picture of sail-photon interaction is rather simplified. In addition to detailed aspects of this interaction, a more general treatment should include other meaningful items. These ones are photon aberration, features of the light source, curved sail, and optical degradation, in the order, according to the progressive removal of some underlying assumptions such as:
A1. direction of incident light along to the X -axis of the sailcraft frame
A2. point-like Sun
A3. flat sail
A4. ideal optics.
We have mentioned that physics in the spacecraft orbital frame does not coincide with that of the heliocentric orbital frame. By neglecting $2^{\text {nd }}$-order and higher terms in the vehicle speed, it is possible to carry out the following connection equations

[^1]\[

\mathbf{L}=\lambda_{0} n_{x}\left\{\left[\left(2 r n_{x}+\chi_{f} d+\kappa a\right)\left(1-2 \beta_{x}\right)-2 r n_{y} \beta_{y}\right] \mathbf{n}+(a+d)\left[$$
\begin{array}{c}
1-2 \beta_{x}  \tag{IV-15}\\
-\beta_{y} \\
0
\end{array}
$$\right]\right\}
\]

In equation IV-15, we have set
$\boldsymbol{\beta} \equiv \frac{V}{C}\left[\begin{array}{c}\cos \varphi \\ \sin \varphi \\ 0\end{array}\right] \equiv\left[\begin{array}{c}\beta_{x} \\ \beta_{y} \\ 0\end{array}\right], \quad \varphi \equiv \operatorname{angle}(\mathbf{R}, \mathbf{V}), \quad V \equiv|\mathbf{V}|, \quad \lambda_{0} \equiv \frac{1}{2} \frac{\sigma_{c}}{\sigma}, \quad \sigma \equiv \frac{m}{S}$
$\sigma_{c} \equiv 2 \frac{\mathrm{~W}_{1 A U}}{g_{1 A U} C}=0.001538 \mathrm{~kg} \mathrm{~m}^{-2}, \quad \mathrm{~W}_{1 A U}=1367 \mathrm{Wm}^{-2}, g_{1 A U}=0.00593 \mathrm{~ms}^{-2}$
with the sail direction in EHOF given by $\mathbf{n}=\left[\begin{array}{c}\cos \alpha_{n} \cos \delta_{n} \\ \sin \alpha_{n} \cos \delta_{n} \\ \sin \delta_{n}\end{array}\right] \equiv\left[\begin{array}{l}n_{x} \\ n_{y} \\ n_{z}\end{array}\right]$
where $m$ is the (instantaneous) sailcraft mass, S denotes the sail area, C is the speed of light. S is the total vehicle mass divided by the sail area and is usually named the sailcraft sail loading. The quantity denoted by $\sigma_{c}$ is the so-called critical density. Vector $\boldsymbol{\beta}$ accounts for photon aberration, which is linear in the sailcraft speed. The $\kappa$ factor is given by equation IV-14. An important thing to be noted about vector equation IV-15 is that the various optical sail parameters are weighted by quantities of significantly different physical nature. Each optical parameter appears in two independent terms.
Ideally, by a perfectly reflecting planar sail at rest in HIF and orthogonal to the vector position, one would get $\mathbf{L}_{\text {ideal }}=\left[\begin{array}{lll}1 & 0 & 0\end{array}\right]^{T} \sigma_{c} / \sigma$ with the maximum allowed thrust, or equivalently, with a thrust efficiency equal to 1. Thus, in general, sailcraft thrust efficiency can be defined as the actual-on-ideal thrust ratio at any time. It is related to the sailcraft sail loading by the following relationship:

$$
\begin{equation*}
\tau=\lambda \sigma / \sigma_{c} \tag{IV-17}
\end{equation*}
$$

When the sailcraft sail loading equals the critical density, $\lambda<1$ since thrust efficiency is less than unity in any real case.

We have removed assumption A1 in carrying out equations IV-15, which hold for a point-like Sun. If sailcraft comes sufficiently close to the Sun, say, at $R \mathrm{~d} 15 R_{\grave{Y}}\left(1 A U \cong 214.94 R_{\grave{Y}}\right)$, then it begins by sensing the finite size and the limb darkening of the photosphere. They ultimately cause a reduction of the thrust on sail; the nearer the spacecraft is the weaker the thrust is (standing the same sail orientation, distance and speed) with respect to the point-like Sun thrust. Thus, by removing assumption A2 and using the standard gray-atmosphere model, it is possible to carry out exact formulas for an arbitrarily oriented sail (and in relativistic motion too). A modern symbolic-math system on computer is appropriate for achieving this goal. Closed-form solutions are very long. However, we like to report simple classical-dynamics formulas without any terms in vehicle velocity for isolating the mentioned effects on the sail. This results in the following modified connection equations:

$$
\begin{equation*}
\mathbf{L}=\lambda_{0}\left(\left[2 r u_{1}+\left(\chi_{f} d+\kappa a\right) u_{2}\right] \mathbf{n}+(a+d) \mathbf{w}\right) \tag{IV-18}
\end{equation*}
$$

In equations IV-18, we employed the following definitions:

$$
\xi \equiv R / R_{\ddot{Y}} \quad \mathbf{u}_{z} \equiv n_{x} \mathbf{w}^{T} \equiv-\frac{1}{192 \xi}\left(2 n_{x} \mathbf{k} \quad n_{y} \mathbf{q} \quad n_{z} \mathbf{q}\right)
$$

$$
\begin{aligned}
& u_{1} \equiv\binom{2\left(59-9 n_{x}^{2}\right) \xi^{2}-64 \xi \sqrt{\xi^{2}-1}+2\left(3 n_{x}^{2}-1\right)\left(9+16 \sqrt{1-1 / \xi^{2}}\right)+}{+9\left[\left(n_{x}^{2}-3\right) \xi^{3}+2\left(n_{x}^{2}+1\right) \xi+\left(1-3 n_{x}^{2}\right) / \xi\right] \ln \frac{\xi+1}{\xi-1}} / 192 \\
& \mathbf{k} \equiv 9\left(\xi^{2}-1\right)^{2} \ln \frac{\xi+1}{\xi-1}+32\left(\xi^{2}-1\right)^{3 / 2}-2\left(25 \xi^{2}+9\right) \xi \\
& \mathbf{q} \equiv 9\left(3 \xi^{4}-2 \xi^{2}-1\right) \ln \frac{\xi+1}{\xi-1}+32\left(2 \xi^{2}+1\right) \sqrt{\xi^{2}-1}-2\left(59 \xi^{2}-9\right) \xi
\end{aligned}
$$

Obviously, even though sunlight distribution has a cylindrical symmetry in this model, a non-radially oriented sail destroys this symmetry in generating thrust. If the sailcraft moves at a distance $\xi \gg 1$, the actual-Sun lightness vector approaches that one from the point-like Sun, as described by equation IV-15 with zero speed. (The general formulas are coincident in the limit of $\xi \rightarrow \infty$ for any sail orientation and velocity, of course). We close this topic here with mentioning a few values for the pure radial case: at $\xi=4$ (that is at 3 solar radii from photosphere), a correction factor equal to 0.9858 should be applied to the point-like model, whereas at $\xi=21.49(0.1 \mathrm{AU})$, the correction factor would amount to 0.99951 . Finally, at 0.2 AU , deviation would result in -0.00012 , namely, about $1 / 4$ of the photon aberration for a sailcraft traveling at such distance with $15 \mathrm{AU} / \mathrm{yr}$.
Now, let us remove the assumption A3 to have a flat sail. Currently envisaged sails may be grouped into two large classes: (I) plastic substrate sails, (II) all metal sails. A representative of class-I is a three-layer sail consisting of a plastic layer of a few microns thick on which thin reflective and emissive films may be deposited (one film per side, typically). Such a sail may be suitable for (many) interplanetary transfers. Class-II regards bilayer sail configuration consisting of reflective and emissive films alone. Since sailcraft of class-II has a sail loading considerably lower than class-I, it would be appropriate for high-speed missions. Photon pressure on a large surface induces a large-scale curvature that, in turn, causes pressure redistribution and thrust decrease. In class-I, curvature increases when sail temperature increases. Depending on the supporting structure, large-stress values can result in small-scale folds in the sail materials known as the wrinkles. One deems that wrinkles may interact with large-scale curvature by producing hot spots. During the Aurora Collaboration (January 1994 December 2000), a few promising experiments (Scaglione, 1999) were performed for getting a light sail for the AURORA concepts of mission to either the heliopause or the solar gravitational lens. The sail would be manufactured in the following multi-layer mode: Aluminum-Chromium-buffer-UVTplastic, where the buffer layer consists of diamond-like carbon (DLC) ${ }^{3}$. UVTplastic stands for plastic substrate transparent to the solar UV photons. Once deployed in a high orbit about Earth, solar UV light reaches the DLC buffer and weakens its chemical bonds at the interfaces such that it and the plastic film soon detach from the Al-Cr layers. Closely related to techniques for achieving metallic sails without infrastructures in orbit, are the deployment and the sailkeeping methods. The AURORA collaboration studied a circular Al-Cr sail to be deployed in orbit by a small sail-rim-located torus. This is a hydrostatic beam-based deployment system with load-supporting web (Genta et al., 1999); deployment is effected by inserting gas into this peripheral ring. The sail shall take a pillow-like shape, symmetric with respect to the sail axis, with a maximum axial shift depending on the Sun-sailcraft distance (and sail orientation). For instance, a circular sail of $300-\mathrm{m}$ radius exhibits maximum slope of 4.4 degrees at a perihelion as low as 0.15 AU (or, equivalently, a sunward shift of 14 m ). Large-scale curvature radius takes on 3.3 km , by entailing a thrust reduction factor of about 0.998 (with respect to the ideal case of flat sail). These figures would hold only around such perihelion distance. Although some differential equations used for this sail deformation analysis are simplified, nevertheless there is a strong indication that the whole flight of smaller-sail AURORA-type spacecraft, designed for higher perihelion ( $R_{P} \geq 0.2 A U$ ), is compliant with the assumption of a large-scale flat sail. This statement is of great concern with regard to ISP, here.
Finally, we shall remove the assumption A4 regarding ideal optics for a sail. Since this is a special topic with strong consequences on dynamics, we shall devote next section to it. However, before proceeding, we have to be

[^2]more precise about the meaning of the optical parameters entering the connection equations. The set $\{r, d, a\}$ represents the fractions of the incident photons that are specularly reflected, diffusely reflected and absorbed, respectively. Although they are not defined as one usually does in Optics, nevertheless they can be related to the strict optical quantities known as the bi-directional spectral reflectance $\rho_{\text {spec }}(\mathrm{L}, \theta,\{p\})$, the directional hemispherical spectral reflectance $\rho_{\text {diff }}(\mathrm{L}, \theta,\{p\})$ and the directional spectral absorptance $\alpha(\mathrm{L}, \theta)$. (The reader may consult some standard handbook such as the Handbook of Optics by Optical Society of America, 2001, http://www.osa.org ). Here, L denotes the wavelength of the incident light, whereas $\{p\}$ emphasizes parameters characteristic of the reflective sail layer. The above reflectance terms are averaged over all possible orientations of the incident electric field. Note that easy measurable quantities are the total spectral reflected light, giving $\rho(\mathrm{L}, \theta,\{p\})$, and the scattered light (via laser, for example). It is possible to show (Vulpetti, 1999b) that the parameters entering the sailcraft motion equations (through the connection equations) have the following meaning
\[

$$
\begin{align*}
& \mathrm{J}=\int_{\mathrm{L}_{\text {min }}}^{\mathrm{L}_{\text {max }}} \mathrm{U}(\mathrm{~L}) d \mathrm{~L} \\
& r=\rho_{\text {spec }}(\theta,\{p\})=\frac{1}{J} \int_{\mathrm{L}_{\text {min }}}^{\mathrm{L}_{\text {max }}} \rho_{\text {spec }}(\mathrm{L}, \theta,\{p\}) \mathrm{U}(\mathrm{~L}) d \mathrm{~L}  \tag{IV-19}\\
& d=\rho_{\text {diff }}(\theta,\{p\})=\frac{1}{J} \int_{\mathrm{L}_{\text {min }}}^{\mathrm{L}_{\text {max }}} \rho(\mathrm{L}, \theta,\{p\}) \mathrm{U}(\mathrm{~L}) d \mathrm{~L}-r \\
& a=1-(r+d)
\end{align*}
$$
\]

In the above equations, $\mathrm{U}(\mathrm{L})$ denotes the spectral radiant exitance of the Sun, which may be assumed as blackbody source with 5777 K , (corresponding to the solar constant value of $1367 \mathrm{~W} / \mathrm{m}^{2}$, §IV.5.4). Wavelength could range from $1,000 \AA$ to $40,000 \AA$ for a number of physical reasons. For a given sail material and film deposition method, entries in the thrust parameter set $\{r, d, a\}$ depend only on the photon incidence angle, though, in some case, some parameter may exhibit a quasi-independence on this angle. Anyway, they are assumed to not change with time. That is what we mean by ideal optics here. Actually, any $d>0$ entails a sort of intrinsic degradation in terms of thrust because of the different coefficients that the specular and diffuse terms have in the connection equations. One needs a device separating these contributions to the total reflectance. Particularly appropriate to the solar sailing thrust modeling is the Scalar Scattering Theory (SST), where the main parameter is the root mean square roughness of the reflective layer, hereafter denoted by d It is closely related to the sail making process that causes irregularities in the deposited Aluminum film, for instance. The underlying assumptions of SST are discussed in (Vulpetti, 1999b) relatively to space sailing. Here, we limit to report the simple equation between total and diffuse reflectance:

$$
\begin{equation*}
\rho_{\text {diff }}(\mathrm{L}, \theta, \delta)=\rho(\mathrm{L}, \theta)\left[1-e^{-\left(4 \pi \frac{\cos \theta \delta}{\mathrm{~L}}\right)^{2}}\right] \tag{IV-20}
\end{equation*}
$$

Total spectral reflectance does not depend on d ; however, light scattering causes specular and diffuse components to be distributed differently. Equation IV-20 shows that diffuse reflectance augments non-linearly with roughness. Strange enough at first glance, $\rho_{\text {diff }}$ achieves its maximum value at normal incidence $\theta=0$. Depending on the actual sail, consequences to sailcraft dynamics could be significant, through equation IV-15.

## IV. 4 External Optical Degradation

Space is known to be a very complex environment that behaves very differently, even as seen from different artifacts and with respect their goals. In addition to classical design items (spacecraft thermal control, spacecraft system \& sub-system protection, payload degradation and so forth), modern objectives regard tests on inflatable structures too (Stuckey et al., 2000). These systems can include different structural elements that have to be capable of tolerating space environment for the time necessary to allow the payload mission. From this point of view, any sail system is a special deployable system. Apart from some simple Russian tests in orbit, a full
preliminary experimental mission sailcraft has yet to be flown (August 2001). There are only very scarce experimental data specifically oriented to solar sailing hitherto. We shall use part of them for exploring consequences on fast sailcraft trajectory such as the ISP's. To this aim, we have to build some model that accounts for the environment a deep-space sailcraft sail is able to sense. Since our interest is in all-metal sails, as explained above, we may focus on two major causes that could induce a decrease of the sail performance, that is a modification of the ideal-optics conditions as stated in §IV.3. These causes are the solar ultraviolet photons and the solar wind particles that will continuously impinge on a space sail. In this current investigation for NASA, it has been agreed that, considering the very limited amount of experimental data, only effects stemming from solar wind should be considered. Nevertheless, we present calculations that should hold even in a next research phase about the influence of the solar UV flux on the mission design of a fast sailcraft, namely a sailcraft flyingby the Sun at low perihelion. By using the concepts of exitance, radiance and irradiance from classical optics, it is a simple matter to carry out the integrated flux of UV photons onto a sail of a sailcraft in the time interval $\left[t_{0}, t\right]$. One gets the energy fluence

$$
\begin{equation*}
\Psi_{U V}=f_{U V} W_{1 A U} \int_{t_{0}}^{t} a(\theta) \frac{\cos (\theta)}{R^{2}} d t \tag{IV-21}
\end{equation*}
$$

Equation IV-21 holds for a sail having absorptance $a$ and distance $R$ from a point-like Sun. UV beam impinges on sail with an incidence angle $\theta$ from the sail normal $\mathbf{n}$. (The relativistic energy shift, sensed in the sailcraft frame, has been neglected). Symbol fuv represents the ultraviolet fraction of the solar constant; it may be easily estimated by the blackbody distribution at 5777 K . For instance, $f_{\mathrm{UV}}=0.122$ over the $1,000-4,000 \AA$ range, namely, $167 \mathrm{~W} / \mathrm{m}^{2}$ of UV flux at 1AU. An important thing to be noted in equation IV-21 is that the absorptance function is not exhaustively given by equations IV-19 as they hold for (time-independent) ideal optics. We shall return on this topic in § IV.4.1 since it regards the lightness vector computation.
As far as the energy deposited by the solar-wind particles on a moving sail, we make some simplifying assumptions here. They are: (i) solar wind flows radially from the Sun with a speed constant from $\approx 20 R_{\hat{\gamma}}$ to the termination shock, (ii) solar-wind number density scales as $1 / \mathrm{R}^{2}$ everywhere in this range of distance, (iii) interplanetary magnetic field does not interact with sail. A few remarks about these points. Solar wind is an expanding momentum-dominated high-conductivity super-alfvénic (pseudo) supersonic collisionless plasma for which a continuum description applies. Very schematically, it may be viewed at large as composed of quiet background plasma of low speed, on which non-radial fast streams of essentially electrons and protons overlap almost periodically. Solar-wind speed changes with the helio-magnetic latitude and reaches a minimum close the interplanetary current sheet. Our assumption (i) is somewhat elementary, but it has the great advantage to make calculations affordable in the context of this report. In contrast, assumptions (ii) and (iii) appear rather realistic also on considering that here one is interested in fast sailcraft receding from the Sun. Thus, in the sailcraft frame of reference, the (differential) flux of proton energy arriving at the sail during the time $d t$ is given by

$$
\frac{d}{d t} \Psi_{S W}=\frac{v_{1 A U} m_{p}\left(W^{2}-2 W V \cos \varphi+V^{2}\right)}{2 R^{2}}\left(\left[\begin{array}{c}
W-V \cos \varphi  \tag{IV-22}\\
-V \sin \varphi \\
0
\end{array}\right] \cdot \mathbf{n}\right)
$$

In equation IV-22, $W$ is the solar-wind speed in heliocentric frame, $m_{p}$ denotes the proton mass and $v_{1 A U}$ represents the (mean) proton number density at 1 AU . The energy per unit area absorbed by the sail in the time interval $\left[t_{0}, t\right]$ can then be written down as

$$
\begin{equation*}
\Psi_{S W}(t)=\int_{t_{0}}^{t}\left(1-y_{p} \varepsilon_{p}\right)\left(\frac{d \Psi_{S W}}{d t}\right) d t \tag{IV-23}
\end{equation*}
$$

In IV-23, $y_{p}$ and $e_{p}$ denote the proton backscattering yield and the proton backscattering energy fraction, respectively. Actually, computation of IV-23 is a long iterative process, which may be simplified by estimating the proton backscattering properties in the energy range related to the sail and sailcraft under consideration. By using a sophisticated Monte Carlo code, such as SRIM 2000 (Ziegler, 2001), it is possible to study the
interaction of protons and Aluminum. We have focused attention on a number of fast sails and missions; for instance, fast-stream proton energy, as sensed by the sailcraft, ranges from 1.8 to 3.4 keV . A radial-in-EHOF $200-\mathrm{nm}$ sail, moving at $15 \mathrm{AU} / \mathrm{yr}$, is characterized by a backscattering yield equal to 0.039 and a backscattering energy fraction of 0.205 ; therefore, 99.2 percent of the solar-wind proton energy flux is deposited on the sail (in a max depth equal to 110 nm ). On the other side, a $130-\mathrm{nm} 22-\mathrm{AU} / \mathrm{yr}$ sail at perihelion absorbs 97.8 percent of the proton energy flux (in 115 nm ). Along a trajectory, sailcraft experiences differential proton energy flux, which changes as sail orientation and sailcraft position \& velocity evolve.
Energy from UV photons and solar-wind protons, absorbed by the reflective sail material through a very short thickness, alters reflectance and absorptance permanently. Mathematically, the independent variable is the energy fluence, of which equations IV-21 and IV-23 represent our present evaluation. Here, we adopt the following model of optical-parameters change

$$
\begin{align*}
& \delta a \equiv a_{\text {actual }}-a_{\text {ideal }}=A(\Psi) \\
& \left(r_{\text {ideal }}+d_{\text {ideal }}\right)(1-\varsigma)+a_{\text {ideal }}+\delta a=1  \tag{IV-24}\\
& \Rightarrow \\
& r_{\text {actual }}=(1-\varsigma) r_{\text {ideal }}, \quad d_{\text {actual }}=(1-\varsigma) d_{\text {ideal }}
\end{align*}
$$

This model entails that we should have some experimental data about absorptance change, namely, the function $A$ of fluence at time $t$, from which we could calculate the alteration in reflectance (since we know how to calculate the ideal or reference optics discussed in §IV.3). The second equation in IV-24 assumes that the relative changes of both specular and diffuse reflectance are equal to one another. Thus, immediately we get

$$
\begin{equation*}
\varsigma=A(\Psi) /\left(r_{\text {ideal }}+d_{\text {ideal }}\right) \tag{IV-25}
\end{equation*}
$$

Equations IV-24 have been written to having changes as positive quantities. Finally, though sail material emissivity does not change as a temperature function, however its actual range is shifted according to the absorptance change. Thus, all thermo-optical sail parameters entering the sailcraft motion equations are modified by the UV field and solar plasma that the sail gradually experiences.
On a conceptual basis, one can note that when surface roughness (an internal degradation) is introduced, part of the specular reflectance turns into diffuse reflectance. In contrast, when external degradation is considered, part of the total reflectance turns into absorptance.

### 4.1 Integro-Differential Equations of Sailcraft Motion

Despite the simplicity of the above particular model, the mathematical problem that stems from any optical degradation model consists of parameters depending on some quantity that is, at any time $t>0$, function of the previous history of the sailcraft trajectory. The optical parameters, modified through the energy fluence that depends on the sailcraft state evolution in $\left[t_{0}, t\right]$, determine the actual lightness vector at time $t$ that affects the sailcraft motion during the interval ( $t, t+d t$ ]. Equations IV-2, IV-15 (or IV-18), IV-24 and IV-25 are coupled. As soon as the last three equations are substituted into IV-2, equations of sailcraft motion appear as a system of integro-differential equations (IDE). In other words, whereas the ideal optics for sail entails a system of ODE, the introduction of optical degradation requires the numerical integration of a system of IDE for computing the sailcraft motion.
In the computer code shortly described in §IV.5, we had to modify some of the routines of the numerical integrators used for ODE in order to deal with the problem of optical degradation (even though model IV-24 is formally simple). In §IV.6, we shall show that some sailcraft trajectories are significantly affected by a progressive change of the thermo-optical sail parameters.

### 4.2 Experimental Data Fitting

What remains to do here is to discuss the determination of the function $A(\Psi)$. We began with the experimental data reported in (Werts et al., 2000), but we proceeded with using a different fitting procedure in order to be compliant with our present optical model. As of September 2001, the paper by Wertz was the only one, on this matter, supplied by NASA/MSFC to the author of this chapter. In addition, some of the public space literature on the UV-photon-induced degradation either regards organic materials or has contradictory results about thin metal films. In such literature, topics are not oriented specifically to solar sailing materials. Thus, in using data from Wertz paper, we had to assume that electron-dose damage may be similar to solar-wind proton's. No reliable data about UV-induced damage of Al-Cr films have been found by the author at the writing time. Nevertheless, the theoretical model described in this section and some consequences reported in §IV. 6 may be of considerable importance for solar sailing in general, even though we deal with only one of the pieces to the actual change of the thermo-optical sail parameters. With this in mind, we proceeded to the computation of the $A$-function into two steps. First, we fitted the experimental data of absorptance as function of the (electron) dose by considering that (1) if dose is very low, then the actual absorptance practically coincides with the ideal one, (2) if dose is very high, then the material is completely degraded, in practice $a_{\text {actual }} \rightarrow 1$. This has carried out the following fit


Figure IV.4-1

In the above plot, $\mathrm{D}_{\mathrm{e}}$ denotes the electron dose expressed in Mrads ( $1 \mathrm{Mrad}=10^{4} \mathrm{~Gy}$ ). Experimental data regarded beams incident orthogonally to the specimen surface. This fit produces absorptance residuals of zero mean ( $<1 \mathrm{E}-14$ ) and standard deviation equal to 0.00085 .
The second step consisted of transforming dose into energy fluence by utilizing the specimen materials, their geometrical configuration (Wertz, 2000) and noting that $a_{\text {ideal }}(\theta=0)=0.0720$ (independently of roughness) for Aluminum. That has resulted into the following absorptance change law

$$
\begin{equation*}
A(\Psi)=0.92027 \tanh \left(0.25215 \Psi_{\mathrm{SW}}\right)+0.00793 \tag{IV-26}
\end{equation*}
$$

In IV-26, the energy fluence is expressed in $\mathrm{MJ} / \mathrm{m}^{2}$. The last term in equation (IV-26) represents the difference between the experiment control value, taken at (small) non-zero fluence, and the ideal absorptance value given above. It has been retained as a small conservative bias; for a real mission, some bias will probably happen due to the non-negligible time between sail making (on ground) and sail deployment (in space).

## IV. 5 A Computer Code

The numerical cases of trajectory optimization presented extensively in §IV. 6 have been computed by using a computer code named Starship/Spaceship Mission Analysis Code (SMAC). The author has implemented SMAC on PC in the 1986-2001 timeframe.

### 5.1 General Description

SMAC has been designed and is maintained for computing spacecraft trajectories related to propulsion modes such as nuclear/solar electric propulsion, antimatter propulsion, space ramjet, laser/microwave sailing, solar sailing, plasma-driven sailing and any physically-admissible combination two-three modes. Obviously, some combinations of modes are hard to be realized in practice; they are useful for evaluation analysis and/or performance limit. User can perform trajectory computation in either classical or (full) relativistic dynamics. (SMAC was used by the author in his research on interstellar flight in the 1988-90 timeframe and during the AURORA Collaboration mentioned in §IV.3). SMAC is now in full Fortran-90/95 and currently runs under MSWindows 98 -SE. User graphic interface (GUI) has been designed in MS-Visual Basic 5. SMAC includes a 3D graphic module for quick output visualization.
Current SMAC version (A.45.93a) consists of about 24,600 lines. Employed compiler is a commercial highly optimized compiler for Pentium-III.
Solar-sail mode is one of the most detailed propulsion modes in SMAC. The whole of the solar sailing theory described in the previous sections comes from as special case of a more general solar-sailing model embedded in a set of Fortran modules and procedures; these ones are designed to grow with the user needs.
With regard to the Interstellar Probe mission concept, Normalized Solar Units (NSU) have been used by setting $\mathrm{GM}_{\mathrm{SUN}}=1$ and Astronomical Unit $(\mathrm{AU})=1$. Internal computations have been performed in full double precision according to IEEE 754.

### 5.2 Integrators

SMAC user can select different numerical integrators for different trajectory arcs, according to the propulsion types, star and planetary fields. The available methods for integrating ODE are:

```
Adams-Bashforth-Moulton (variable stepsize, variable order)
Bulirsch-Stoer (variable stepsize)
Runge-Kutta-Shank (modified)
    Fixed step
    Automatic variable stepsize
    User-defined variable stepsize
```

The above three methods are known to be based on quite different principles. They are useful also to compare high-precision integration of difficult mission profiles. Each integrator consists of Fortran procedures arranged into three nested levels: the driver routine, the stepper routine and the algorithm routine. The above integrators were originally implemented only for ODE in SMAC. Subsequently we have modified the drivers for also dealing with the integro-differential equations system stemming from the optical degradation problem.

### 5.3 Optimizers

The user can use SMAC in either propagation-mode or optimization-mode. Trajectories can be optimized in the Non-Linear Programming (NLP) sense; the analyst can minimize one objective function chosen out of five criteria. Optimization may be constrained on either control or state, or both. Additional linear/non-linear constraints, relevant to special propulsion modes (e.g. the solar sailing) are dealt with. Very shortly, a trajectory can be segmented into a number of arcs each of which is characterized by its own propulsion mode (one or more depending on the research purposes), star field, planetary perturbation(s), attitude control parameters, state/control constraints and so on. Through the GUI, the analyst can choose which controls are to be optimized arc-by-arc, including launch date and/or part of the initial spacecraft state relatively to either the departure star or the departure planet. Similarly, the final spacecraft state (at target) can be partially left open.
SMAC knows two robust optimization algorithms: the Marquardt method revised by Levenberg-MarquardtMorrison (or the LMM algorithm), the Levenberg-Marquardt method improved by Moré (Argonne Lab., 1980)
or the LME algorithm. The original implementation of LME was in FORTRAN-IV; it was ported to Fortran-90 by Vulpetti in the Nineties. Its current version in SMAC is either standard or interactive. Due to the different minimum-search policies of the two methods, the analyst may utilize both algorithms for solving problems exhibiting many local minima that differ slightly in value or by small amounts of the (optimized) control parameters, or both.

### 5.4 Constants and Standard Files

In addition to what explained in § IV.2.1, the following constants have been used in the present investigation by this computer code:

| Solar Gravitational Constant | $1.327124400180 \mathrm{E}+20 \mathrm{~m}^{3} / \mathrm{s}^{2}$ |
| :--- | :--- |
| Astronomical Unit | $1.495978706910 \mathrm{E}+11 \mathrm{~m}$ |
| Unit Mass | the spacecraft initial mass $[\mathrm{kg}]$ |
| Solar Constant | $1367 \mathrm{~W} / \mathrm{m}^{2}$ |
| 1 AU $/$ standard year | $4.740470 \mathrm{~km} / \mathrm{s}$ |
| Solar radius | $6.961 \mathrm{E}+05 \mathrm{~km}$ |

Basic physical constants have been taken from Particle Data Group (2000) available from CERN, LBNL and at http://pdg.lbl.gov. File DE403/LE403 from Jet Propulsion Laboratory (JPL) has been used for planetary ephemerides. With regard to the assumed value for the solar constant, it is an excess-rounded (by about 0.7 $\mathrm{W} / \mathrm{m}^{2}$ ) average of the daily-means of the total solar irradiance (that is time-variable) measured by satellite throughout the year 2000. For details, visit the site http://obsun.pmodwrc.ch. We have considered such value in this mission analysis of the Interstellar Probe, for a presumable launch in 2010/2011, namely, about one solar cycle from now. Some care about it should be used, in general. Sometimes, one might adopt a round value (1.4 $\mathrm{kW} / \mathrm{m}^{2}$ ) in rapid computation of solar sail trajectories This entails higher lightness numbers that, in turn, could induce some non-negligible shift of some key quantity (e.g. the perihelion distance). The result may be a nonlinear (generally optimistic) change of the trajectory performance index.

## IV. 6 The Case for Interstellar Probe

We shall study ISP mission opportunities involving sailcraft motion reversal. They might be added to the mission profiles already analyzed by JPL (Mewaldt et al., 2000). We deal with trajectories from sailcraft injection into the solar gravitational field to the target distance of 200 AU in the heliopause nose direction.

### 6.1 Investigation Line and Problem Statement

In its most general form, the lightness vector depends on variables and parameters of different physical origin that one may group as follows: (a) source-of-light parameters, (b) physical/geometrical sail parameters, (c) sailcraft state variables (mass, position, velocity), (d) environmental parameters, and the time elapsed since deployment. In particular, $\mathbf{L}$ is proportional to $\sigma_{c} / \sigma ; \sigma$ is a (technological) control parameter. We shall analyze aspects of the ISP mission concept through different values of the sailcraft sail loading that, in turn, is strongly related to the whole sailcraft technology, including the scientific payload. For each value of $\sigma$, typically we first discuss one (optimized) trajectory opportunity with ideal sail optics and, then, the corresponding opportunity with optical sail degradation. For the case $\sigma=2 \mathrm{~g} / \mathrm{m}^{2}$, more than one ideal-optics profiles will be presented. The meaning of the term "corresponding" used above is the following: once the idealoptics trajectory has been optimized (in the sense described below), one switches from ODE to IDE by considering optical sail degradation; then, optimization is performed by inserting the ideal-optics optimal controls as the guessed or starting control set. In the next sub-sections, we will discuss six profiles by $\sigma$ ranging from 2.2 to $1 \mathrm{~g} / \mathrm{m}^{2}$.
We computed admissible ranges of geocentric vector position and velocity (or the hyperbolic state) of a sailcraft in the fuzzy boundaries of the Earth-Moon-Sun system. We considered some of the current launchers capable to deliver a spacecraft of (at least) $200-350 \mathrm{~kg}$ with hyperbolic excess up to $1 \mathrm{~km} / \mathrm{s}$. Significantly higher values of the hyperbolic excess are excluded here, simply because both direct and reverse motion modes have to obey the
basic rule stated in §IV.2.3. (Obviously, launcher is a primary constraint; however, indicating any specific launcher is not a item of this report). The hyperbolic sailcraft state is added to the Earth state at the injection time, or the mission epoch, of the sailcraft into the solar field. We assume that, at such JD value, sail deployment \& attitude acquisition and any other preliminary operations have been completed. The whole sailcraft trajectory is here segmented in five parts: four sailing thrusting arcs (or T-arc) plus one coasting arc (or C-arc) from sail jettisoning to target. The first three T-arcs entail a three-axis stabilized attitude control, whereas sailcraft is spun in the fourth one. (Why sail is not jettisoned at few AU past the perihelion has been explained in Chapter-III of this report). In order to simplify the ISP $H$-maneuver, we have considered the following trajectory control parameters:
(1) Epoch $\left(\mathrm{t}_{0}\right)$
(2) Direction of the geocentric hyperbolic position (resolved in HIF) at $\mathrm{t}_{0}$
(3) Geocentric hyperbolic excess
(4) $1^{\text {st }} \mathrm{T}$-arc duration and sail direction constant in EHOF
$2^{\text {nd }} \mathrm{T}$-arc duration and sail direction constant in HIF
$3^{\text {rd }} \mathrm{T}$-arc duration and sail direction constant in EHOF
$4^{\text {th }} \mathrm{T}$-arc duration and sail direction constant in HIF
$1^{\text {st }} \mathrm{C}$-arc duration

$$
\begin{equation*}
1^{\text {st }} \mathrm{C} \text {-arc duration } \tag{7}
\end{equation*}
$$

Control sets 4-5-6 represent a simple realization of the 3D H-reversal motion detailed in (Vulpetti, 1999a). In addition, we have set the following constraints:

$$
\begin{align*}
\min (H) & >0 \\
\min (R) & \geq 0.2 \mathrm{AU}  \tag{IV-28}\\
\max \left(T_{S}\right) & <600 \mathrm{~K} \\
t_{f}-t_{0} & \leq 18 \mathrm{yr}
\end{align*}
$$

The following endpoint conditions have been applied

$$
\begin{align*}
& \left|\mathbf{R}\left(t_{0}\right)-\mathbf{R}_{\text {Earth }}\left(t_{0}\right)\right|=0.01776 A U \\
& R\left(t_{f}\right)=200 A U  \tag{IV-29}\\
& \Lambda\left(t_{f}\right)=254.5^{\circ} \quad \Theta\left(t_{f}\right)=7.5^{\circ}
\end{align*}
$$

We chose the flight time upper limit in IV-28 such that, combined with the optimized coasting speed, the whole ISP mission, with a potential prolongation from 200 AU to 400 AU (Liewer et al., 2000), may last less than a typical human job time (HJT) or 35 yr. However, the sailcraft distance baseline was fixed at 200 AU. The third row of IV-29 represents the ecliptic longitude-latitude coordinates of the sailcraft target position. The other endpoint values have been left free and optimized according to NLP. The index of performance, here, is the sailcraft speed at 200 AU. Thus, the current problem of astrodynamics can then be stated as follows:
Given either the previous ODE or IDE system, describing the motion of a sailcraft in the solar system, with vector state $\mathbf{S} \equiv\left[\begin{array}{lll}m & \mathbf{R} & \mathbf{V}\end{array}\right]^{T}$ driven from $\mathbf{S}_{0}$ to $\mathbf{S}_{f}$ (partially-fixed states) by the
control $\{U\}$ (defined in IV-27), find the special set $\left\{U^{\text {opt }}\right\}$ that maximizes the sailcraft speed at $t_{f}$ while satisfying the linear and non-linear constraints IV-28.

As far as the planetary perturbations are concerned, we considered both inner and outer planets; eventual planetary swing(s)-by of the sailcraft is(are) computed during the trajectory optimization process. When in the solar field, gravitational perturbation from the Earth-Moon system to the sailcraft is modeled as stemming from their barycenter.

### 6.2 Arrangement of the Results

In the following subsections, we discuss the numerical results of the problem stated in §IV.6.1. For each case and for each optimization, we have arranged the main results in six-Figure tables (on a one-per-page basis), which are grouped sequentially in §IV.6.11. Each table contains an header reporting the values of the quantities by which we made mission profiles distinct. They are: sailcraft sail loading (input), root mean square roughness (input), optical sail degradation switch (input), actual sailcraft perihelion (output). Each Figure in a set is labeled by both paragraph (of discussion) and progressive number. Figures 1-2 regard the projection of the sailcraft trajectory onto the ecliptic, or the XY plane, and the YZ plane. The orbits of the first four planets are also shown in the two plot windows. Figure 3 shows the evolution of the $H$-invariant. On the left side of the $H$ minimum, the sailcraft motion is direct, whereas on the right side it is reversed. The ensuing sailcraft cruise phase "saturates" the invariant. This behavior, which looks like a sort of "square root", is quite general for the 3D $H$-reversal mode aimed at getting away from the solar system. Time at which the vector $\mathbf{H}$ crosses the ecliptic plane is shown by a vertical segment in Fig.-3. Reversal time decreases with the sailcraft sail loading. Figure 4 is the plot of the timehistory of the lightness vector components (in EHOF). Motion reversal line is shown again. Controlling the first three T -arcs entails $\mathbf{L}(\mathrm{t})$ continuous, whereas the optimal spin-stabilized T -arc requires an attitude maneuver. After such a maneuver, supercritical sailcraft results in a quasi-radial lightness vector. In contrast, sub-critical sailcraft shows high non-radial numbers: the transversal number increases energy while the normal number steers to the target direction. During the spin phase, the radial number is close to unity or higher, so counterbalancing or overcoming the solar gravitational acceleration. Sailcraft speed and orbital energy are graphed in Figure 5. There, the perihelion time (vertical) line is added to show that maxima of speed and energy take place past the perihelion, with the following distinction: supercritical sailcraft exhibits a local maximum of speed and an asymptotic maximum of energy, whereas sub-critical sailcraft evidences asymptotic maxima of both. With regard to Figure 6, we plotted the history of sail temperature for the ideal sail optics (i.e. switching degradation to off); when degradation $=\mathrm{ON}$, we reported temperature, fluence and change of optical sail parameters altogether.
All Figures focus on suitable time windows that highlight the behaviour of functions. In discussing results, we limit ourselves to some points, whereas other considerations, which can be read out easily from Figures, are left to the reader.

Table IV.7-1 summarizes the main input and output values. We shall refer also to this table in discussing results.
Unless otherwise specified, the root mean square roughness has been fixed to 20 nm . This means that a roughness uncertainty from 3 standard deviations or 60 nm is reasonably compliant with the construction of a large surface with Aluminum-Chromium film nominally 200 nm thick.
Sailcraft sail loading will be given with two decimal digits. Units are grams per square meter. This means that, in the range considered in the present analysis, two mission profiles differing by less than $0.01 \mathrm{~g} / \mathrm{m}^{2}$ in this technological quantity can be considered identical, in practice.

### 6.3 The $2.20 \mathrm{~g} / \mathrm{m}^{2}$ case

This case has been considered to show the difficulty of a sailcraft of $2.2 \mathrm{~g} / \mathrm{m}^{2}$ to move as fast as the ISP mission concept would require.
Figures IV.6.3-[1-6] show the optimized profile for ideal optics. Radial, transversal and normal lightness numbers are such that motion reversal can take place. Orbital angular momentum decreases in magnitude and bends progressively until it lies on the ecliptic plane, 1.492 years after injection. At such a time, the transversal number vanishes and the normal number achieves its local positive maximum, according to the theory. Since this instant on, the transversal component of the lightness vector becomes positive whereas angular momentum bending continues as the normal number is still positive. As a result, sailcraft motion reverses while energy increases. Sailcraft moves toward the Sun with increasing speed not only because potential energy decreases but also since total energy augments significantly. It achieves the escape point $(E=0)$ and rapidly rises before the perihelion. Acceleration keeps on after the perihelion, but now the normal number goes to zero from the right side, while the sailcraft distance from the Sun rapidly increases because of the very high speed. All this means that angular momentum stops bending and the $H$-function evolves asymptotically. The subsequent attitude
maneuver for getting a spinning sailcraft completes both speed keeping and steering of sailcraft toward the target direction.
In the current framework, the above description applies qualitatively to any $H$-reversal evolution. However, as we decrease the sailcraft sail loading, we will find a corresponding progressive shifting of values (not of behavior) that is important in the ISP context.
In the present case, the direct motion arc - always characterized by the $H$-invariant decrease - is slow because the transversal number, responsible for the energy change, is not negative enough. Even the radial number is not sufficiently greater than $1 / 2$ for allowing a high perihelion. Consequently, if one wants a cruise speed satisfying the mission flight-time constraint, then perihelion has to be low. Getting a cruise speed more than $14 \mathrm{AU} / \mathrm{yr}$ entails a non-negligible perihelion violation, namely, $\mathrm{R}_{\mathrm{P}}=0.175$ AU here. Such a low perihelion may not be a problem, in general, for an advanced sailcraft. The true problem arises in the presence of optical degradation.
To figure out better, a sailcraft trajectory - satisfying active constraints - may be generally regarded as a sort of delicate compromise between conflicting key quantities such as hyperbolic state (with respect to the departure planet), time interval to perihelion, perihelion distance, sail temperature effects, range of lightness numbers, and so on. They "interact" to each other, of course. As pointed out, in the current case the lightness numbers are not so high to decelerate sailcraft fast enough. Thus, solar-wind energy fluence increases and induces a strong absorptance change. This one, in turn, increases sail temperature significantly. On the other side, if one decreased the hyperbolic excess at epoch, then a time-to-perihelion reduction could take place; nevertheless, since the radial lightness number does not depend on hyperbolic excess, one would have a further lowering of perihelion and an additional increase of the fluence on the sail. Thus, in getting a trajectory satisfying perihelion and temperature constraints, both baseline and extended-mission flight times exceed their limits, as reported in Table IV.7-1, as cruise speed falls down to $11 \mathrm{AU} / \mathrm{yr}$. The present value of S may be considered in a transition zone (relatively to the ISP mission concept) where some constraint, unavoidably, cannot be satisfied.

### 6.4 The $2.10 \mathrm{~g} / \mathrm{m}^{2}$ case

As pointed out above, $\mathbf{L}$ depends on $\mathbf{S}$ non-linearly. With respect to the previous case, a decrease of 4.5 percent in S induces a change of 9.6 percent in the range of the optimal transversal lightness number of the directmotion arc (ideal optics, Figures IV.6.4-[1-6]). This quantity is the major responsible for the change of key values with respect to those ones related to $2.20-\mathrm{g} / \mathrm{m}^{2}$. As a point of fact, even though the radial number varies by about 1 percent, $H$-reversal time and perihelion time are back shifted by 15.7 and 13.1 percent, respectively. Every constraint is satisfied; in particular, perihelion takes place at 0.204 AU . Note that the duration of the $2^{\text {nd }} \mathrm{T}$ arc decreases from about 60 to 33.5 days. In this arc, the angular momentum bends and reverses by passing through a minimum in magnitude. The interval of such a T-arc is a non-linear function of the sailcraft sail loading. Its allocation after the $1^{\text {st }} \mathrm{T}$-arc, where the sailcraft's deceleration occurs, is a key factor for achieving the condition of motion reversal.
Optical degradation brings on perihelion rising of 0.044 AU with a delay of 84 days (or about 14.9 percent) with respect to the just-mentioned ideal-optics case. However, relatively to the $2.20 \mathrm{~g} / \mathrm{m}^{2}$ case, the "gain" in terms of mean distance and time in the pre-perihelion motion is such that fluence at perihelion decreases down to 0.57 $\mathrm{MJ} / \mathrm{m}^{2}$ or -3.4 percent. This is enough to not violate the temperature limit and get a good margin. Fluence saturation is achieved two years after injection, namely, one year (or 30 percent) in advance with respect to the 2.20 -case. Trajectory profiles are shown in Figures IV.6.4-[7-12]. One has only a slight violation ( 0.1 yr ) of the baseline flight time. Cruise speed amounts to $12.23 \mathrm{AU} / \mathrm{yr}$.
In the current framework, the $2.10 \mathrm{~g} / \mathrm{m}^{2}$ case could be considered the lower bound of the above-mentioned transition from mission infeasibility to mission feasibility.

### 6.5 The $2.00 \mathrm{~g} / \mathrm{m}^{2}$ case

The present S value is very close to that considered for ISP in (Mewaldt and Liewer, 2000) and (Liewer et al., 2000). We first present a number of trajectory profiles with different values of the root mean square roughness. Key values are collected in background-colored rows of Table IV.7-1.

In principle, the best case one may envisage is a sail with neither roughness nor degradation. Plots related to this special case of optimized trajectory are shown in Figures IV.6.5-[1-6]. Pre-perihelion trajectory is almost tangential to the Mars orbit. Motion reversal begins after 321 days (since injection) with $H_{\min }=0.0226 \mathrm{AU}^{2} / \mathrm{yr}$. The sailcraft proceeds to perihelion, in about 76 days, with a speed of $16.78 \mathrm{AU} / \mathrm{yr}$; maximum speed is as high as $17.79 \mathrm{AU} / \mathrm{yr}$. However, since the max value ( 0.736 ) of the lightness number is less than unity even in this ideal case, speed has to decrease while sailcraft recedes from the Sun. Nevertheless, a cruise speed of 15.22 $\mathrm{AU} / \mathrm{yr}$ is achievable by satisfying constraints widely. This results in baseline flight time of about 14.2 yr with additional 13 yr to accomplish the prolonged mission. In one HJT, sailcraft could reach 516 AU .
Figures IV.6.5-[7-12] show that this performance is decreased only slightly if the sail were made with a root mean square roughness equal to 10 nm . This is a direct consequence of the diffuse-reflectance law given by equation IV-20. The most visible differences are: earlier launch date (on October 7) by almost three days, the increase of the hyperbolic excess from $10 \mathrm{~m} / \mathrm{s}$ to $70 \mathrm{~m} / \mathrm{s}$. Both compensate for the (low) reduction of transversal lightness number; thus, without remarkable changes in the other decision parameters, perihelion remains unchanged and cruise speed can be kept over $15 \mathrm{AU} / \mathrm{yr}$. In one HJT, sailcraft could reach 509 AU .
There is still a good margin in accepting a sail made with higher roughness $d$ and, at the same time, finding a perihelion very close to the value given in (Liewer et al, 2000). The set of plots for $\mathrm{d}=20 \mathrm{~nm}$ and ideal optics are displayed in Figures IV.6.5-[13-18]. The pre-perihelion arc elongates beyond the Mars orbit, H-reversal delays by 61 days $\left(H_{\min }=0.0115 \mathrm{AU}^{2} / \mathrm{yr}\right)$ and perihelion occurs at 0.24 AU . As a result, cruise speed decreases to 13.17 $\mathrm{AU} / \mathrm{yr}$. However, both baseline and extended mission flight times satisfy the related constraints (even though the extended mission lasts four years more). In one HJT, sailcraft could reach 443 AU.
This $\mathrm{d}=20$ ideal-optics solution is important since it is changed exiguously, injection date included, by the optical degradation (Figures IV.6.5-[19-24]). As a point of fact, the lightness numbers are still sufficiently high to ultimately keep fluence below $0.55 \mathrm{MJ} / \mathrm{m}^{2}$ around the perihelion. Thus, temperature constraint is not violated $\left(T_{\max }=587 \mathrm{~K}\right)$. Fluence achieves saturation $\left(0.7 \mathrm{MJ} / \mathrm{m}^{2}\right)$ in 1.7 yr . From Table IV.7-1, one can see that both time to and speed at 200 AU are such that 441 AU could be achieved in one HJT. In addition, the current cruise speed of $13.13 \mathrm{AU} / \mathrm{yr}$ compares well to $V_{\infty}^{p}$ or $14.41 \mathrm{AU} / \mathrm{yr}$, given by equation IV-6 (which does not include any degradation).
From what so far described, one should note that decreasing the sailcraft sail loading from 2.2 to $2.0 \mathrm{~g} / \mathrm{m}^{2}$ means moving from risk to feasibility, at least from the nominal-mission viewpoint.

### 6.6 The $1.80 \mathrm{~g} / \mathrm{m}^{2}$ case

In full degradation conditions, the value of $2.00 \mathrm{~g} / \mathrm{m}^{2}$ would cause a temperature violation if one attempted to use a perihelion even reduced by 0.011 AU . For instance, some sail control errors may force to flyby the Sun at a lower distance during the real flight. On the other hand, some meaningful perihelion decrease is necessary to increase the cruise speed. That may be accomplished by further reducing the sailcraft sail loading. In the idealoptics mode, $1.80 \mathrm{~g} / \mathrm{m}^{2}$ would allow the sailcraft to flyby the Sun at $R_{\mathrm{P}}=0.20 \mathrm{AU}$ and to complete the extended mission in 26.2 years. One would get 538 AU in 1 JHT .
However, in the optical-degradation mode, perihelion cannot be lower than 0.22 AU . At this value, fluence takes on $0.5 \mathrm{MJ} / \mathrm{m}^{2}$ that induces 597 K of max sail temperature. Fluence saturates at $0.64 \mathrm{MJ} / \mathrm{m}^{2}$, practically achieved in 1.1 yr . With this perihelion, cruise speed comes to $14.8 \mathrm{AU} / \mathrm{yr}$; whence, baseline flight time amounts to about 14.4 yr and the extended mission lasts 27.9 yr. After a time equal to 1 HJT , sailcraft would achieve 505 AU . Plots of the current case are displayed in Figures IV.6.6-[1-12].
The main advantage stemming from making the ISP sailcraft with $1.8 \mathrm{~g} / \mathrm{m}^{2}$ instead of $2.0 \mathrm{~g} / \mathrm{m}^{2}$ would consist of flight error counterbalance through a set of admissible backup trajectories with respect to a nominal trajectory having $0.22 \mathrm{AU}<R_{\mathrm{P}}<0.25 \mathrm{AU}$, especially if the actual energy fluence were to result meaningfully different from the predicted one.

### 6.7 The Critical Case

As we know, the attribute critical refers normally to the equality between the sailcraft sail loading and that ideal value, which would allow a sailcraft to balance the solar gravity exactly. We mentioned in §IV. 3 that such value pertains to a perfectly reflecting sail (at-rest in HIF) oriented radially and receiving light from the point-like Sun. However, any real sailcraft at criticality, i.e. with $\sigma=\sigma_{c}$, would exhibit a maximum value of the lightness number lower than unity at any time, as its thrust efficiency is certainly less than unity throughout the flight. Besides, the max value of this efficiency in this case is close to 0.87 . Consequently, such a sailcraft would not be dynamically critical, inasmuch as the lightness number would be meaningfully lower than one throughout the flight. We shall go forward to analyzing some sub-critical cases.

### 6.8 The $1.28 \mathrm{~g} / \mathrm{m}^{2}$ case

In terms of S, this sub-critical 1.28 is as distant from $\mathrm{S}_{\mathrm{C}}$ as 1.80 is. For an ideal-optics sail, the pre-perihelion arc is characterized by a mean value of the transversal number equal to -0.375 . This is sufficient negative to lower aphelion, increase energy loss and achieve perihelion $(0.20 \mathrm{AU})$ in 212 days. After the attitude maneuver at the beginning of the fourth T-arc (at 0.27 AU ), the post-perihelion trajectory arc exhibits comparable values of all components of the lightness vector. This allows both energy and speed to evolve with profiles practically flat throughout the fourth T-arc (that ends at 120 AU ). Strictly speaking, the local maximum of sailcraft speed still exists, but it is so broad, on the right, that it is rendered indistinct from the cruise level or 20.8 AU/yr. Baseline mission could be accomplished in 10.2 yr. Sailcraft could reach 716 AU in 1 HJT.
When optical sail degradation is considered, the pre-perihelion arc is still so fast that, very close to the perihelion, solar-wind energy fluence is as low as $0.37 \mathrm{MJ} / \mathrm{m}^{2}$ at which sail temperature rises to 578 K , its max value. Sail achieves fluence saturation $\left(0.48 \mathrm{MJ} / \mathrm{m}^{2}\right)$ in 0.7 yr since injection. The optimal profiles for opticaldegradation are very similar to those ones without it. One value for all, ISP would reach a distance, again, equal to 716 AU in 1 HJT .
This case is shown in Figures IV.6.8-[1-12].

## $6.9 \quad$ The $1.00 \mathrm{~g} / \mathrm{m}^{2}$ case

In contrast to the above cases, some lightness number can now be greater than unity in some T -arcs; in particular, one gets $\lambda \cong 1.24, \lambda_{r} \cong 1.17, \lambda_{t} \cong 0.34$ (ideal optics) in the spinning-sail T-arc. The main result consists of obtaining the sailcraft speed increasing as sailcraft moves far away from the Sun. As a point of fact, once the sailcraft overcomes the perihelion, some maneuver can be accomplished in order to reorient the sail with a radial number constantly greater than unity. Thus, the local speed maximum of the previous cases has "evolved" into an asymptotic absolute maximum. The $H$-reversal arc duration is still quite manageable (2 days). The optimal profiles are shown in Figures IV.6.9-[1-6].
By including optical degradation, the above set of lightness values changes into $\lambda \cong 1.14, \lambda_{r} \cong 1.08, \lambda_{t} \cong 0.29$, which allows sailcraft to accelerate again asymptotically. The related profiles are shown in Figures IV.6.9-[7-12]. Sail temperature takes on a max value of 547 K at fluence equal to 0.31 $\mathrm{MJ} / \mathrm{m}^{2}$. The dynamical output one gets at 200 AU consists of sailcraft speed equal to $23.5 \mathrm{AU} / \mathrm{yr}$. Baseline mission lasts 9.03 years, whereas the extended mission to 400 AU may be accomplished in less than 18 years. 809 AU could be reached in one HJT.
From Table IV.7-1, one can note that the current max value of sail temperature is the lowest one out of all cases hitherto analyzed. (The temperature margin may be used to design a new profile with perihelion less than 0.2 AU, but still keeping fluence sufficiently low not to violate 600 K . Such an analysis may be among the topics of a future study on faster ISP). Finally, one should note that, in this case of sub-critical sailcraft sail loading, $V_{\infty}^{p}$ amounts to $21.34 \mathrm{AU} / \mathrm{yr}$, namely, lower than the current cruise speed. It is to be ascribed mainly to the large transversal lightness number that can change energy (equation IV-5c) to overcome the pure-radial solution significantly.

### 6.10 Further Remarks

1. Keeping the sail attitude constant, or so, in the sailcraft orbital frame entails that the sail axis has to be rotated sufficiently fast in the inertial frame, especially when sailcraft moves around the perihelion. For instance, the attitude control system has to output about 9.7 deg/day and 15.1 deg/day for the $2 \mathrm{~g} / \mathrm{m}^{2}$ and $1 \mathrm{~g} / \mathrm{m}^{2}$ case, respectively. In the present model of sailcraft, although detailed system description and modeling is beyond the scope of this report, we assumed a small-rocket attitude control; each pair of micro-engines (endowed with small solar panel) is placed on the sail rim. In the fastest trajectories here analyzed, maximum fuel consumption is less than 1 percent of the initial sailcraft mass. In general, a "mixed" attitude control system may be considered: non-rocket devices (Wright, 1993) and microthrusters, depending on the distance from the Sun and the trajectory control requirements.
2. The optimal trajectory profiles presented in this report are characterized, among many things, by a double-crossing of the ecliptic plane, with the perihelion between the two. Perihelion latitude ranges from $-14.8^{\circ}$ to $-47.8^{\circ}$. Therefore, there is no geometric problem in the sailcraft-Earth communication around the perihelion. What shall be analyzed in detail is the location of the onboard antenna with respect to the sail.
3. In addition to the mission unfeasibility-feasibility transition, there exist another special value of the sailcraft sail loading. For the ISP-mission Al-Cr sail spacecraft with H -reversal motion, this value is very close to $1.3 \mathrm{~g} / \mathrm{m}^{2}$. Below it, the pre-perihelion trajectory arc can be so fast that (despite the angle between sailcraft position and velocity is significantly greater than $90^{\circ}$ for over 50 percent of time), the optimal performance indexes of the ideal-optics and the optical-degradation flights can be considered equal to one another ( $<1$ percent). Above this limit, the influence of the energy fluence on mission feasibility cannot be neglected. Reasonably, such a feature should hold even for a direct-motion fly-by of the Sun. At the time of this writing, though, it is not known.
4. A sailcraft with $1.2 \mathrm{~g} / \mathrm{m}^{2}$, or less, would be able to fast explore the solar gravitational lens in deeper focal zones. For instance, if sailcraft were able to fly-by the Sun at perihelion equal to 0.15 AU (Vulpetti, 2000), it could navigate the interval from 763 AU to 821 AU in 2.3 yr and reach 821 AU after 32.2 yr since injection. That would be appropriate for observing distant photon sources in the range from 160.4 GHz to 122.3 GHz (Maccone, 2000). At 122.3 GHz , the photon path bending due to the solar gravity is counterbalanced by the contrary deflection caused by the solar corona plasma. Photon frequencies different from such no-lensing value behave differently in total deflection. In the context of a generalized ISP mission concept, such a potential flight may be revisited by adding optical degradation, telecommunication system and launcher constraint.

### 6.11 Figures

Case id: $\sigma=2.20 \mathrm{~g} / \mathrm{m}^{2}$, r.m.s. $\delta=20 \mathrm{~nm}$, Degradation=off, perihelion=0.175 AU

Figure IV.6.3-1


Figure IV.6.3-3


Figure IV.6.3-5


Figure IV.6.3-2


Figure IV.6.3-4


Figure IV.6.3-6


Case id: $\sigma=2.20 \mathrm{~g} / \mathrm{m}^{2}$, r.m.s. $\delta=20 \mathrm{~nm}$, Degradation $=\mathrm{ON}$, perihelion=0.261 AU

Figure IV.6.3-7


Figure IV.6.3-9


Figure IV.6.3-11


Figure IV.6.3-8


Figure IV.6.3-10


Figure IV.6.3-12


Case id: $\sigma=2.10 \mathrm{~g} / \mathrm{m}^{2}$, r.m.s. $\delta=20 \mathrm{~nm}$, Degradation=off, perihelion=0.204 AU

Figure IV.6.4-1


Figure IV.6.4-3


Figure IV.6.4-5


Figure IV.6.4-2


Figure IV.6.4-4


Figure IV.6.4-6


Case id: $\sigma=2.10 \mathrm{~g} / \mathrm{m}^{2}$, r.m.s. $\delta=20 \mathrm{~nm}$, Degradation=ON, perihelion=0.248 AU

Figure IV.6.4-7


Figure IV.6.4-9


Figure IV.6.4-1 1


Figure IV.6.4-8


Figure IV.6.4-10


Figure IV.6.4-12


Case id: $\sigma=2.00 \mathrm{~g} / \mathrm{m}^{2}$, r.m.s. $\delta=0 \mathrm{~nm}$, Degradation=off, perihelion=0.20 AU Figure IV.6.5-1


Figure IV.6.5-3


Figure IV.6.5-5


Figure IV.6.5-4


Figure IV.6.5-6


Case id: $\sigma=2.00 \mathrm{~g} / \mathrm{m}^{2}$, r.m.s. $\delta=10 \mathrm{~nm}$, Degradation=off, perihelion=0.20 AU

Figure IV.6.5-7


Figure IV.6.5-9


Figure IV.6.5-11


Figure IV.6.5-8


Figure IV.6.5-10


Figure IV.6.5-12


Case id: $\sigma=2.00 \mathrm{~g} / \mathrm{m}^{2}$, r.m.s. $\delta=20 \mathrm{~nm}$, Degradation=off, perihelion=0.24 AU

Figure IV.6.5-13


Figure IV.6.5-15


Figure IV.6.5-17


Figure IV.6.5-14


Figure IV.6.5-16


Figure IV.6.5-18


Case id: $\sigma=2.00 \mathrm{~g} / \mathrm{m}^{2}$, r.m.s. $\delta=20 \mathrm{~nm}$, Degradation $=\mathrm{ON}$, perihelion=0.24 AU

Figure IV.6.5-19


Figure IV.6.5-21


Figure IV.6.5-23


Figure IV.6.5-20


Figure IV.6.5-22


Figure IV.6.5-24


Case id: $\sigma=1.80 \mathrm{~g} / \mathrm{m}^{2}$, r.m.s. $\delta=20 \mathrm{~nm}$, Degradation=off, perihelion=0.20 AU

Figure IV.6.6-1


Figure IV.6.6-3


Figure IV.6.6-5


Figure IV.6.6-2


Figure IV.6.6-4


Figure IV.6.6-6


Case id: $\sigma=1.80 \mathrm{~g} / \mathrm{m}^{2}$, r.m.s. $\delta=20 \mathrm{~nm}$, Degradation $=\mathrm{ON}$, perihelion=0.22 AU

Figure IV.6.6-7


Figure IV.6.6-9


Figure IV.6.6-1 1


Figure IV.6.6-8


Figure IV.6.6-10


Figure IV.6.6-12


Case id: $\sigma=1.28 \mathrm{~g} / \mathrm{m}^{2}$, r.m.s. $\delta=20 \mathrm{~nm}$, Degradation=off, perihelion=0.20 AU

Figure IV.6.8-1


Figure IV.6.8-3


Figure IV.6.8-5


Figure IV.6.8-2


Figure IV.6.8-4


Figure IV.6.8-6


Case id: $\sigma=1.28 \mathrm{~g} / \mathrm{m}^{2}$, r.m.s. $\delta=20 \mathrm{~nm}$, Degradation=ON, perihelion=0.20 AU

Figure IV.6.8-7


Figure IV.6.8-9


Figure IV.6.8-1 1


Figure IV.6.8-8


Figure IV.6.8-10


Figure IV.6.8-12


Case id: $\sigma=1.00 \mathrm{~g} / \mathrm{m}^{2}$, r.m.s. $\delta=20 \mathrm{~nm}$, Degradation=off, perihelion=0.20 AU

Figure IV.6.9-1


Figure IV.6.9-3


Figure IV.6.9-5


Figure IV.6.9-2


Figure IV.6.9-4


Figure IV.6.9-6


Case id: $\sigma=1.00 \mathrm{~g} / \mathrm{m}^{2}$, r.m.s. $\delta=20 \mathrm{~nm}$, Degradation=ON, perihelion=0.20 AU

Figure IV.6.9-7


Figure IV.6.9-9

[ yr ]

Figure IV.6.9-1 1


Figure IV.6.9-8


Figure IV.6.9-10


Figure IV.6.9-12


## IV. 7 Summary Table

Table IV.7-1. ISP H-reversal trajectory opportunity: main features from the optimal profiles discussed in §IV.6. Constraint violation is marked bold. Italic figures in the rightmost column represent the flight time of the extended mission to 400 AU.

| $\sigma\left[\mathrm{g} / \mathrm{m}^{2}\right]$ | $\delta$ [ nm ] | Optical Degradation | Perihelion distance [AU] | $\begin{gathered} \text { Aphelion in } \\ \text { pre-perihelion } \\ \text { arc [AU] } \\ \hline \end{gathered}$ | Time to Aphelion [year] | Time to H-reversal [year] | Time to Perihelion [year] | Max Sail Temperature $[K]$ | Speed at 200 AU [AU/yr] | $\begin{gathered} \text { Time to } \\ 200 \mid 400 \mathrm{AU} \\ \text { [year] } \end{gathered}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 2.20 | 20 | Off | 0.175 | 2.130 | 0.931 | 1.492 | 1.776 | 530 | 14.34 | 15.698\|29.65 |
| 2.20 | 20 | ON | 0.261 | 2.636 | 1.283 | 1.934 | 2.470 | 574 | 11.02 | $\mathbf{2 0 . 5 6 5 \| 3 8 . 7 1 ~}$ |
| 2.10 | 20 | Off | 0.204 | 1.938 | 0.806 | 1.258 | 1.543 | 490 | 13.20 | 16.667 \| 31.82 |
| 2.10 | 20 | ON | 0.248 | 2.118 | 0.922 | 1.393 | 1.773 | 584 | 12.23 | $\mathbf{1 8 . 0 9 6}$ \| 34.45 |
| 2.00 | 00 | Off | 0.20 | 1.570 | 0.556 | 0.879 | 1.086 | 492 | 15.22 | 14.211\|27.35 |
| 2.00 | 10 | Off | 0.20 | 1.613 | 0.583 | 0.922 | 1.137 | 490 | 15.04 | 14.424 \| 27.72 |
| 2.00 | 20 | Off | 0.24 | 1.809 | 0.716 | 1.089 | 1.383 | 450 | 13.17 | 16.543 \| 31.73 |
| 2.00 | 20 | ON | 0.24 | 1.827 | 0.726 | 1.105 | 1.405 | 587 | 13.13 | 16.611 \| 31.84 |
| 1.80 | 20 | Off | 0.20 | 1.426 | 0.457 | 0.736 | 0.913 | 487 | 15.79 | 13.565 \| 26.23 |
| 1.80 | 20 | ON | 0.22 | 1.470 | 0.485 | 0.769 | 0.967 | 597 | 14.84 | 14.429 \| 27.91 |
| 1.28 | 20 | Off | 0.20 | 1.158 | 0.257 | 0.462 | 0.581 | 471 | 20.79 | 10.201 \| 19.82 |
| 1.28 | 20 | ON | 0.20 | 1.159 | 0.257 | 0.464 | 0.582 | 578 | 20.79 | 10.202\|19.82 |
| 1.00 | 20 | Off | 0.20 | 1.099 | 0.201 | 0.390 | 0.496 | 458 | 23.57 | $8.986 \mid 17.47$ |
| 1.00 | 20 | ON | 0.20 | 1.099 | 0.201 | 0.391 | 0.496 | 547 | 23.46 | $9.026 \mid 17.55$ |

## IV. 8 Feasibility of ISP from Trajectory Design Viewpoint

These following considerations complement those made in §IV.6.10. As it is well known, Interstellar Probe is not only a sophisticated scientific mission concept; among the main things, it should prove that it is possible to travel fast to distant targets with low cost and high reliability. These features generally depend on sailcraft operations, no other propulsion (apart from lifting off, of course), strong increase of the launch window, higher number of missions per time unit (e.g. on a quinquennium basis) and so forth. Thus, the existence of an additional launch opportunity for the ISP mission concept should be of high concern. Previous sections have, no doubt, shown that there exists such an opportunity for ISP sailcraft, in October of every year. This could be accomplished by utilizing one of the several peculiarities of space sailing: the fly-by of the Sun via motion reversal. A spectrum of fourteen optimized mission profiles have been computed by a code that takes into account a high number of real effects. Distinct trajectories correspond to different key parameters such as the sailcraft sail loading, sail roughness and optical sail degradation due to solar wind. (Ultraviolet-photon degradation was not considered by lack of experimental data appropriate to solar sailing). Solar wind fluence has been recognized relevant to a sailcraft approaching the Sun closely. In addition, a major item has consisted of dealing with integro-differential equations for modeling sailcraft motion appropriately. Optical degradation, with constraints on temperature, perihelion and flight time, has resulted in a key item for designing some fast sailcraft trajectory to many hundreds of AU. By considering both baseline and extended mission concepts, ISP is certainly feasible from motion-reversal trajectory viewpoint if the sailcraft sail loading is lower than $2.1 \mathrm{~g} / \mathrm{m}^{2}$. The current literature value of the ISP-sailcraft sail loading is very close to $2 \mathrm{~g} / \mathrm{m}^{2}$. This is a value sufficiently lower than the above threshold to allow the following time line (since injection): (1) launching in October, (2) flying-by the Sun at 0.24 AU after 1.40 years, (3) achieving 200 AU after 16.6, (4) extending the mission to 400 AU by 15.2 years more. (A slightly lower value of the sailcraft sail loading in the range $[1.9,1.95] \mathrm{g} / \mathrm{m}^{2}$ is suggested to deal with small attitude control errors). These ones and the other numerical results, discussed in this document, should be considered realistic enough due to the many key elements and detailed features included in the present dynamical model of sailcraft motion.

## IV. 9 Conclusions and Future Research

The analysis performed so far, and presented in this report, is sufficiently general in some aspects to allow us to suggest some major lines for future investigation. They may be expressed as follows
A. ISP feasibility: additional aspects are to be investigated and improved, of course; however, it is hard that the ISP concept may result unfeasible from mission viewpoint. That is enforced by two launch opportunities per year. By considering how complex and various are solar-sailing trajectories, it would be interesting to investigate whether there is some other opportunity.
B. Optical sail degradation: there is the need for additional experimental data about solar wind and new data on UV. Once again, we stress that the evolution of the optical sail parameters is one of the major aspects of solar sailing. Other potential missions close to the Sun may benefit from such data; for instance, a solar-sail mission to solar poles, with final orbit achieving $90^{\circ}$ in heliographic latitude, should be investigated with respect to this critical point as well. Furthermore, a future interplanetary sail shuttle might be limited in lifetime by optical degradation before any other system fails.
C. A sensitivity analysis on the baseline ISP profile is strongly recommended. The optimization process performed in this work was rather complicated; although not reported here since beyond the present aims, however it revealed that many decision parameters affect the solar sailcraft flyby very differently.
D. Aluminum-Chromium is appropriate for the ISP of first generation ( 400 AU ). Assessing feasibility for second-generation ISP ( $800-1000 \mathrm{AU}$ ) with perihelion at 0.15 AU would deserve a dedicated study. New sail materials, e.g. according to the line open by Matloff (Matloff, 1997-2000), should be investigated for third-generation ISP that, for instance, may achieve 10 light-days in one human job time, or less.

## IV. 10 References

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[^0]:    ${ }^{\text {Iv-1 }}$ Chief Scientist, Full Member of the International Academy of Astronautics

[^1]:    ${ }^{\text {IV-2 }}$ We use optical terms ending in 'ance' since they apply to real specimens regardless of their geometric thickness and physical surface state. Terms ending in 'ivity' are normally used to highlight optically smooth specimens.

[^2]:    ${ }^{\text {IV-3 }}$ DLC is a metastable disordered solid that shows a mix of diamond and graphite structures.

