Magnetic-free non-reciprocity and isolation based on parametrically modulated coupled-resonator loops

Nicholas A. Estep†, Dimitrios L. Sounas†, Jason Soric and Andrea Alù*

Non-reciprocal components, which are essential to many modern communication systems, are almost exclusively based on magneto-optical materials, severely limiting their applicability. A practical and inexpensive route to magnetic-free non-reciprocity could revolutionize radio-frequency and nanophotonic communication networks. Angular-momentum biasing was recently proposed as a means of realizing isolation for sound waves travelling in a rotating medium1, and envisaged as a path towards compact, linear integrated non-reciprocal electromagnetic components2,3. Inspired by this concept, here we demonstrate a subwavelength, linear radio-frequency non-reciprocal circulator free from magnetic materials and bias. The scheme is based on the parametric modulation of three identical, strongly and symmetrically coupled resonators. Their resonant frequencies are modulated by external signals with the same amplitude and a relative phase difference of 120°, imparting an effective electronic angular momentum to the system. We observe giant non-reciprocity, with up to six orders of magnitude difference in transmission for opposite directions. Furthermore, the device topology is tunable in real time, and can be directly embedded in a conventional integrated circuit.

Early attempts to realize magnetic-free non-reciprocity were based on the non-reciprocal properties of transistors at microwave frequencies4, and on networks of electro-optical modulators at optical frequencies5–8. However, such approaches traded the absence of magnetic bias with other significant drawbacks, such as the strong nonlineairities and poor noise-performance of transistors, or the large size and complexity of the required electro-optical networks. More recently, non-reciprocity has been achieved in transistor-loaded metamaterials9,10 and nonlinear devices11–14. Also these solutions impose severe restrictions on the input power levels, generally degrading the signal quality because of noise or signal distortion. Another interesting approach to magnetic-free non-reciprocity has been introduced15, using asymmetric mode conversion in spatiotemporally modulated waveguides. This concept is especially attractive for integrated optical networks, as it may be fully realized in silicon photonics16. However, this technique and its variants17–22 lead to structures much larger than the wavelength, owing to the weak electro-optic or acousto-optic effects on which they rely, and require complex modulation schemes. In a similar context, the concept of a non-reciprocal device based on parametrically coupled resonators has been theoretically explored23.

An approach that can lead to compact, magnetic-free non-reciprocal devices with relaxed implementation complexity was recently introduced24,25, based on angular-momentum biasing of a resonant ring. Angular momentum can be applied either by mechanically spinning a fluid, as proved for acoustic waves1, or, more conveniently for electromagnetic waves, by spatiotemporal modulation with a travelling wave, realizing an effective electronic spin25, as illustrated in Fig. 1a. The resonant nature of the modulated ring can substantially boost the otherwise weak electro-optic effects through which spatiotemporal modulation is typically achieved25,26, allowing the design of largely non-reciprocal devices with dimensions of the order of, or even smaller than the wavelength. Furthermore, in contrast to other approaches based on spatiotemporal modulation25,26, angular-momentum biasing is based on uniform modulation across the ring cross-section, thus significantly simplifying the fabrication process.

Inspired by these ideas, here we propose a device that provides strong magnetic-free non-reciprocity at the subwavelength scale.

**Figure 1 | Magnetic-free non-reciprocity with angular-momentum biasing.** a, An azimuthally symmetric ring with spatiotemporal permittivity modulation \( \Delta \varepsilon(\varphi, t) = \Delta \varepsilon_m \cos(\omega_m t - \Omega_m \varphi) \). The modulation imparts an effective electronic spin to the ring, with angular velocity \( \Omega_m = \omega_m / l_m \), which lifts the degeneracy of counter-propagating resonant states and induces non-reciprocity. Its practical realization typically involves discretizing \( \Delta \varepsilon \) into \( N \) different regions (three in the figure). b, A loop consisting of three strongly coupled resonators, whose frequencies are modulated according to \( \omega_1(t) = \omega_0 + \Delta \omega_1 \cos(\omega_m t) \), \( \omega_2(t) = \omega_0 + \Delta \omega_1 \cos(\omega_m t + 2\pi / 3) \) and \( \omega_3(t) = \omega_0 + \Delta \omega_1 \cos(\omega_m t + 4\pi / 3) \). Modulation of the resonance frequencies lifts the degeneracy of the counter-rotating states \( \pm \) = \{1, \( e^{i2\pi / 3} \), \( e^{i4\pi / 3} \)\}, producing non-reciprocity with 100% modulation efficiency. \( \kappa \) is the coupling coefficient.

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1. Estep, N. A. et al. Magnetic-free non-reciprocity and isolation based on parametrically modulated coupled-resonator loops. *Nature Physics* 10 Fig. 1 a, b; 2014. E-mail: alu@mail.utexas.edu

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by dynamically modulating three identical resonant circuit tanks arranged in a loop and strongly coupled to each other, as in Fig. 1b. The resonant frequencies of the individual tanks are temporally modulated in a circularly rotating fashion as 
\[
\omega_1(t) = \omega_0 + \delta \omega_m \cos(\omega_0 t + 2\pi t/3) \quad \text{and} \quad \omega_3(t) = \omega_0 + \delta \omega_m \cos(\omega_0 t - 2\pi t/3),
\]
where \( \omega_0 \) is the static value of the resonant frequency, \( \delta \omega_m \) is the modulation amplitude and \( \omega_0 \) is the modulation frequency, so that an effective electronic spin is imparted to the system. Without modulation, the loop supports two degenerate counter-rotating modes, similar to the uniform ring of Fig. 1a. However, when the modulation is switched on, this degeneracy is lifted and non-reciprocity is induced. As we show in the following, this solution markedly boosts the modulation efficiency of the device compared to the case of a single modulated resonant ring, as considered in refs 2,3, largely relaxing the requirements in terms of the modulation intensity and subsequently improving the overall efficiency of the structure.

In the absence of modulation \( (\delta \omega_m = 0) \), the loop of Fig. 1b supports three resonant states: a common state with state vector \( |c\rangle = |1 1 1\rangle \) and frequency \( \omega_c = \omega_0 + 2\kappa \), and two degenerate right- and left-handed states with state vectors \( |\pm\rangle = \left[ e^{i2\pi m/3} \ e^{i2\pi k/3} \right] \) and frequencies \( \omega_\pm = \omega_0 \pm \kappa \), where \( \kappa \) is the coupling coefficient. The applied modulation mixes right- and left-handed states, producing two new hybrid states

\[
\begin{align*}
|R\rangle &= |+\rangle e^{-i\omega_c t} - \frac{\Delta \omega}{\delta \omega_m} |-\rangle e^{-i(\omega_c - \omega_\pm) t} \\
|L\rangle &= |-\rangle e^{-i\omega_c t} + \frac{\Delta \omega}{\delta \omega_m} |+\rangle e^{-i(\omega_c + \omega_\pm) t}
\end{align*}
\]

(1)

where \( \Delta \omega = \sqrt{\omega_c^2 + 4\delta \omega_m^2} - \omega_c \), \( \omega_\pm = \omega_c \pm \Delta \omega/2 \), as analytically derived in the Methods for \( \omega_m \ll \omega_c \).

It is interesting to observe that both \( |R\rangle \) and \( |L\rangle \) consist of a dominant state at \( \omega_c \pm \) and a secondary state, red- or blueshifted by \( \omega_m \), as in the case of the uniformly modulated ring of refs 2,3. However, despite this apparent resemblance in the form of \( |R\rangle \) and \( |L\rangle \), the mechanism that creates the frequency separation \( \Delta \omega \) between resonant states in the geometry analysed here is significantly different from the uniformly modulated ring of refs 2,3. For a uniform resonant ring (Fig. 1a), \( \Delta \omega \) is the result of an azimuthally travelling wave modulation \( \Delta \omega_m \cos(\omega_0 t - l \omega_0^2) \), where \( \Delta \omega_m \) and \( l \) are the modulation amplitude and azimuthal order, respectively. If \( l = 2 \), the resonant order of the ring, \( \delta \omega_m = \omega_m \Delta \omega_m/(2\kappa) \) (refs 2,3), where \( \omega_m \) is the resonant frequency and \( \kappa \) the static permittivity. The ideal continuous modulation assumed in Fig. 1a (top) is difficult, if not impossible, to realize, and an angular discretization is typically required. A discrete modulation profile with \( N \) different modulation regions, as sketched in Fig. 1a (bottom), is equivalent to a continuous effective modulation with reduced effective amplitude \( \Delta \omega_m \approx \Delta \omega_m \text{sinc}(2\pi N) \) (ref. 3), revealing a fundamental trade-off between fabrication complexity, proportional to \( N \), and non-reciprocal response. As an example, for \( N = 3 \)—that is, the minimum value for which \( \Delta \omega_m \neq 0 \)—and \( l = 50 \), a typical value in realistic high-Q micro-ring resonators at 1.55\( \mu \text{m} \), \( \Delta \omega_m = 0.008 \Delta \omega_m \), implying that only 0.8% of the modulation signal is effectively used to generate non-reciprocity.

In contrast, in the composite resonant loop of Fig. 1b the frequency splitting is achieved by modulating the frequency of each resonator, which can be obtained by applying a uniform permittivity modulation with amplitude \( \Delta \omega_m \) all across each resonator\(^2\), leading to \( \Delta \omega_m = \omega_m \Delta \omega_m/(2\kappa) \), as shown in the Methods. Remarkably, in this topology the entire modulation signal is used to produce the frequency separation \( \Delta \omega \), indicating that maximum (unitary) modulation efficiency is achieved in a simple fabrication scheme requiring only three independent modulation regions.

We realized the structure of Fig. 1b at RF using three basic L–C circuit tanks, as in Fig. 2a, where the capacitance \( C \) is equally distributed on both sides of the inductance \( L \) to maintain a symmetric structure (see Supplementary Methods for a full schematic of the realized circuit). The resonance frequency modulation is achieved by means of capacitance modulation, commonly obtained in RF with varactor diodes. These diodes are biased by two signals, a static signal \( V_{dc} \), which provides the required reverse bias and controls the static capacitance, and a RF signal \( V_m(t) \) with frequency \( \omega_m \) and amplitude \( V_m \), providing the time modulation. Assuming that the resonators are coupled to each other through capacitances \( C \), as in Fig. 2b, the frequencies of the common and rotating states are \( \omega_0 = \omega_0/\sqrt{1+2C/L} \) and \( \omega_\pm = \omega_0 \sqrt{(C+3C/2)/(C+2C)} \), respectively, where \( \omega_0 = 1/\sqrt{LC} \) is the static resonance frequency of each tank. Then, if the amplitude of the capacitance modulation is \( \Delta C_m \), the frequency modulation...
amplitude is found as \( \delta \omega_m = \omega_0 \Delta C_m / (2C) \). The frequency \( \omega_0 \) should be designed to be as far as possible from \( \omega_m \) in order for the common mode not to affect the operation of the structure at \( \omega_m \), at which non-reciprocity occurs. In the lumped-element circuit of Fig. 2b this condition is satisfied by taking \( C_m \rightarrow \infty \), or equivalently by coupling the tanks through short circuits, yielding \( \omega_0 = 0 \) and \( \omega_m = \omega_0 \sqrt{3}/2 \).

The non-reciprocal response of the circuit of Fig. 2b is demonstrated by capacitively coupling it to three microstrip transmission lines, realizing a three-port device. Exciting the structure from, for example, port 1 at frequency \( \omega_1 \) results in the excitation of \( [R] \) and \( [L] \) with the same amplitude and opposite phase \( \phi_2 = -\phi_4 \), owing to the symmetrical distribution of these states around \( \omega_m \). Then, the signals at ports 2 and 3 are proportional to \( e^{i2\delta/\delta x} e^{i\phi_1} + e^{-i2\delta/\delta x} e^{-i\phi_1} \) and \( e^{-i2\delta/\delta x} e^{i\phi_4} + e^{i2\delta/\delta x} e^{-i\phi_4} \), respectively, as the superposition of \( [R] \) and \( [L] \) at these ports. If \( \delta \omega_m \) and \( \omega_m \) are selected so that \( \phi_3 = \phi_4 = \pi/6 \), the signal at port 3 is identically zero, while the signal at port 2 is non-zero, routing the incident power from port 1 to port 2. Owing to the symmetry of the structure with respect to its ports, incident power from ports 2 and 3 is similarly routed to ports 3 and 1, and thus realizing the functionality of a non-reciprocal circulator with infinite isolation. Notice that the above description assumes a weak excitation of the common state, which makes clear the importance of choosing its resonance frequency as far as possible from the resonance frequency of the rotating states.

The realized device was designed to resonate at 170 MHz with a Q-factor of about 10 for \( V_{dc} = 1.99 \text{ V} \) and \( V_m = 0 \). The modulation frequency was set to 15 MHz, in order for the intermodulation by-products at frequencies \( \omega \pm \omega_m \) created by the secondary substates of \( [R] \) and \( [L] \), to fall outside the resonance band, whose bandwidth is here around 10 MHz. The exact values of the circuit components and its full topology are provided in the Methods and Supplementary Methods. Figure 2c shows a photograph of the fabricated prototype. We underline here the deeply subwavelength size of the realized device (\( \sim \lambda/75 \)), simply based on three lumped resonant circuit tanks.

Without modulation, the signal is equally split at the two output ports, as expected from symmetry, and the system is fully reciprocal (Fig. 3a). When the modulation signal is switched on, the symmetry is broken and power is unequally split. By varying the modulation amplitude it is possible to find a value for which the signal entering port 1 is routed exclusively to port 2, corresponding to \( \phi_3 = -\phi_4 = \pi/6 \). This condition is satisfied for \( V_m = 0.6 \text{ V} \), as can be seen in Fig. 3b: at the resonance frequency of 170 MHz, power incident to ports 1, 2 and 3 is routed to ports 2, 3 and 1, respectively, demonstrating the operation of an ideal, magnetic-free, deeply subwavelength linear circulator. For comparison, Fig. 3c shows the S-parameters obtained using full-wave and circuit simulations: the agreement with the measurement is excellent.

To get a deeper insight into the effect of \( V_m \) on the device operation, Fig. 4a shows the transmission between ports 1 and 2 at resonance versus \( V_m \). For \( V_m = 0 \), \( S_{21} = S_{31} \), as expected. Increasing \( V_m \) results in an increase of \( S_{21} \) and a decrease of \( S_{12} \) until \( V_m = 0.6 \text{ V} \), where \( S_{12} = 0 \). Past this point, \( S_{12} \) and \( S_{21} \) get closer, as expected when we depart from the destructive interference condition. For very large values of \( V_m \), \( S_{21} \) and \( S_{12} \) both tend to zero, because the counter-rotating states move far from \( \omega_m \) and, therefore, are weakly excited at \( \omega_m \). The magnitude of the asymmetry between \( S_{21} \) and \( S_{12} \) is measured by the isolation \( |S_{21}/S_{12}| \), plotted in Fig. 4b on a logarithmic scale versus \( V_m \). At the optimum modulation voltage \( V_m = 0.6 \text{ V} \), \( S_{12} \) is over four orders of magnitude larger than \( S_{21} \), indicating giant non-reciprocity, well above the levels of any commercial magnetic-based device.

Another unique property of the proposed device consists in its real-time tunability features. The biasing voltage \( V_{dc} \), which provides the reverse biasing condition for the varactor diodes, determines their static capacitance. Therefore, \( V_{dc} \) can be used to actively control the static resonance frequency of the \( L-C \) tanks, and consequently the frequency band over which non-reciprocity occurs. Figure 4c shows the measured isolation versus frequency for \( V_m \) varied between 1.73 V and 4.5 V. The non-reciprocal response of our device can be efficiently tuned between 150 MHz and 210 MHz, corresponding to a relative bandwidth of over 30%. Across all this range, our measured isolation is above 40 dB. This strong tuning capability is an additional advantage of the proposed device compared to conventional magnetic-based microwave circulators, and it may be exploited in scenarios requiring dynamic tuning to balance changes in temperature or in the environment. The electronic spin applied to the proposed coupled-resonator loop realizes the equivalent of a dynamically tunable, strongly biased ferromagnetic metamaterial substrate.

In addition to being an ideal replacement for microwave non-reciprocal components, with significant advantages in terms of size, integration, cost, linearity, tunability and noise reduction, our findings may become even more important when applied to different frequencies or other types of waves, such as light or sound. For instance, this concept may be disruptive for integrated nanophotonic technology, for which optical non-reciprocal components are critical for laser protection and signal routing. At visible frequencies, electro-optic modulation in silicon-based components is typically achieved by means of carrier injection/depletion\(^{24,25}\), which can provide relatively strong permittivity modulation, but is typically accompanied by significant loss and low modulation frequencies for large modulation amplitudes. These side effects impose limitations...
on the applicability of the principle of angular-momentum biasing in uniform micro-ring resonators, as discussed before. In contrast, the concept presented here ensures maximum modulation efficiency, significantly relaxing the requirements in terms of modulation amplitude. This in turn allows large quality factors and large modulation frequencies, which translate into strong non-reciprocal response in deeply subwavelength devices. We also envisage the realization of the proposed rotating modulation of coupled-resonator loops in photonic crystal technology, for which high-Q-factor coupled cavities may be implemented and efficiently modulated. Our study also represents a new demonstration of the exciting possibilities offered by dynamic modulation of coupled-resonator networks, with unique control over the flow of light, in the context of recently presented concepts of photonic topological edge states and effective magnetic fields for photons.

Methods

Modes of the coupled-resonators loop. The coupled-mode equations of the system of Fig. 1 read

\[
\begin{align*}
\dot{a}_1 &= -i\omega_1 a_1 - i\kappa a_2 - i\kappa a_3 \\
\dot{a}_2 &= -i\omega_2 a_2 - i\kappa a_3 - i\kappa a_1 \\
\dot{a}_3 &= -i\omega_3 a_3 - i\kappa a_1 - i\kappa a_2
\end{align*}
\]

(2)

where \(a_1, a_2, a_3\) are the complex amplitudes of the three resonators. Equation (2) can be written in the more compact form

\[
\frac{d}{dt}|\psi\rangle = -i\Omega |\psi\rangle
\]

(3)

where \(|\psi\rangle = [a_1 \quad a_2 \quad a_3]^T\) is the state vector of the system and

\[
\Omega = \begin{bmatrix}
\omega_1 & \kappa & \kappa \\
\kappa & \omega_2 & \kappa \\
\kappa & \kappa & \omega_3
\end{bmatrix}
\]

In the absence of modulation, \(\omega_1, \omega_2, \omega_3\) and \(\omega_0\) are equal to \(\omega_0\). Then, the eigenfrequencies and the corresponding state vectors of the system are found by the eigenvalues and eigenvectors of \(\Omega\), respectively. In particular, it can be shown that there are three states, a common state with resonant frequency \(\omega_0 = \omega_0 + 2\kappa\) and state vector \(|\psi\rangle = (1/\sqrt{3}) [1 \ 1 \ 1]\), a right-handed rotating state with resonant frequency \(\omega_+ = \omega_0 - \kappa\) and state vector \(|+\rangle = (1/\sqrt{3}) [1 \ e^{i\pi/3} \ e^{i5\pi/3}]\), and a left-handed rotating state with resonant frequency \(\omega_- = \omega_0\) and state vector \(|-\rangle = (1/\sqrt{3}) [1 \ e^{i\pi/3} \ e^{i5\pi/3}]\). Note that because the eigenvalues \(\omega_+\) and \(\omega_-\) are degenerate, the eigenvectors \(|+\rangle\) and \(|-\rangle\) are not the only ones corresponding to these eigenvalues. As a matter of fact, any linear combination of \(|+\rangle\) and \(|-\rangle\), such as the vectors \([1 \ -1 \ 0]^T\) and \([1 \ 0 \ -1]^T\), are also valid eigenvectors of \(\omega_+\) and \(\omega_-\). However, hereafter, we will use \(|\pm\rangle\) and \(|\mp\rangle\), because they bear an immediate physical meaning as counter-rotating states of the coupled-resonators loop, and they significantly simplify the mathematical analysis.

In the presence of modulation \(\omega_0(t) = \omega_0 + \delta\omega_0 \cos(\delta\omega_0 t)\), \(\omega_+(t) = \omega_0 + \delta\omega_0 \cos(\delta\omega_0 t + 2\pi/3)\) and \(\omega_- (t) = \omega_0 + \delta\omega_0 \cos(\delta\omega_0 t + 4\pi/3)\) result in a time-dependent \(\Omega\). In this case, the eigenstates of the system cannot be found by the eigenvalues and eigenvectors of \(\Omega\), and a full solution of equation (3) is necessary. Because modulation constitutes a perturbation of the coupled system, it is convenient to express the eigenstates of the modulated system in terms of the eigenstates of the coupled non-modulated system. To this end, equation (3) is expressed in the basis of \(|\mp\rangle\), \(|\pm\rangle\) and \(|\mp\rangle\), by multiplying \(|\psi\rangle\) with the conjugate transpose of the matrix

\[
U = \frac{1}{\sqrt{3}} \begin{bmatrix}
1 & e^{i\pi/3} & e^{i5\pi/3} \\
1 & e^{i\pi/3} & e^{i5\pi/3} \\
1 & e^{i\pi/3} & e^{i5\pi/3}
\end{bmatrix}
\]

with columns the state vectors \(|\pm\rangle\), \(|\pm\rangle\) and \(|\mp\rangle\). In the new basis, \(|\psi\rangle = [a_+ \quad a_- \quad a_-]^T\), where \(a_+, a_-\) and \(a_-\) are the complex amplitudes of the common, right- and left-handed states, respectively, and

\[
\Omega = \Omega_0 + \delta\Omega
\]

where

\[
\Omega_0 = \begin{bmatrix}
\omega_0 & 0 & 0 \\
0 & \omega_0 & 0 \\
0 & 0 & \omega_0
\end{bmatrix}, \quad \delta\Omega = \frac{\delta\omega_0}{2} \begin{bmatrix}
0 & e^{-i\omega_0 t} & e^{i\omega_0 t} \\
e^{-i\omega_0 t} & 0 & e^{i\omega_0 t} \\
e^{i\omega_0 t} & e^{-i\omega_0 t} & 0
\end{bmatrix}
\]

(3)

If \(\omega_\pm \ll |\omega_+ - \omega_-|\), coupling between the common and rotating states, corresponding to the first row and column of \(\delta\Omega\), can be neglected and equation (3) simplifies to

\[
\begin{align*}
\dot{a}_+ &= \omega_0 a_+ + \frac{\delta\omega_0}{2} e^{i\omega_0 t} a_- \\
\dot{a}_- &= \omega_+ a_+ + \frac{\delta\omega_0}{2} e^{i\omega_0 t} a_- \quad \text{and} \quad \dot{a}_- = \omega_- a_+
\end{align*}
\]

(4)

It can be seen that equation (4) is satisfied if

\[
\begin{align*}
a_+ &= A_- e^{-i\omega_0 t} \\
a_- &= A_+ e^{i\omega_0 t}
\end{align*}
\]

where \(A_+, A_-\) and \(\omega_0\) are constants. Then, equation (4) becomes

\[
\begin{bmatrix}
\omega_0 \\
\delta\omega_0/2 \\
\omega_0 + \omega_0
\end{bmatrix} \begin{bmatrix}
A_+ \\
A_- \\
A_-
\end{bmatrix} = \omega_0 \begin{bmatrix}
A_+ \\
A_- \\
A_-
\end{bmatrix}
\]
which is an eigenvalue problem with respect to $\omega$. The eigensolutions of this problem yield the eigenstates of the modulated system, as given by equation (1).

Modulation amplitude of the coupled-resonators system. We assume a resonator whose modal distribution fully resides in materials with permittivity $\varepsilon$, permeability $\mu$, and resonant frequency $\omega_0$. It can be shown from perturbation theory that a small change $\Delta \varepsilon$ of the permittivity results in the following change of the resonance frequency

$$\omega - \omega_0 \approx -\omega_0 \frac{\int \Delta \varepsilon |E|^2 \, dV}{\int \varepsilon |E|^2 + \mu |H|^2} \, dV$$

where $E$ and $H$ are the resonant electric and magnetic field, respectively, and integration is performed over all the volume of the resonator. Furthermore, it is known that at resonance the electric and magnetic energies are equal, hence $\int \varepsilon |E|^2 \, dV = \mu |H|^2 \, dV$ and

$$\omega - \omega_0 \approx -\frac{\omega_0}{2} \int \Delta \varepsilon |E|^2 \, dV$$

Thus, the frequency modulation $\Delta \omega_0$ is equal to $\delta \omega_0 = \omega_0 \Delta \varepsilon / (2\varepsilon)$.

Description of the experimental set-up. The complete experimental set-up is shown in Supplementary Fig. 2 and a list of the associated equipment is provided in Supplementary Table 2. A waveform generator provides the modulation signal, which is split into three equal parts by means of a power divider. The output signals are then led to three phase shifters, which provide the required phase modulation of the coupled-resonators system.

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Author contributions
N.A.E. performed the experiment. D.L.S. and N.A.E. designed the structure and conducted the numerical calculations and theoretical modelling. J.S. helped in the selection and modelling of the modulation varactors. A.A. directed and supervised the project. All authors have read and commented on the paper.

Additional information
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Competing financial interests
The authors declare no competing financial interests.