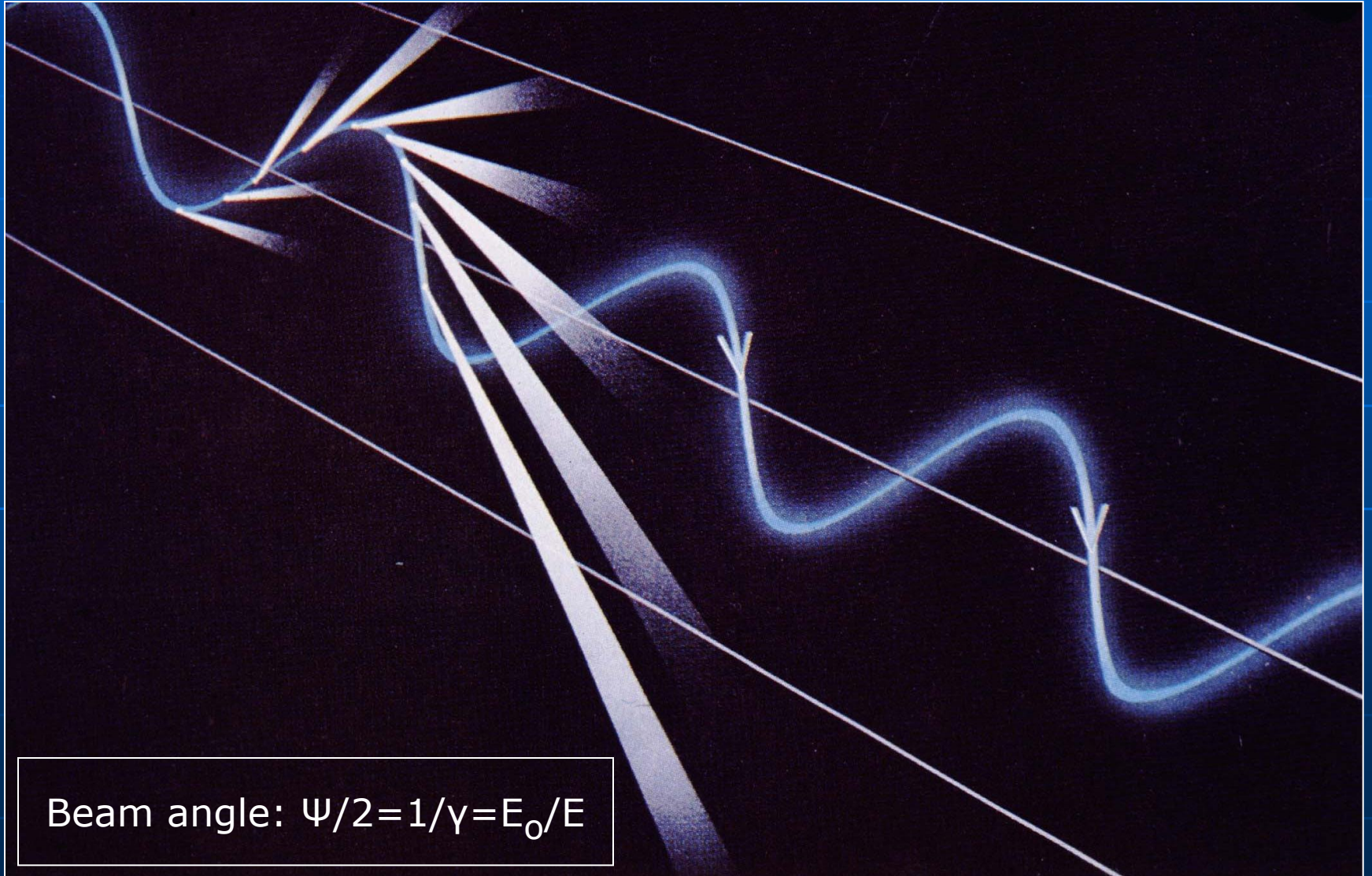


Radio Continuum:

Cosmic Rays
&
Magnetic Fields

Rainer Beck
MPIfR Bonn

Synchrotron emission



Radio continuum tools to study GeV Cosmic ray electrons (CRE)

- **Synchrotron spectrum:**
Energy density, energy spectrum,
energy losses of CRE
- **Distribution of synchrotron spectral index:**
Propagation type and velocity of CRE
- **Scale height/length of galaxy and cluster halos:**
Bulk outflow velocity, diffusion coefficient

Synchrotron emission

- **Power-law** energy spectrum of CRE
(with spectral index ε):

$$N(E) dE = N_0 E^{-\varepsilon} dE$$

- Intensity of synchrotron spectrum:

$$I_\nu \sim \int N_0 B_\perp^{(\varepsilon+1)/2} \nu^{-(\varepsilon-1)/2} dL$$

- Synchrotron spectral index:

$$\alpha = (\varepsilon-1)/2$$

Strong shocks: $\varepsilon=2$, $\alpha=0.5$

Energy loss mechanisms of CRE

Ionisation

$$-\left(\frac{dE}{dt}\right)_{\text{ion}} \propto \ln E \sim \text{constant}$$

Bremsstrahlung

$$-\left(\frac{dE}{dt}\right)_{\text{brem}} \propto E$$

Adiabatic cooling

$$-\left(\frac{dE}{dt}\right)_{\text{adiab}} \propto E$$

Synchrotron

$$-\left(\frac{dE}{dt}\right)_{\text{syn}} \propto E^2$$

Inverse Compton

$$-\left(\frac{dE}{dt}\right)_{\text{invC}} \propto E^2$$

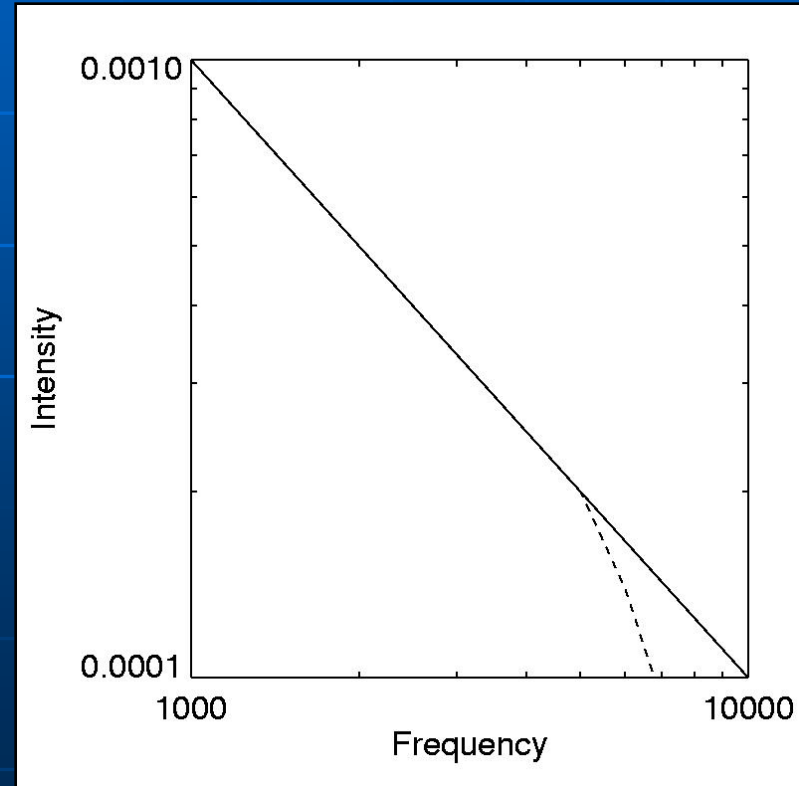
Escape into halo

$$\text{diffusion coefficient } D \propto E^\delta.$$

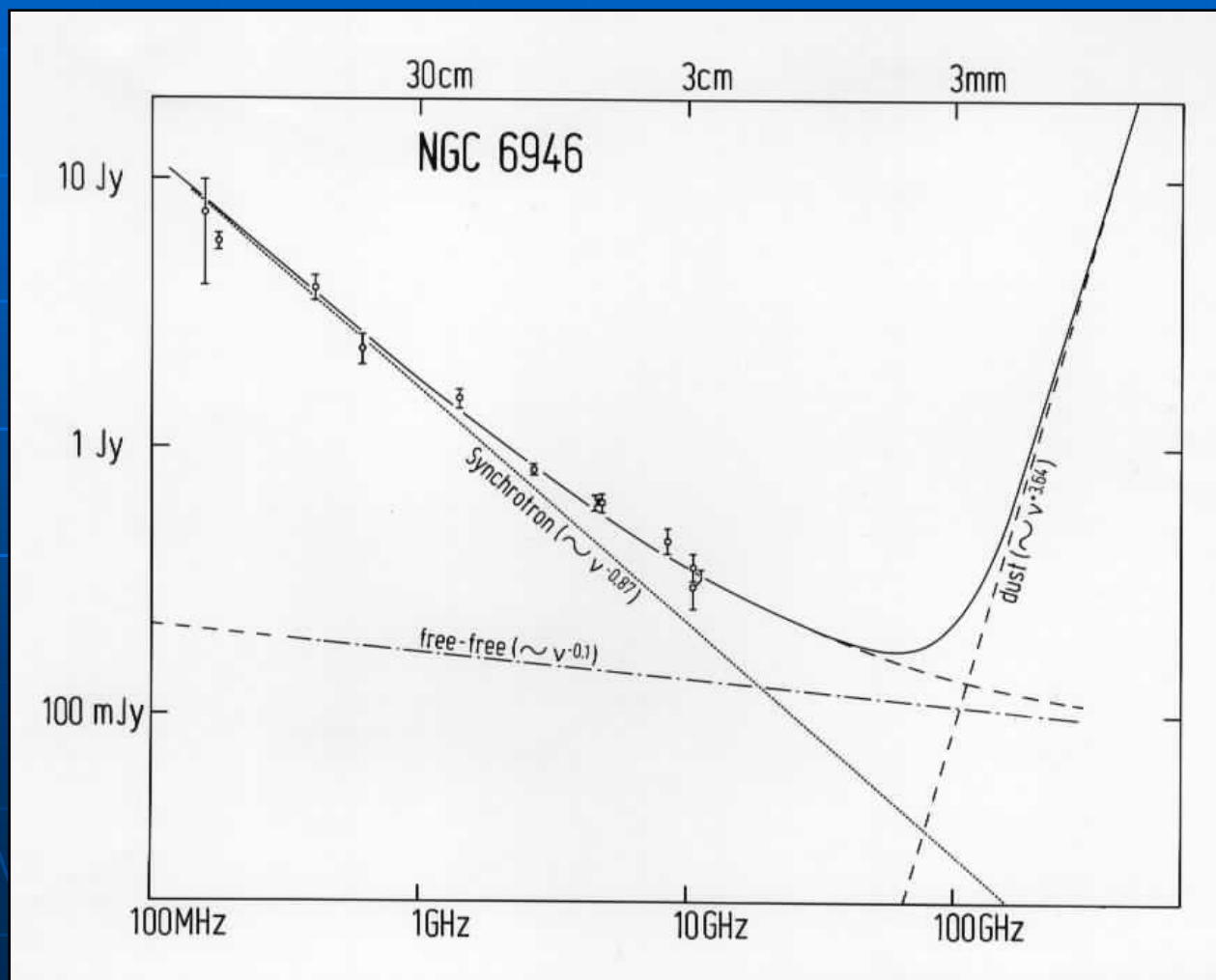
Synchrotron lifetime of GeV CRE

$$t_{\text{syn}} \approx 1 \text{ Gyr } B_{\perp} [\mu\text{G}]^{-1.5} \nu_{\text{syn}} [\text{GHz}]^{-0.5}$$

Continuous injection:
synchrotron spectrum
steepens by $\Delta\alpha = 0.5$
above a critical frequency



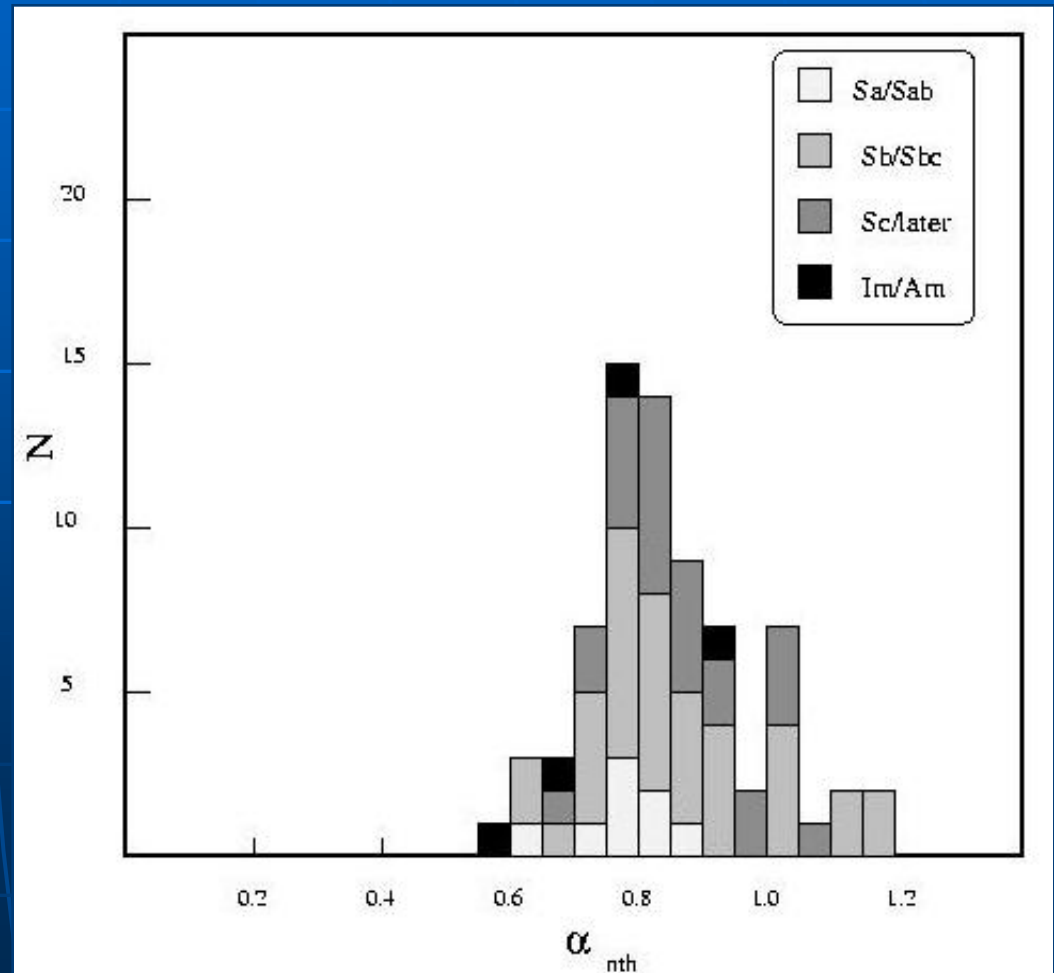
Typical radio continuum spectrum of a spiral galaxy



Thermal-nonthermal separation of total flux densities of galaxies

$$\alpha_{\text{sync}} = 0.85 \pm 0.05$$
$$\epsilon = 2.7 \pm 0.1$$

Niklas 1997



Origin of GeV CRE spectra in galaxies

Observed: $\varepsilon \approx 2.7$ in most galaxies (and in the Milky Way)

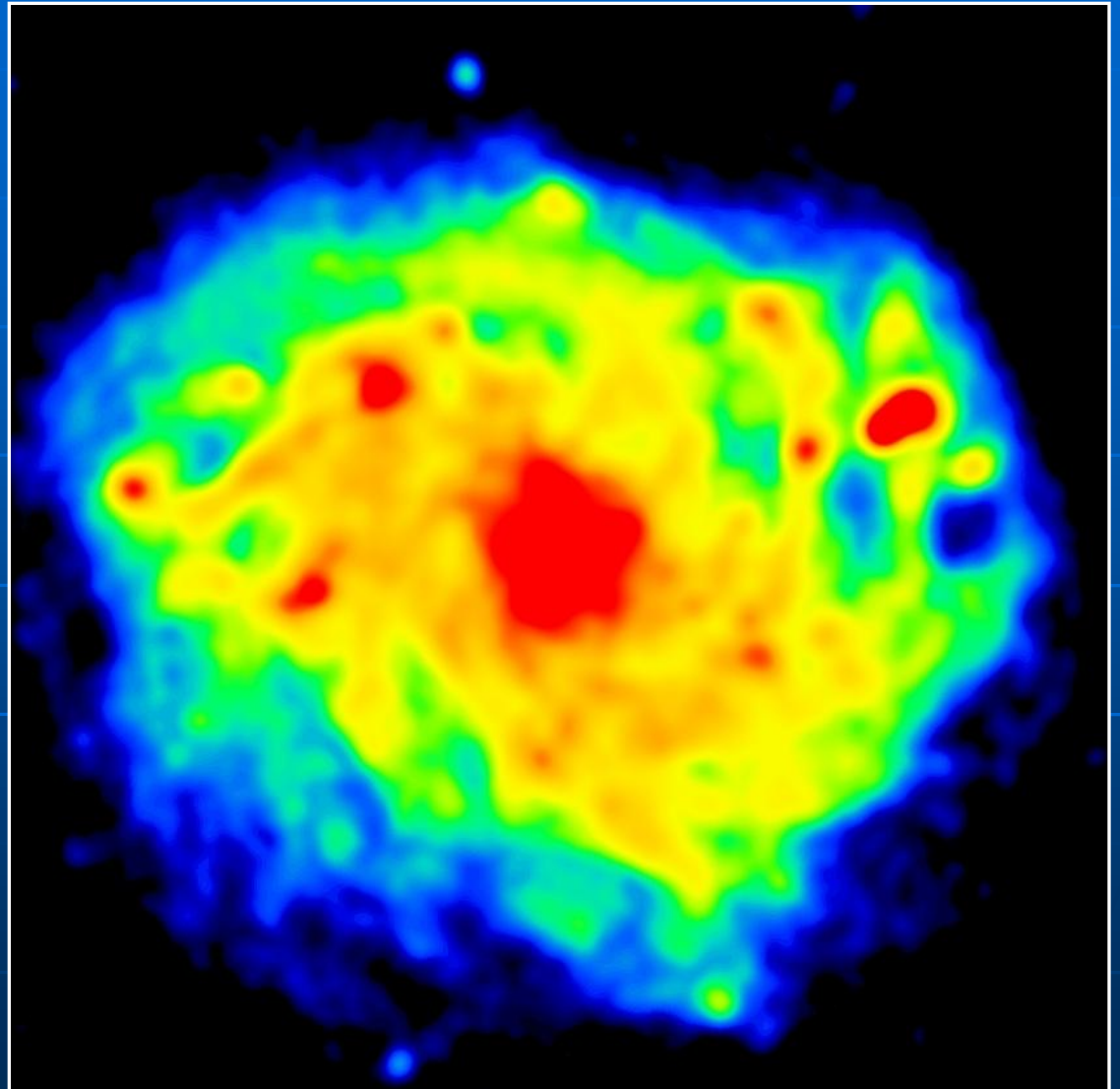
- Injection by supernova remnants ($\varepsilon \approx 2.2$)
+ energy-dependent escape ($\rightarrow \varepsilon \approx 2.7$)
- Mixture of young CRE from SNRs ($\varepsilon \approx 2.2$) and old CRE steepened by synchrotron loss ($\varepsilon \approx 3.2$)
- Injection with $\varepsilon \approx 2.7$ (?)

NGC 6946

20cm VLA
Total intensity
(Beck 2007)

Exponential
radio disk:
mostly synchrotron

Extent is limited by
energy losses of the
CRE



Typical exponential scale lengths of radio disks of spiral galaxies

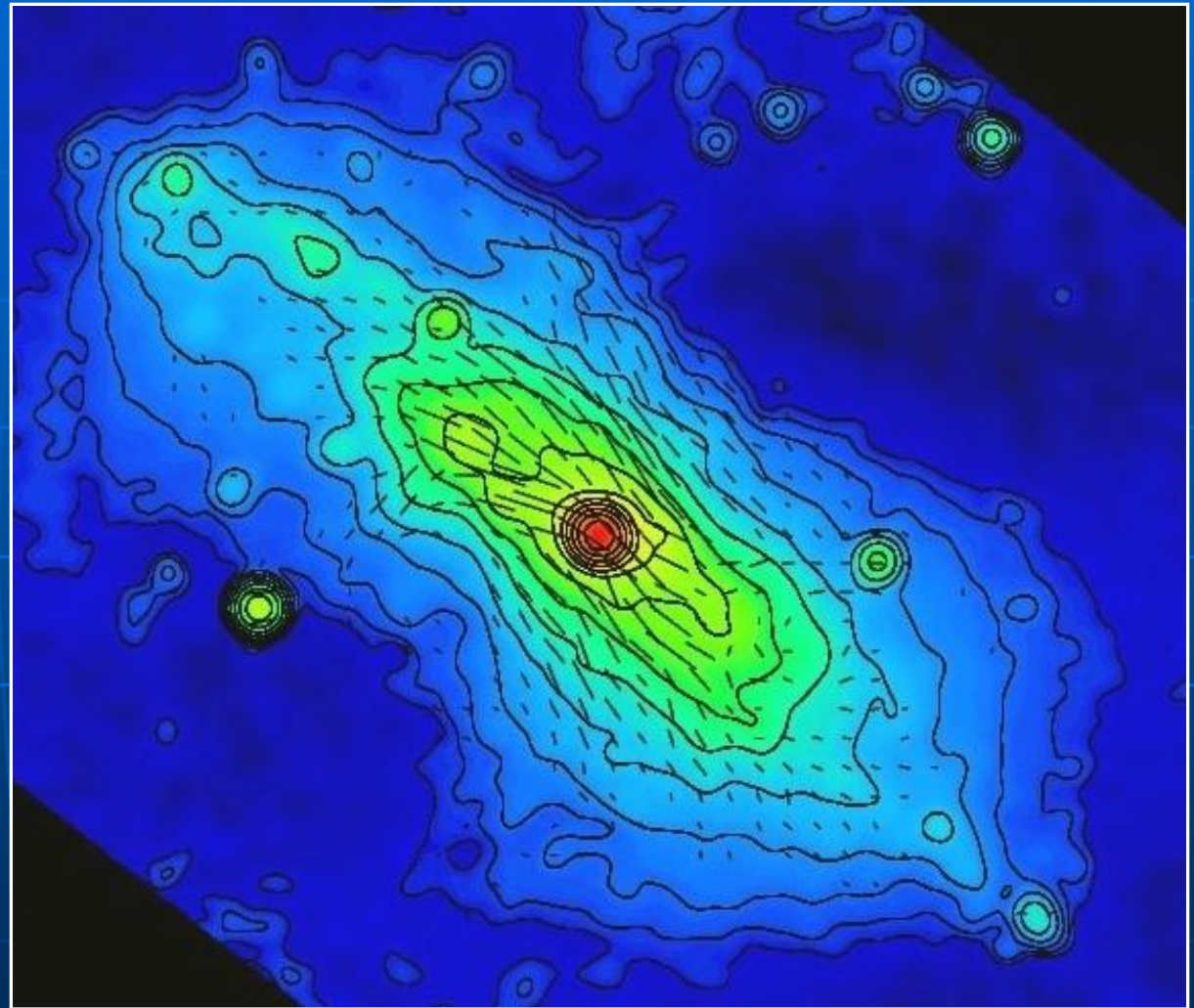
- Cold & warm gas: ≈ 4 kpc
- Synchrotron: ≈ 4 kpc
- **Cosmic-ray electrons: ≤ 8 kpc**
(assuming equipartition, upper limit due to energy losses)
- **Total magnetic field: ≥ 16 kpc**

NGC 253

6cm
VLA+Effelsberg
Total intensity
+ B-vectors
(Heesen et al. 2009)

Exponential
radio halo:

Extent is limited by
energy losses of the
CRE



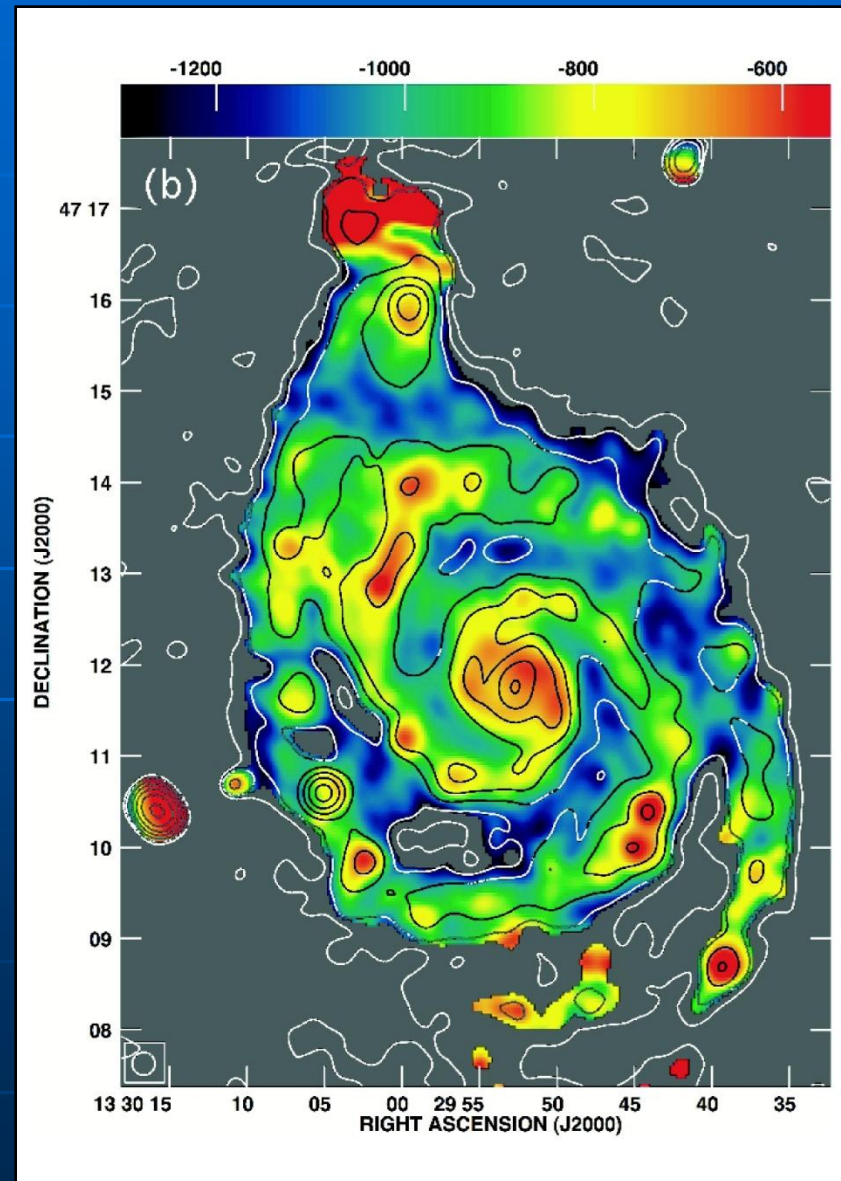
Typical exponential scale heights of radio halos

- Cold gas: ≈ 0.1 kpc
- Warm gas: ≈ 1 kpc
- Synchrotron: ≈ 2 kpc
- **Cosmic-ray electrons: ≤ 4 kpc**
(assuming equipartition, upper limit due to energy losses)
- **Total magnetic field: ≥ 8 kpc**

Spectral index in M51

Spectral index is flat
in the spiral arms and
steep in interarm regions:

Synchrotron & IC
losses of CRE



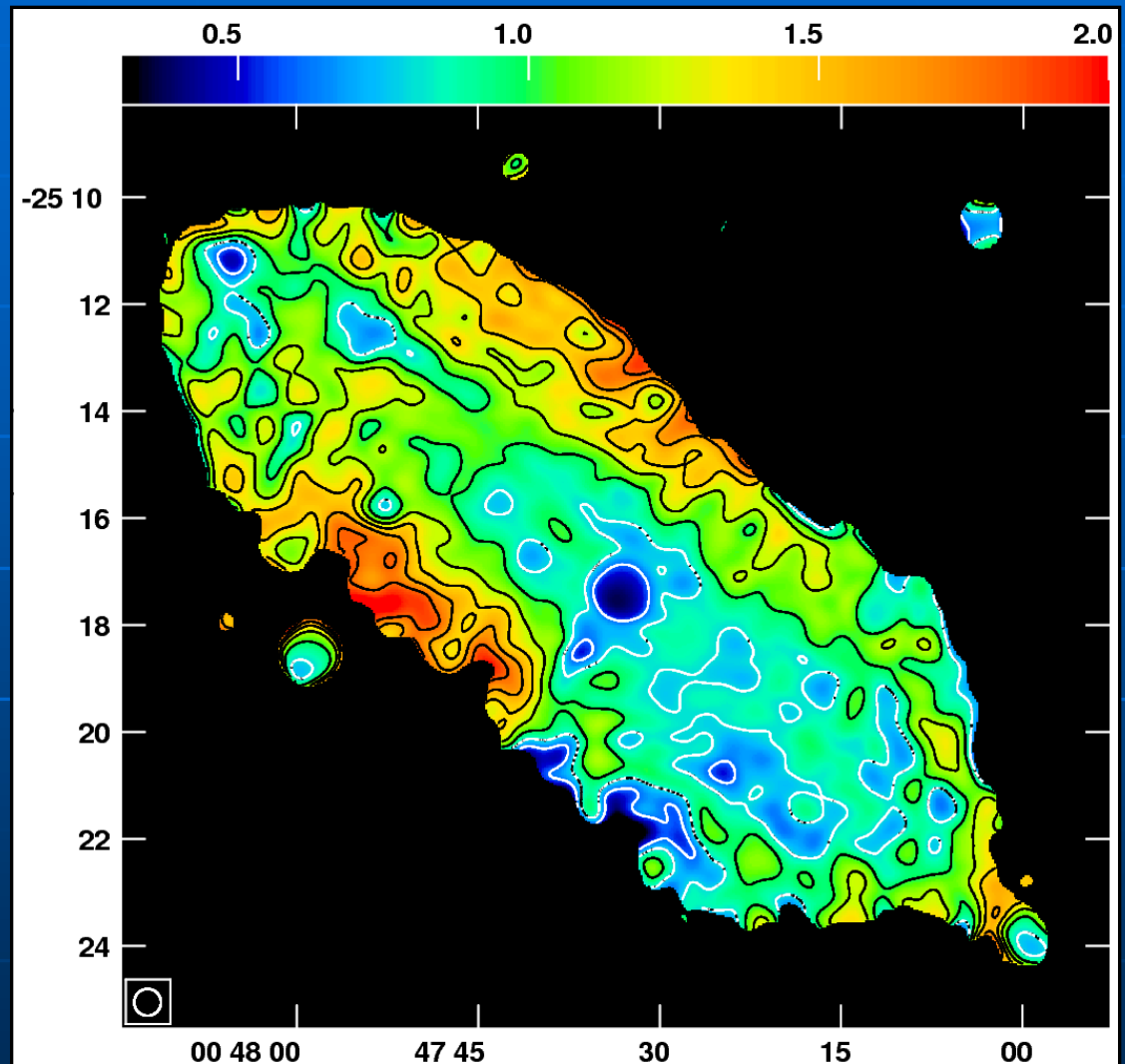
NGC 253

Spectral index
6/20cm

(Heesen et al. 2009)

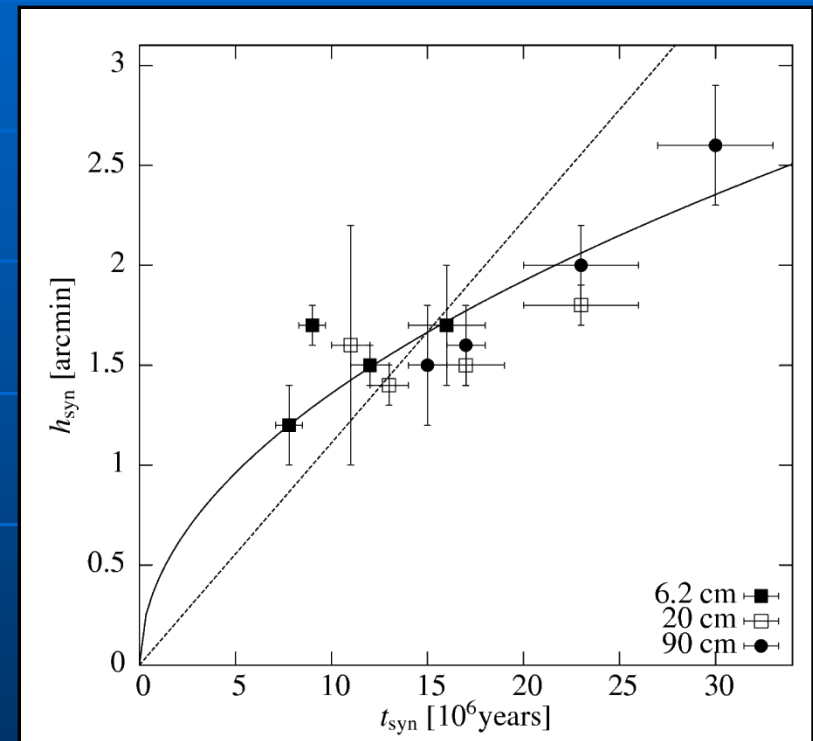
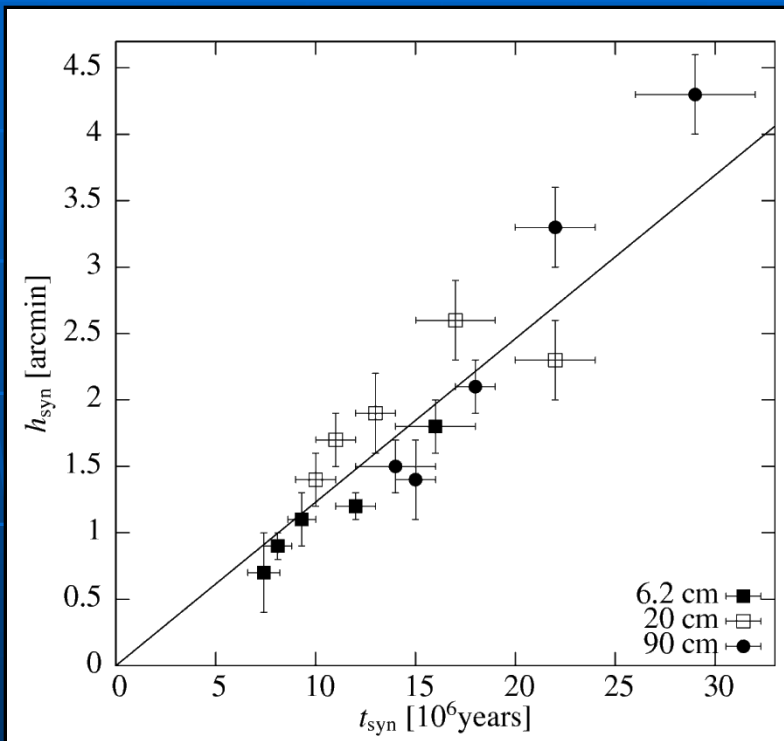
Spectral index
steepens with height:

Synchrotron & IC
losses of CREs



Scale heights of cosmic-ray electrons in NGC 253

Heesen et al. 2009



- North: Convection dominates, bulk speed $v_z = 300 \pm 30$ km/s
- South: Diffusion dominates, $D = (2 \pm 0.2) 10^{29}$ cm² s⁻¹

Radio continuum tools to study Magnetic fields

- **Total synchrotron intensity:**
Strength of total B_{\perp}
- **Polarized synchrotron intensity:**
Strength and structure of ordered B_{\perp}
- **Faraday rotation:**
Strength and sign of ordered B_{\parallel}
- **Faraday depolarization:**
Strength and scale of turbulent fields

Equipartition strength of the total field

(assuming equipartition between magnetic fields and cosmic rays)

Beck & Krause 2005

$$B_{eq,\perp} \propto \left(I_{sync} (K+1) / L \right)^{1/(3+\alpha)}$$

I_{sync} : Synchrotron intensity

L : Pathlength through source

α : Synchrotron spectral index

K : Ratio of cosmic-ray proton/electron number densities n_p/n_e
Usual assumption: $K \approx 100$ (no energy losses of CR electrons)

Energy spectra of cosmic rays

Diffusive shock acceleration:

$$\varepsilon \geq 2$$

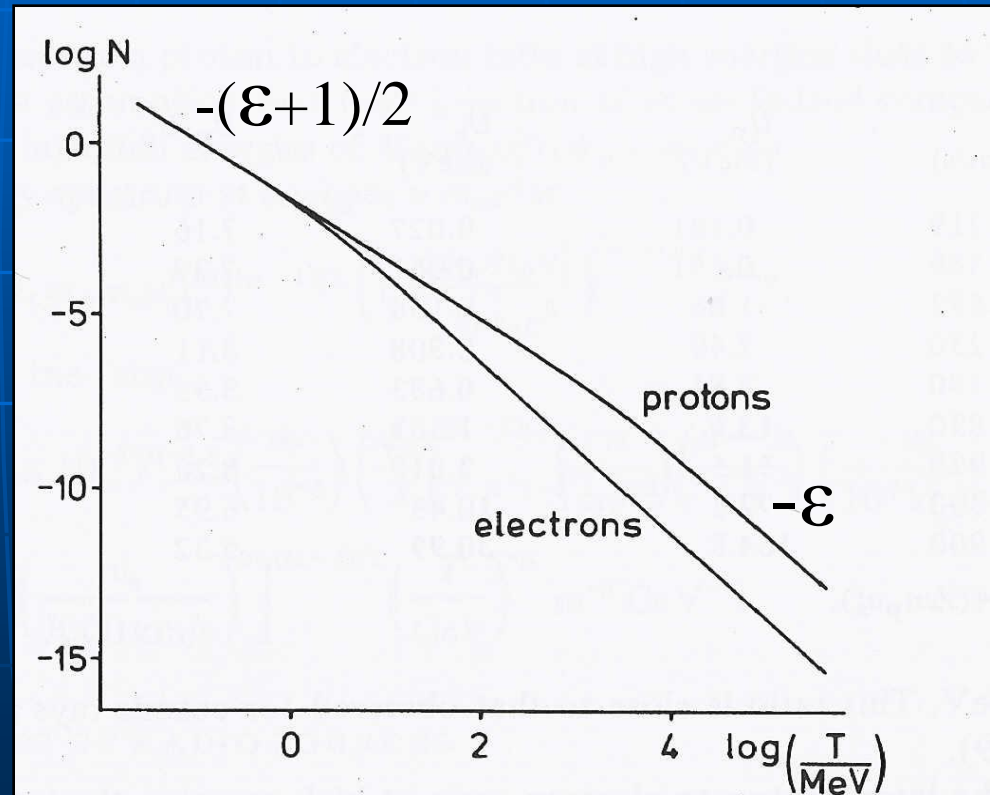
$$\alpha \geq 0.5$$

$E > 1$ GeV:

$$K = (m_p/m_e)^{(\varepsilon-1)/2}$$

$$\varepsilon \approx 2.2: K \approx 90$$

Bell 1978



Equipartition magnetic field strengths

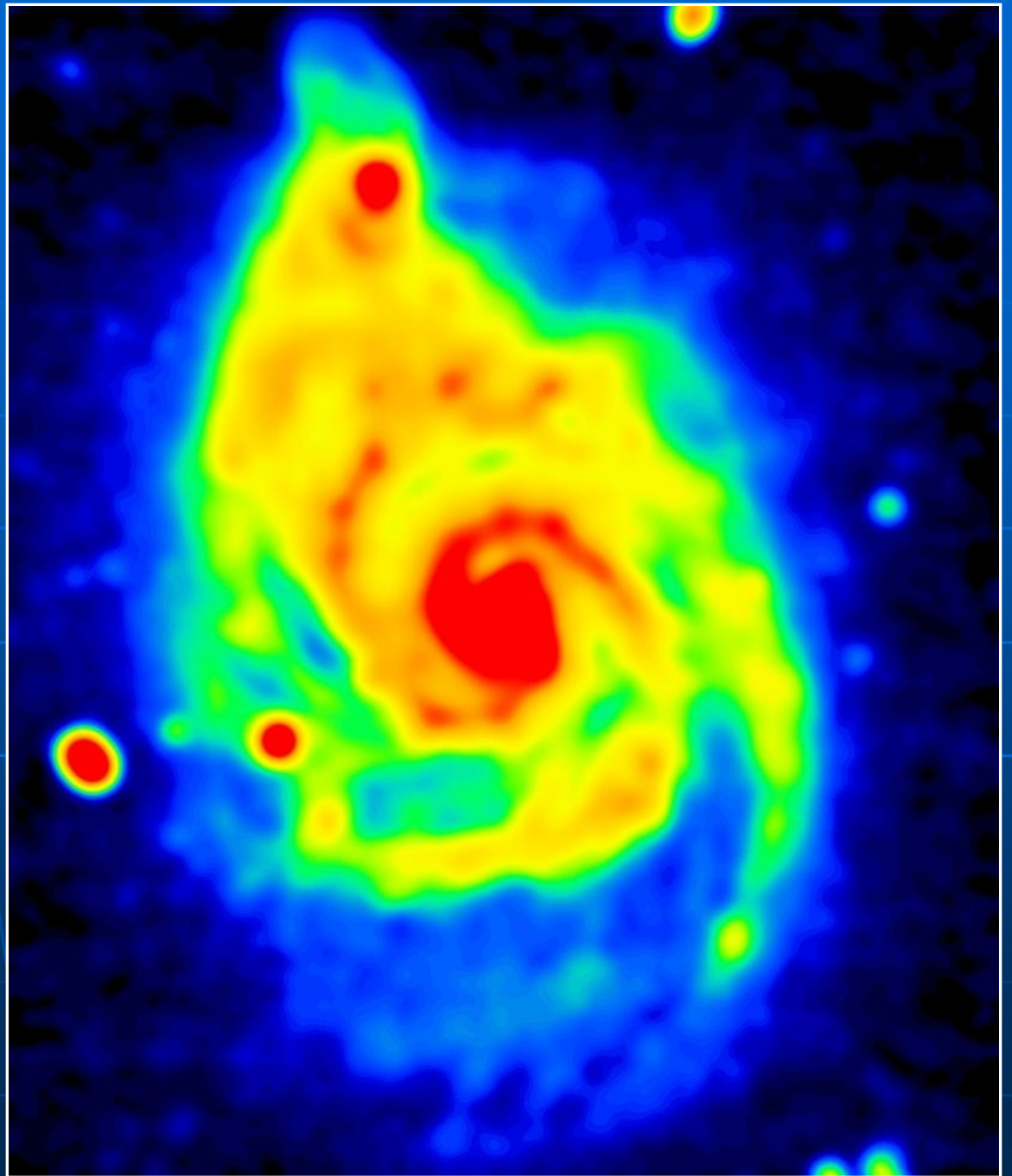
CRE energy losses:

- Spectral index (ϵ_e) is modified
- Proton/electron ratio is larger than 100
- **Equipartition field estimate is too small**
(Beck & Krause 2005)

Needed: independent data on CR proton spectrum
(e.g. from γ rays) or CR electron spectrum (from X-rays)

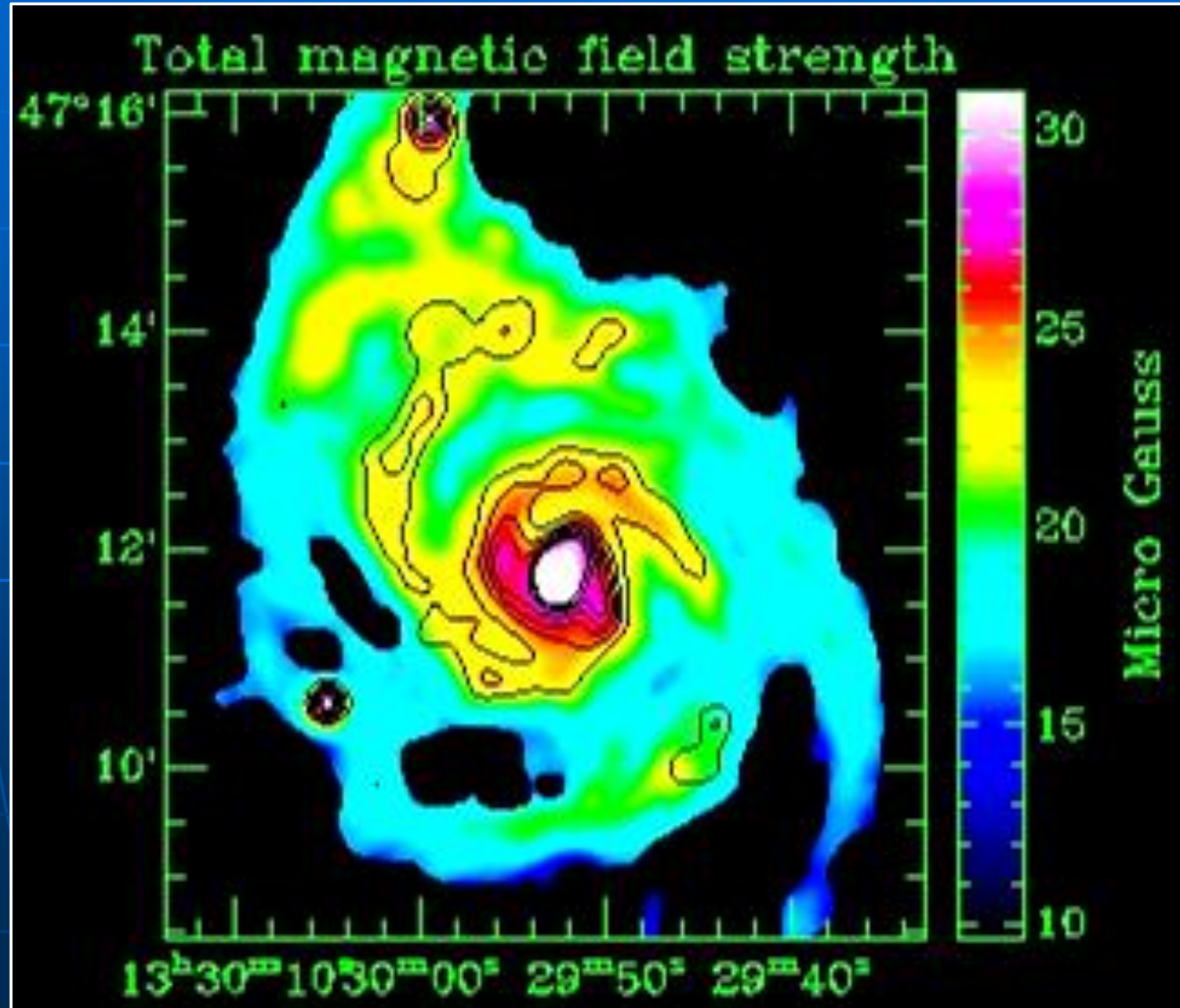
M 51

20cm VLA
Total intensity
(Fletcher et al. 2010)



Equipartition field strengths in M 51

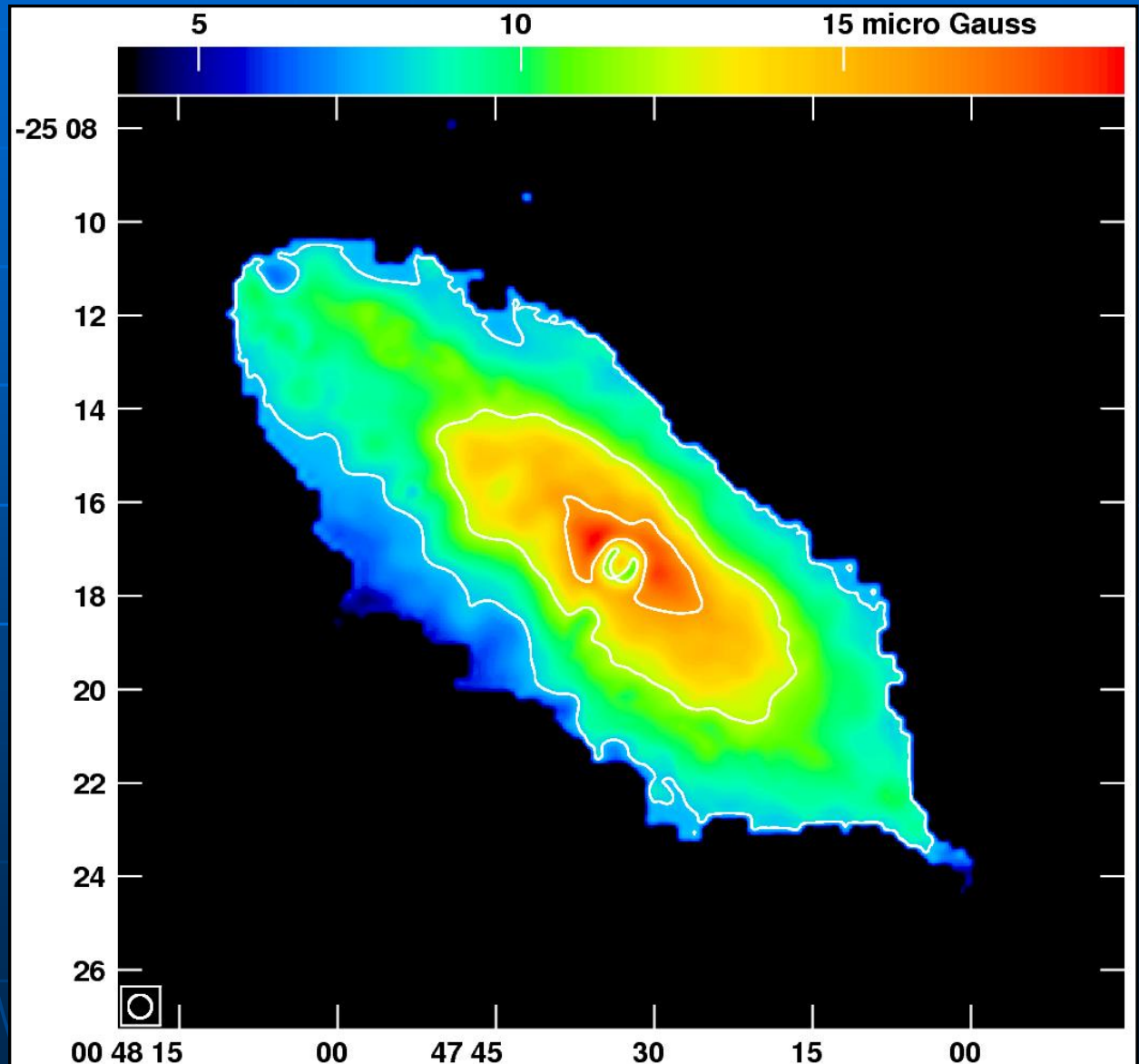
Equipartition underestimates the field in the outer galaxy due to energy losses of CRE



Fletcher et al. 2010

Equipartition field strengths in NGC 253

Equipartition underestimates the halo field due to energy losses of CR electrons



Heesen et al. 2009

Equipartition magnetic field strengths in spiral galaxies

Total field in spiral arms:	20 - 30 μG
Regular field in interarm regions:	5 - 15 μG
Total field in circum-nuclear rings:	40 - 100 μG
Total field in galaxy center filaments:	$\approx 1 \text{ mG}$

Synchrotron polarization

for a power-law electron spectrum

Intrinsic degree of linear polarization:

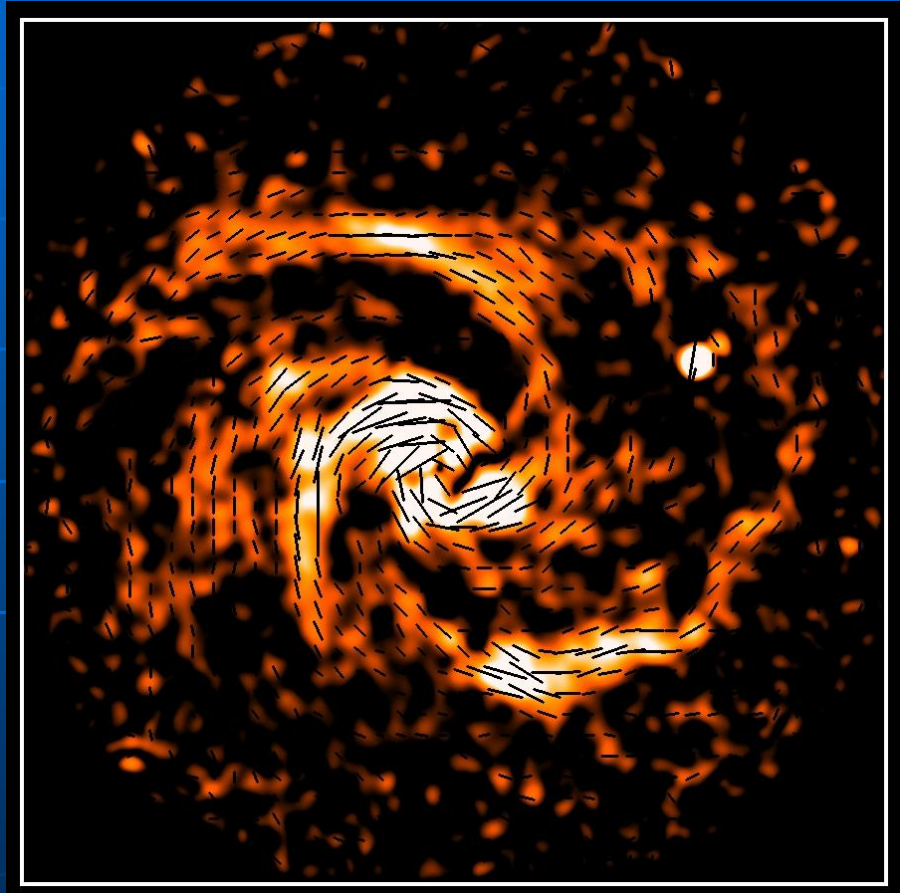
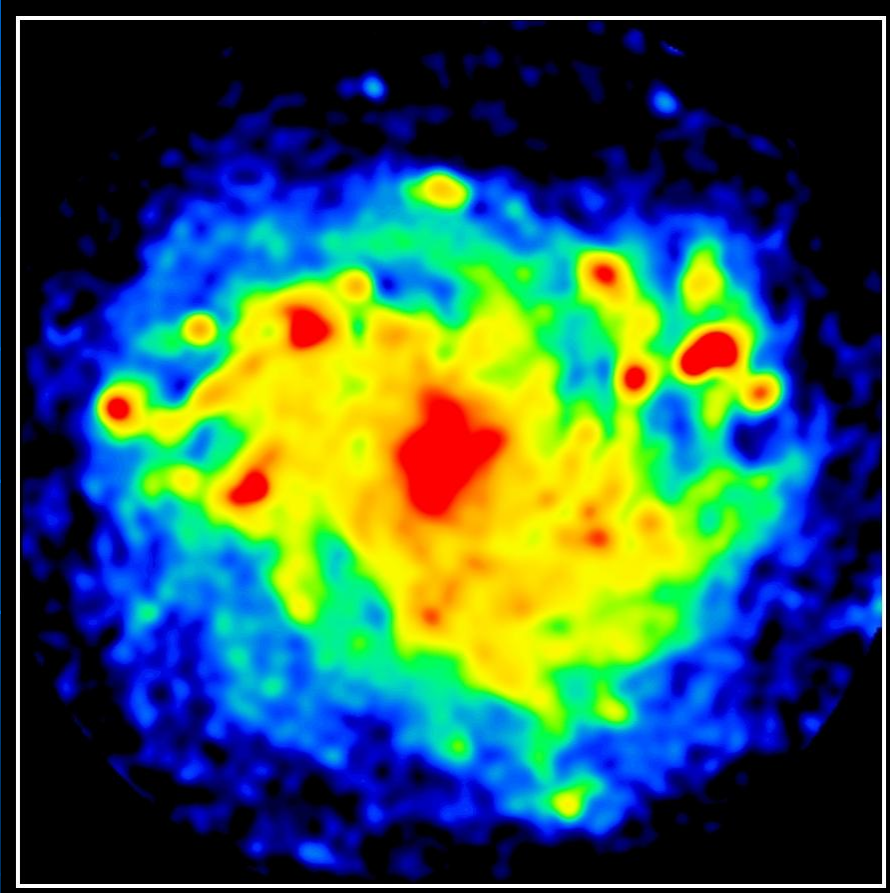
$$p_o = (\varepsilon+1) / (\varepsilon+7/3)$$
$$= (\alpha+1) / (\alpha+5/3)$$

Typical value: $\alpha=0.85$, $p_o=74\%$

Note: circular polarization is generally negligible

Synchrotron polarization

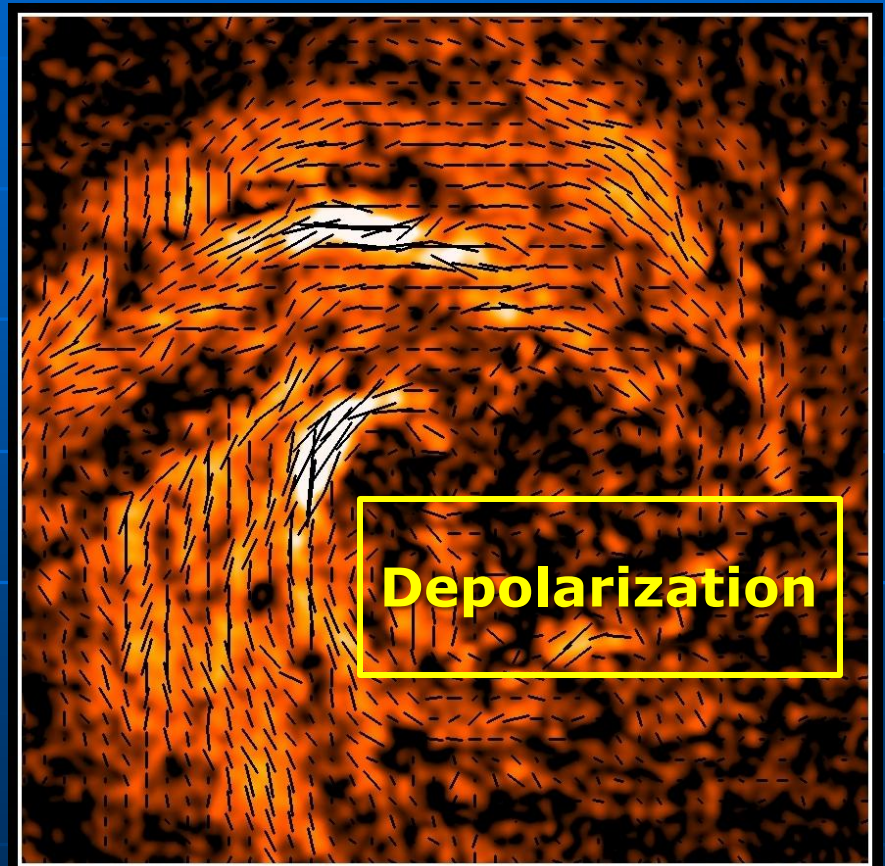
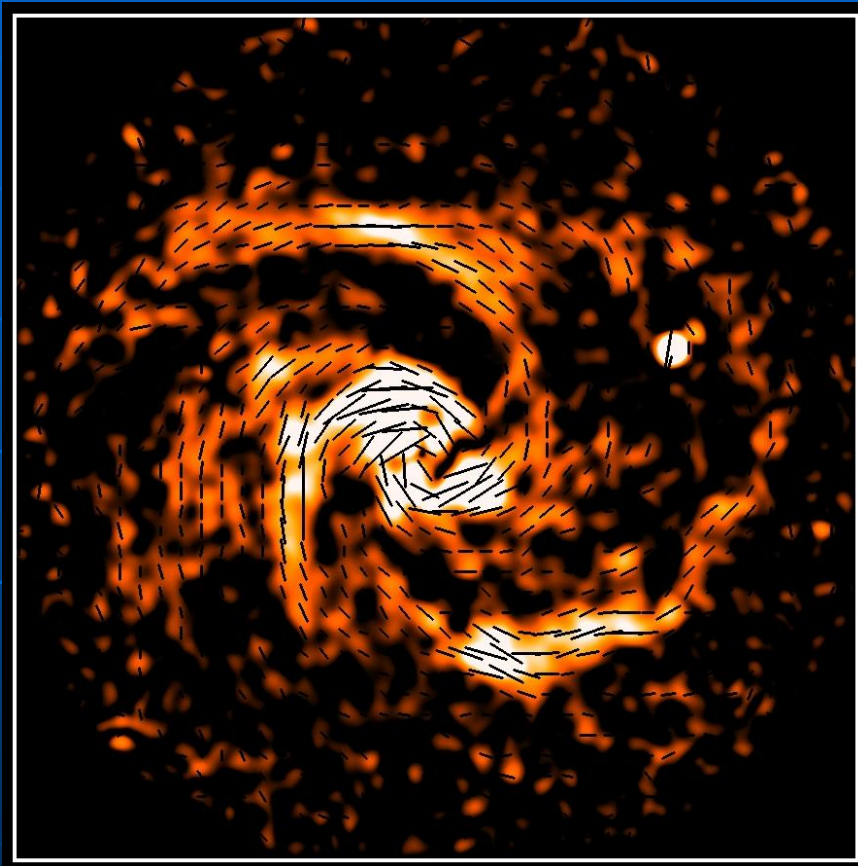
Beck & Hoernes 1996



NGC 6946 Total and polarized intensity at 6cm

Faraday depolarization

Beck 2007



NGC 6946 Polarized intensity at 6cm and 20.5cm

Degree of polarization in galaxies:

$\leq 5\%$ in spiral arms

20 - 60% in magnetic arms at ≥ 5 GHz,

$\leq 10\%$ at ≤ 1.4 GHz

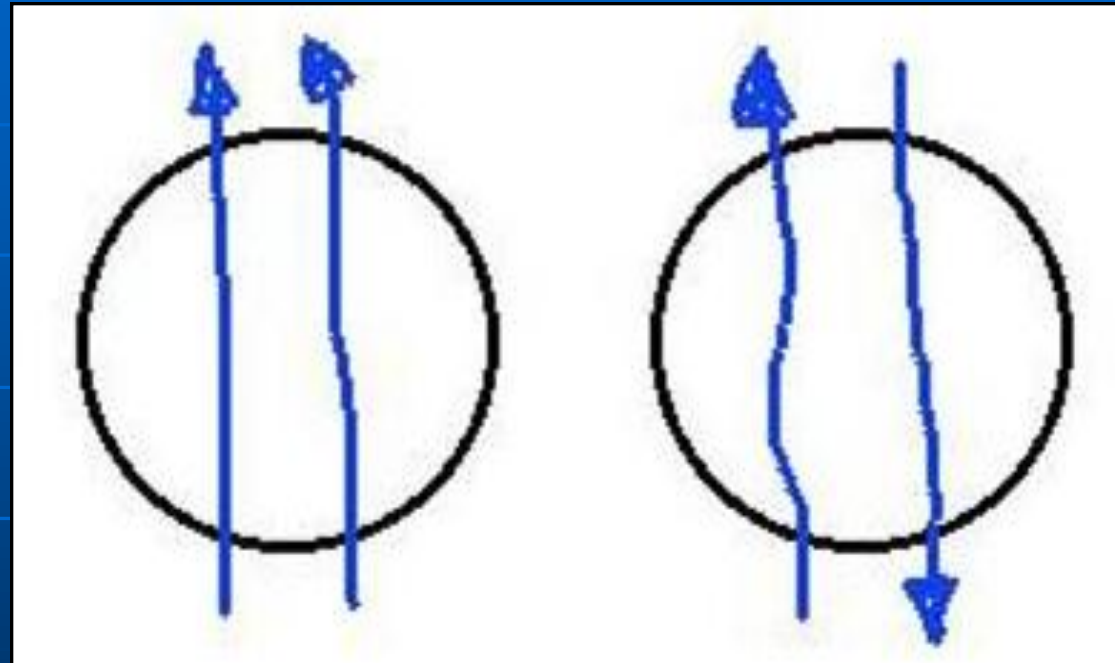
Ratio of random to regular magnetic fields:

≥ 4 in spiral arms and starburst regions,

0.5 - 2 in magnetic arms

Regular
(coherent)
field

Anisotropic
(incoherent)
field



Polarization :

strong

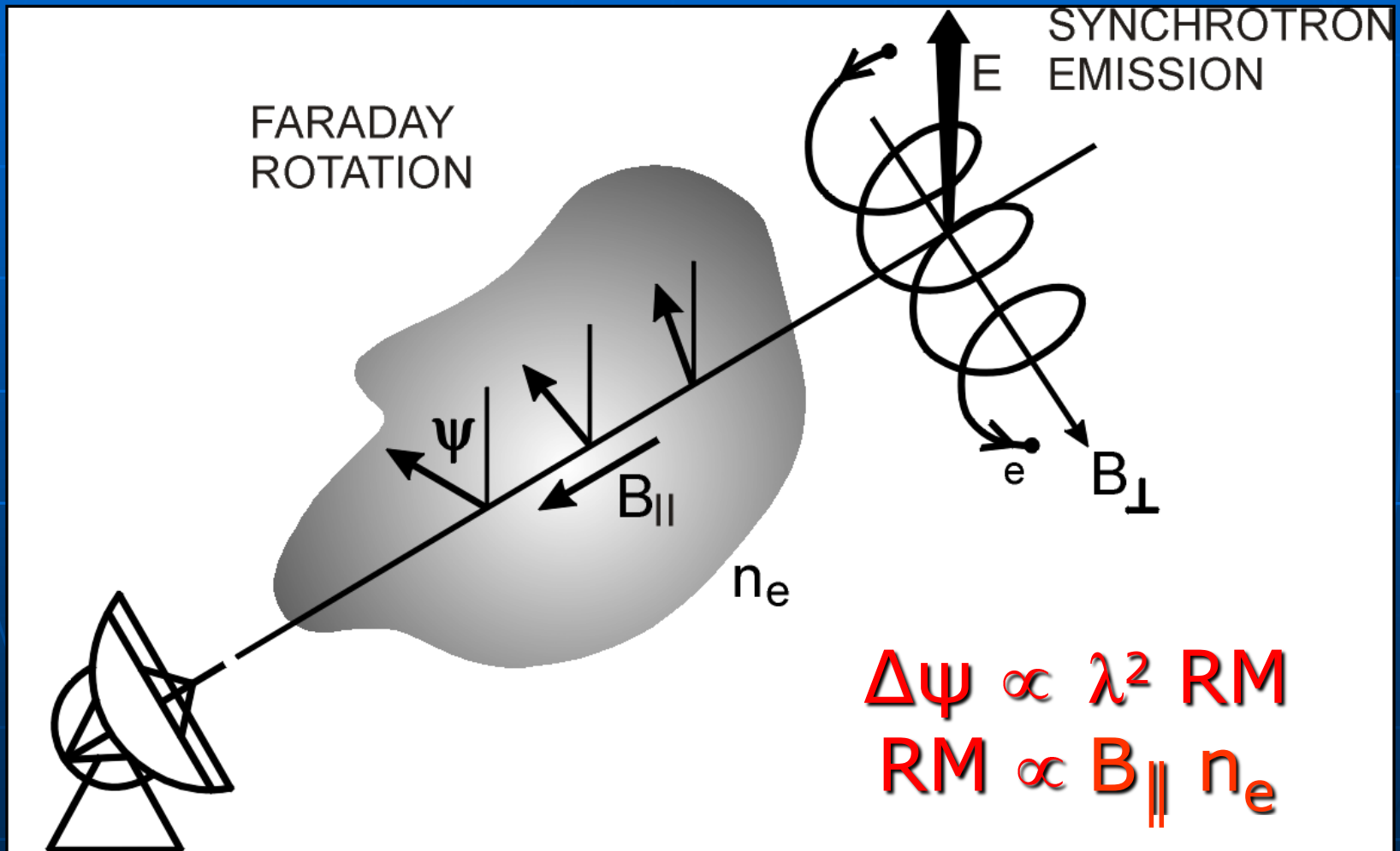
strong

Faraday rotation :

high

low

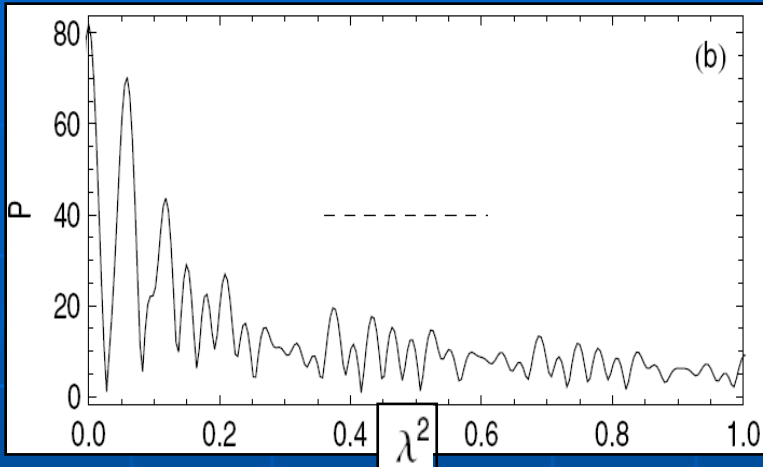
Faraday rotation



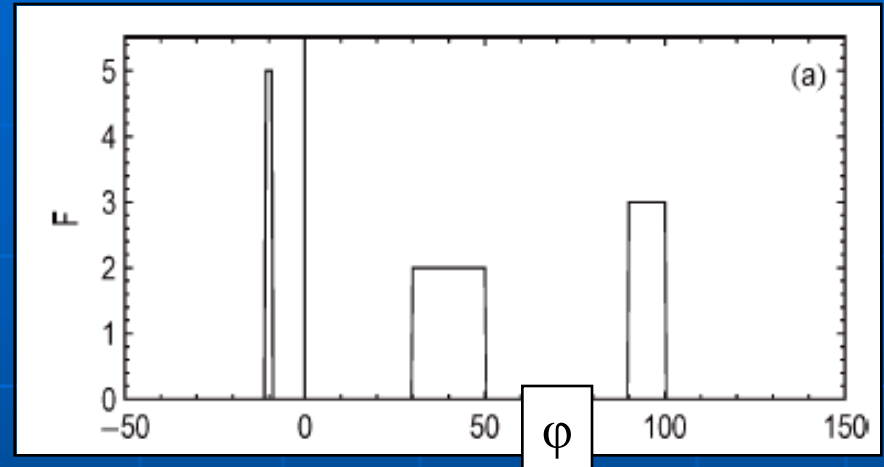
Faraday rotation angles

	 RM =	10	1	0.1 rad m⁻²
1400 MHz	$\Delta\chi =$	30°	3°	0.3°
200 MHz	$\Delta\chi =$	1300°	130°	13°
120 MHz	$\Delta\chi =$	3600°	360°	36°

RM Synthesis



Frequency spectrum of complex polarized intensity



Faraday spectrum of Faraday depth components

The observed complex polarization P is the Fourier transform of the complex **Faraday spectrum $F(\varphi)$** (the "source distribution" in Faraday depth φ)

RM Synthesis

(radio spectro-polarimetry)

- The observed spectrum of complex polarization in frequency is Fourier-transformed into the **Faraday spectrum** in **Faraday depth**
- **Faraday depth** ($\varphi \propto \int B_{\parallel} n_e dl$) is a physical quantity, different from the classical (observable) rotation measure
- The **Faraday spectrum** allows to model different layers of magneto-ionic gas along the line of sight (**Faraday tomography**)

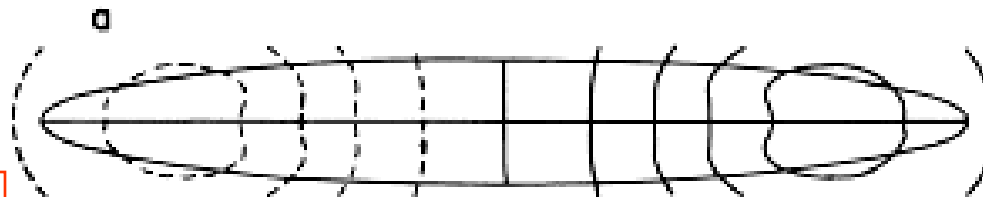
“Mean-field” dynamo theory for galactic magnetic fields

- Ingredients:
Ionized gas + differential rotation + turbulence
- Dynamical separation between large scales and small scales
- Microphysics approximated by the average parameters
“alpha-effect” (helicity) and magnetic diffusivity
- Solutions: large-scale modes

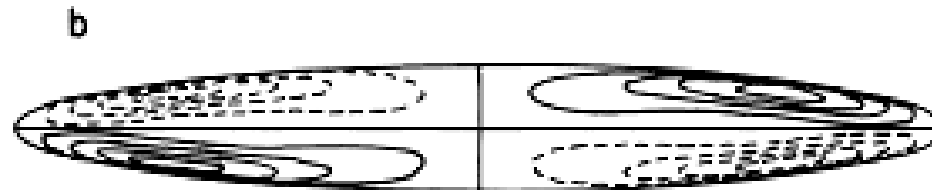
Antisymmetric and symmetric dynamo modes

Stix 1975

A0 mode



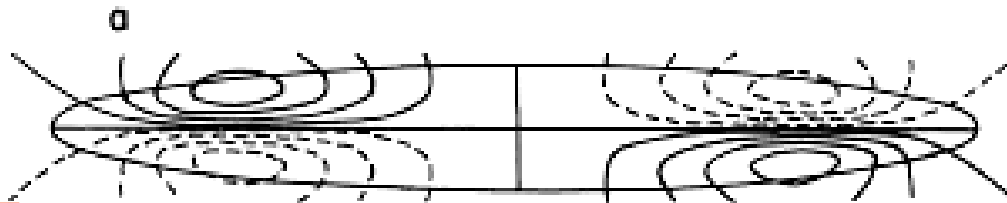
Dipolar poloidal field



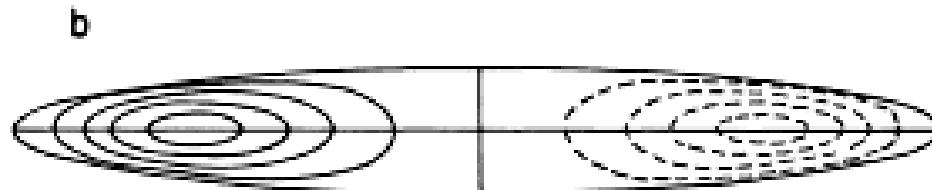
Reversing toroidal field in the plane

Fig. 1a and b. Poloidal field lines (a) and curves of constant toroidal field strength (b) for a dipole type field, with $R = 15$ kpc, $b = 2$ kpc, and $P = 1.1 \cdot 10^3$

S0 mode



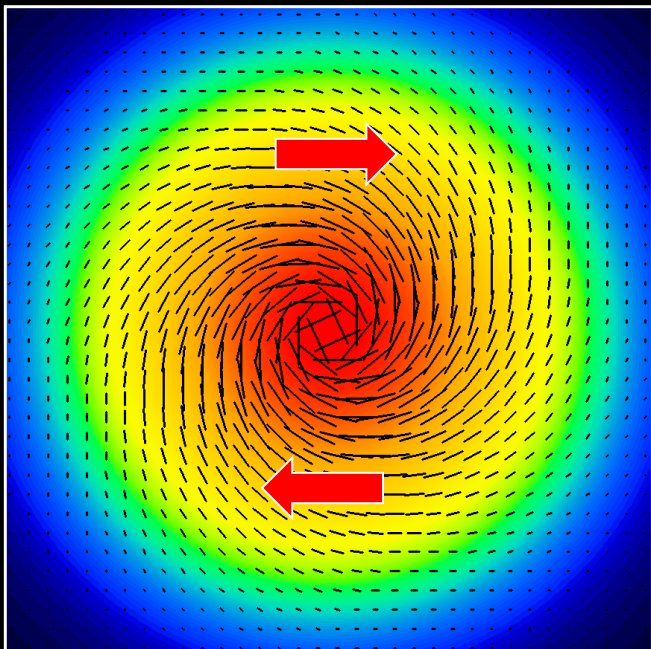
Quadrupolar poloidal field



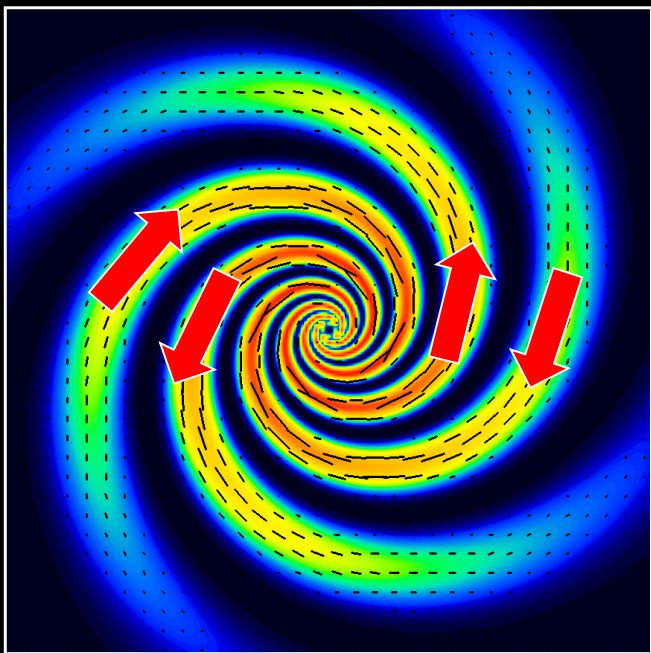
No reversing toroidal field

Fig. 2a and b. Poloidal field lines (a) and curves of constant toroidal field strength (b) for a quadrupole type field, with $R = 15$ kpc, $b = 2$ kpc, and $P = -8.5 \cdot 10^3$

Dynamo Mode 0 (Axisymmetric Spiral)

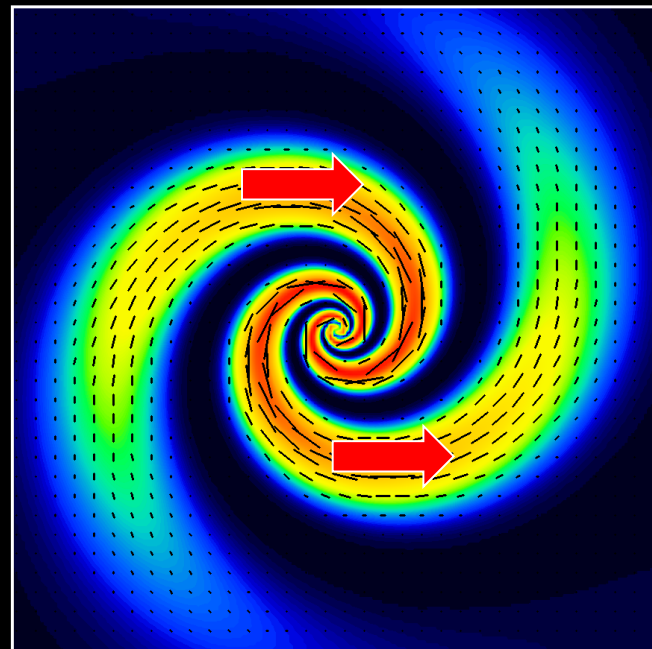


Dynamo Mode 2 (Quadrilateral Symmetric Spiral)

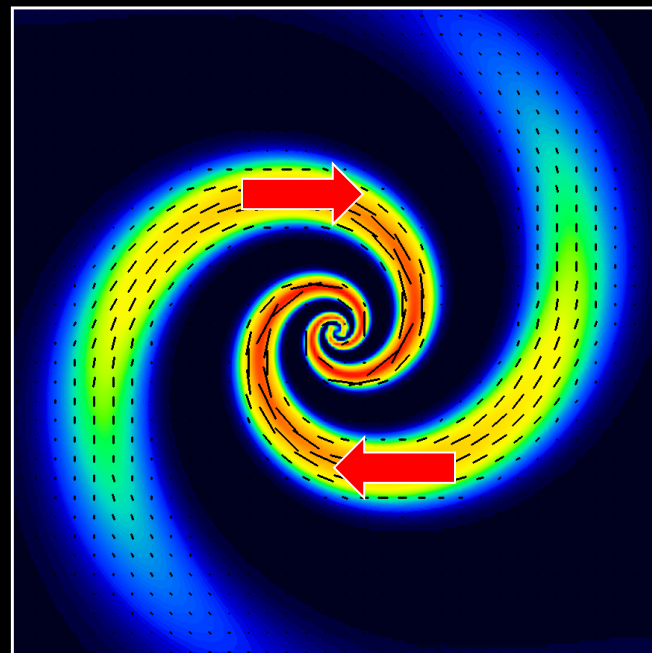


dyna

Dynamo Mode 1 (Bisymmetric Spiral)

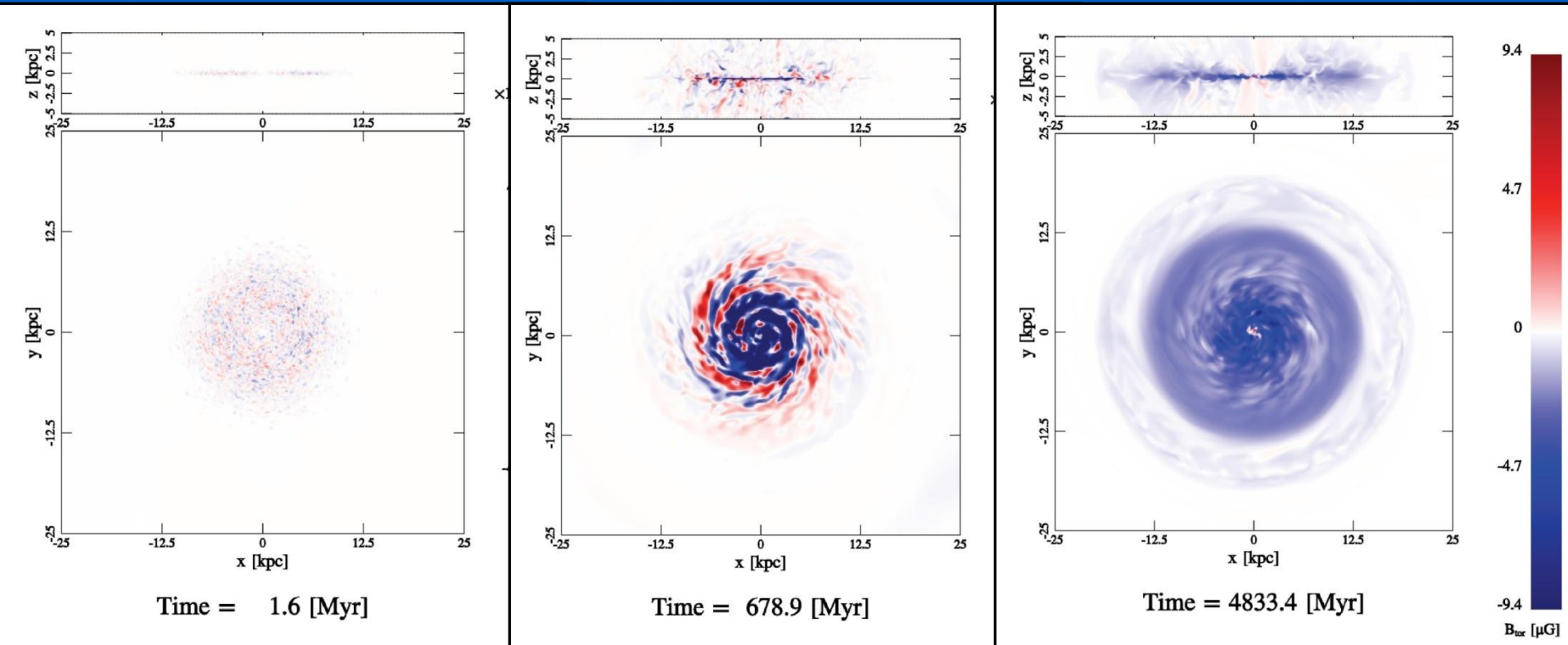


Dynamo Modes 0 + 2



Global cosmic-ray driven MHD model

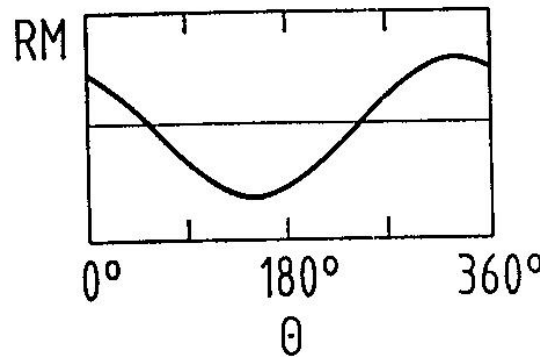
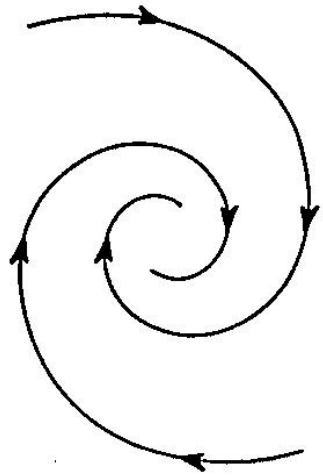
Hanasz et al. 2009



Generation of a dominant axisymmetric mode:
Confirmation of the mean-field model

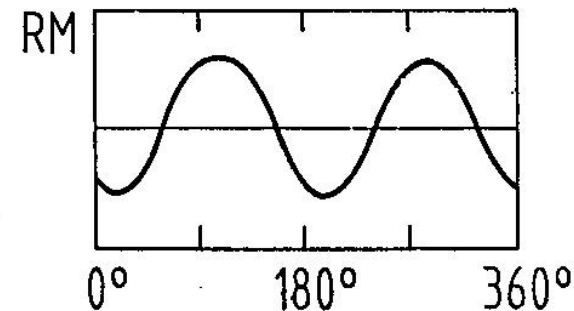
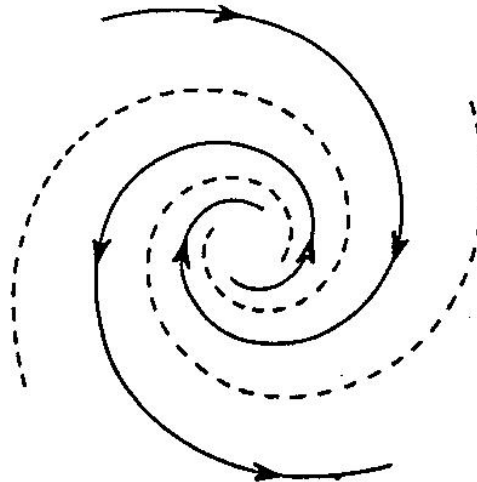
Finding dynamo modes: Azimuthal variation of Faraday rotation

Krause 1990



Axisymmetric spiral
($m=0$)

Bisymmetric spiral
($m=1$)



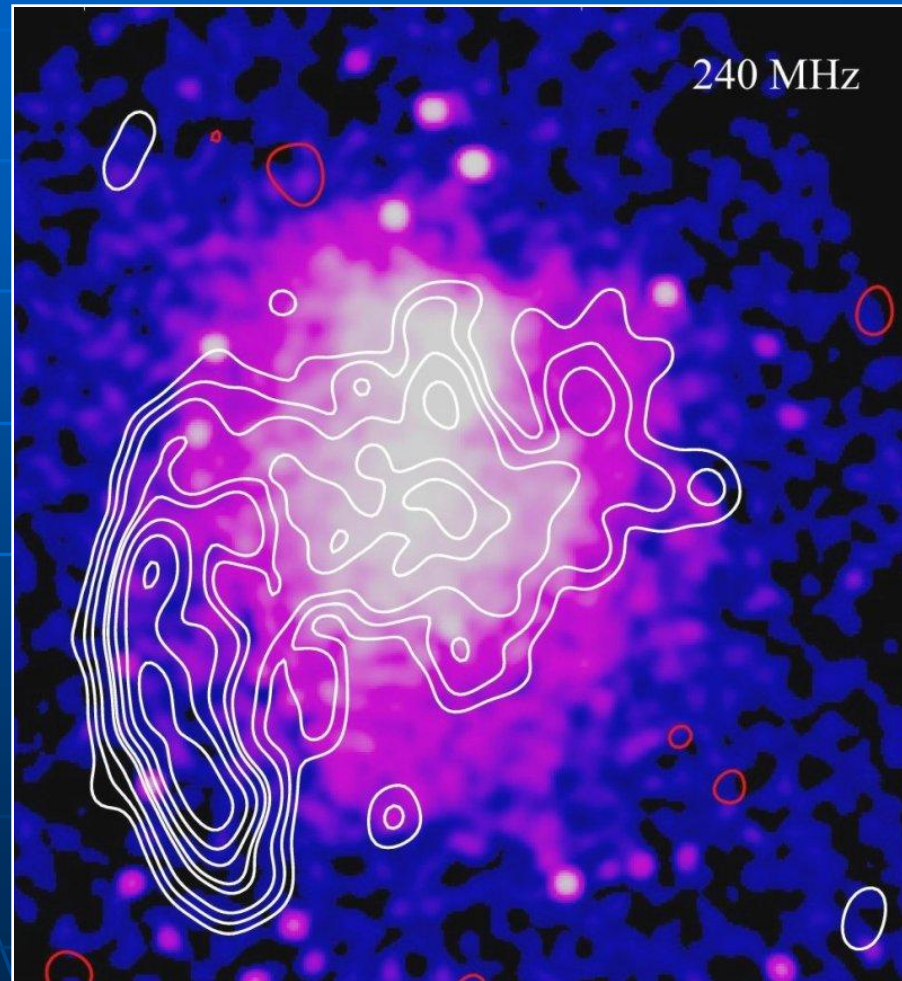
Future radio telescopes

- Higher resolution: EVLA, SKA
- Larger sensitivity: EVLA, MeerKAT, SKA
- Higher frequencies: ALMA
- Lower frequencies: LOFAR, SKA
- Higher survey speed: LOFAR, ASKAP, APERTIF, SKA

The advantages of low-frequency radio observations

- Low frequency synchrotron emission traces cosmic-ray electrons in **weak magnetic fields**
- Low frequencies trace **old cosmic-ray electrons far away from their acceleration sites**
- Low frequencies measure **small rotation measures from weak magnetic fields**

Halo and relic emission from Abell521 (GMRT 240MHz)



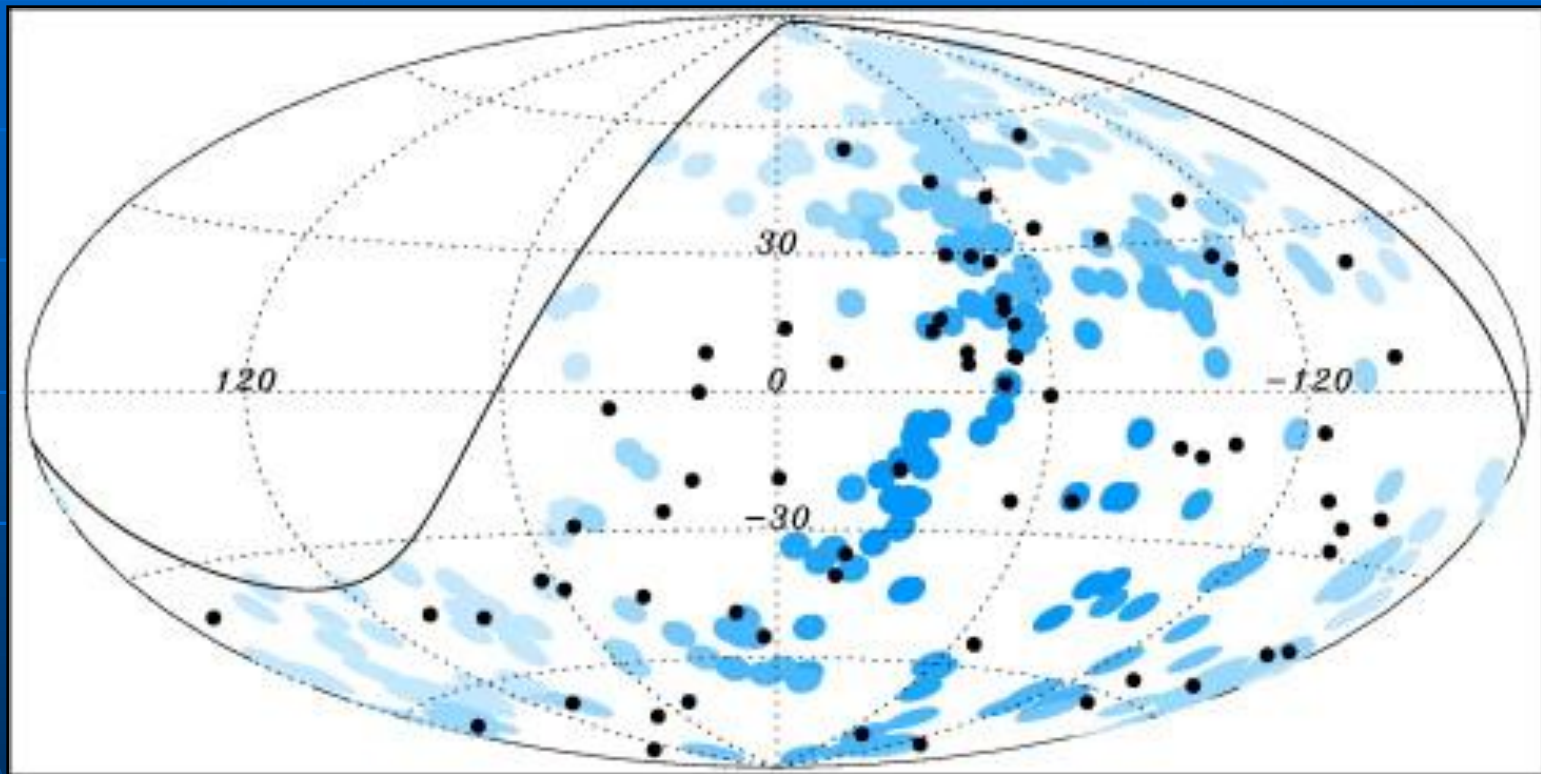
Brunetti et al.
2008

Faraday rotation with LOFAR

- LOFAR can measure very low Faraday rotation measures of polarized background sources and hence detect very **weak magnetic fields**:
- **Galaxy halos, clusters, relics:**
 $n_e = 10^{-3} \text{ cm}^{-3}$, $B_{\parallel} = 1 \text{ } \mu\text{G}$, $L = 1 \text{ kpc}$: $RM \sim 1 \text{ rad m}^{-2}$
- **Intergalactic magnetic fields:**
 $n_e = 10^{-5} \text{ cm}^{-3}$, $B_{\parallel} = 0.1 \text{ } \mu\text{G}$, $L = 100 \text{ kpc}$: $RM \sim 0.1 \text{ rad m}^{-2}$

AUGER UHECR events ($> 5 \cdot 10^{19}$ eV)

AUGER 2010



Localizing the UHECR sources requires knowledge about the Milky Way's magnetic field